

Introduction to Brain Network Modeling

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Abstract

Diffusion tensor imaging offers a unique opportunity to characterize the structural connectivity of the human brain non-invasively by tracing white matter fiber tracts. Whole brain tractography studies routinely generate up to half million tracts per brain, which serves as edges in an extremely large 3D graph with up to half million edges. Currently there is no agreed-upon method for constructing the brain structural network graphs out of large number of white matter tracts. In this paper, we review basics of structural brain network modeling and discuss various challenges.

Outline

fMRI connectivity

DTI connectivity

PET connectivity

in autism

NIH Launches the Human Connectome Project to Unravel the Brain's Connections

The National Institutes of Health Blueprint for Neuroscience Research is launching a \$30 million project that will use cutting-edge brain imaging technologies to map the circuitry of the healthy adult human brain. By systematically collecting brain imaging data from hundreds of subjects, the Human Connectome Project (HCP) will yield insight into how brain connections underlie brain function, and will open up new lines of inquiry for human neuroscience.

www.humanconnectomeproject.org

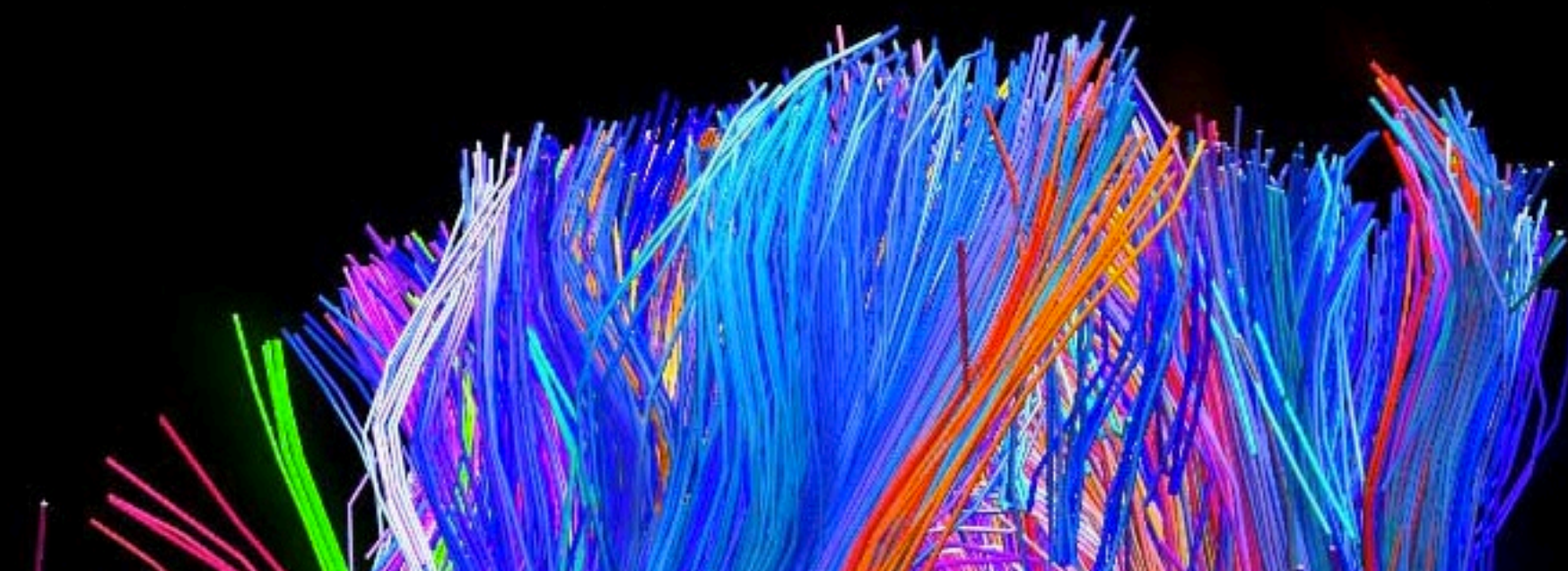
The NIH Human Connectome Project

Harvard/MGH-UCLA Consortium

WU-Minn Consortium

Neuroscience Blueprint

Human Connectome Project

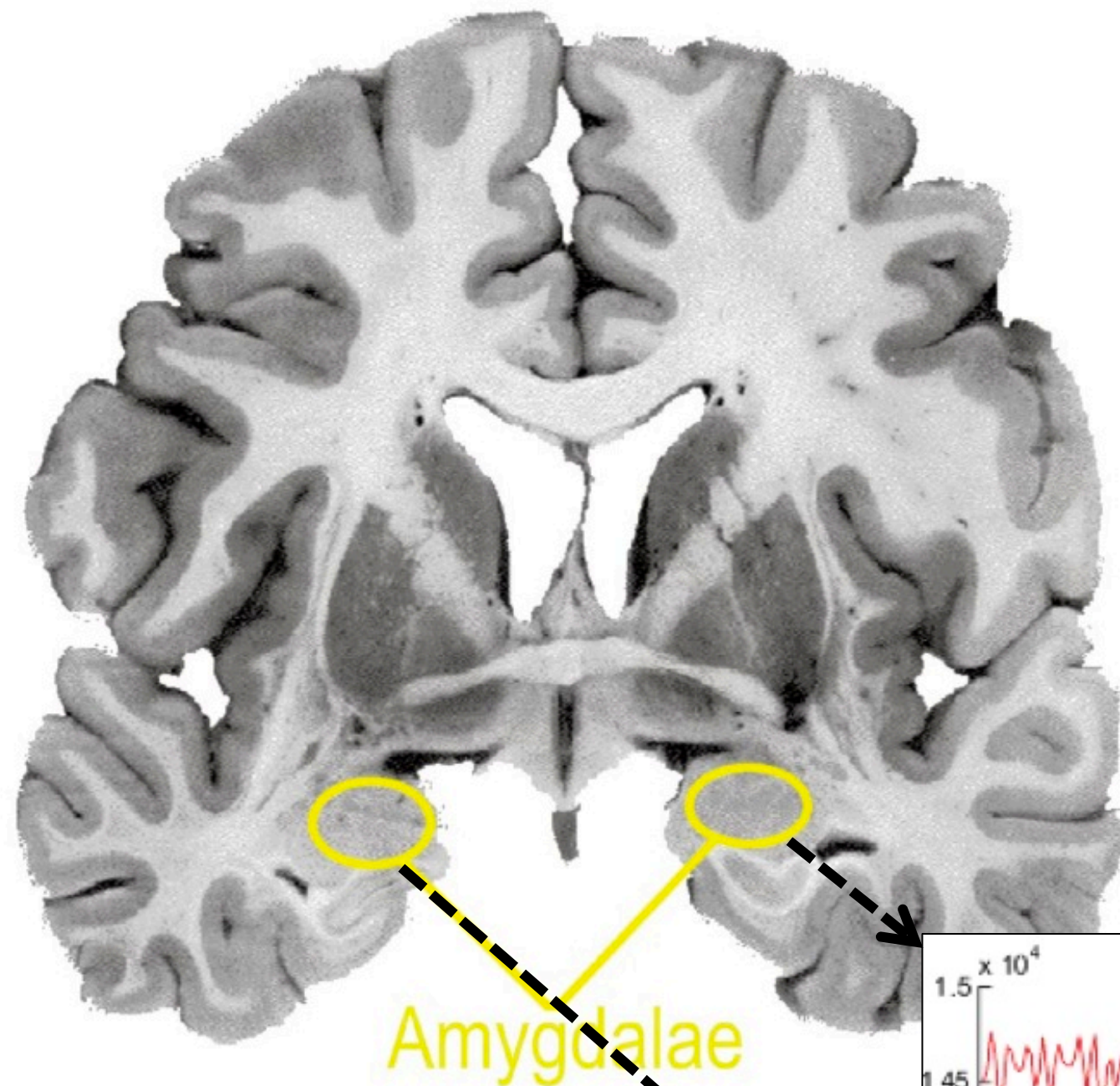
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The Human Connectome Project

Navigate the brain in a way that was never before possible; fly through major brain pathways, compare essential circuits, zoom into a region to explore the cells that comprise it, and the functions that depend on it.

The Human Connectome Project aims to provide an unparalleled compilation of neural data, an interface to graphically navigate this data and the opportunity to

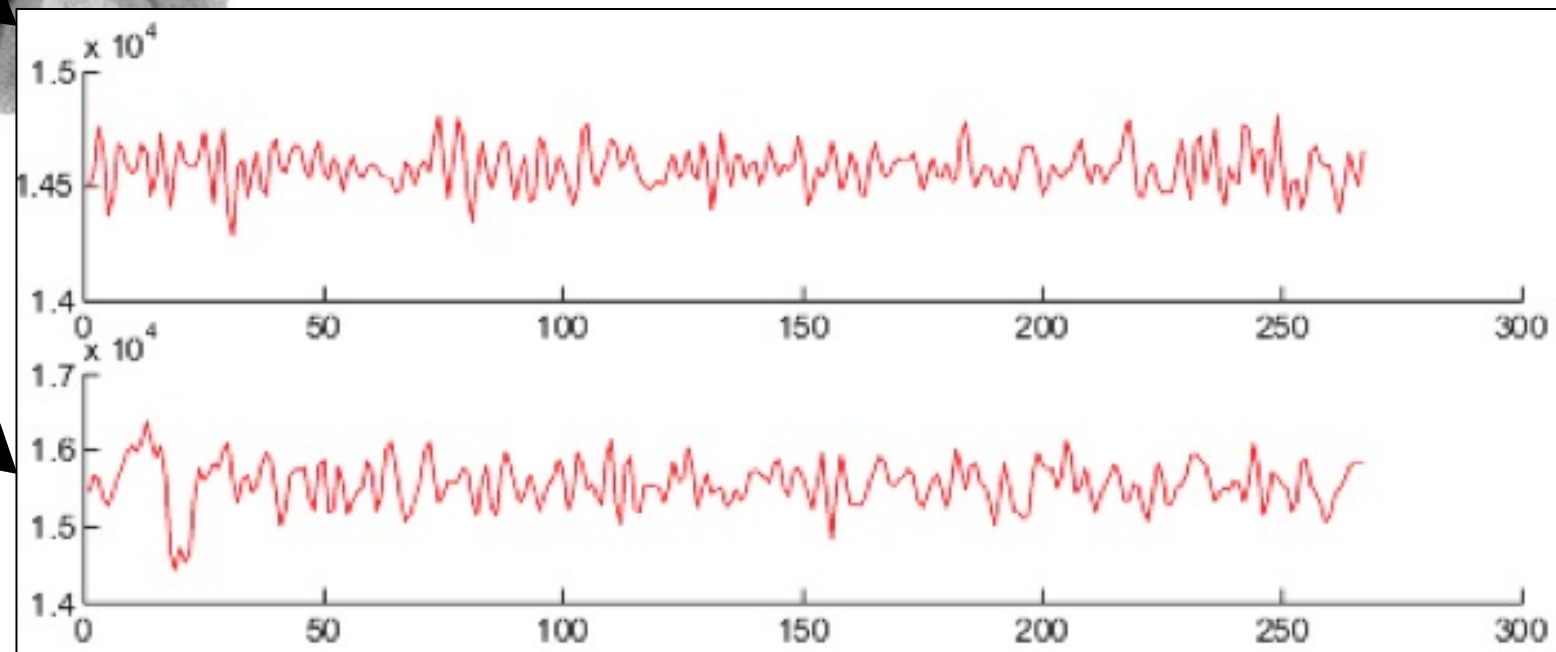
Functional magnetic resonance imaging (fMRI)



Amygdalae

Specialized MRI scan used to measure the hemodynamic response (change in blood flow) in the brain.

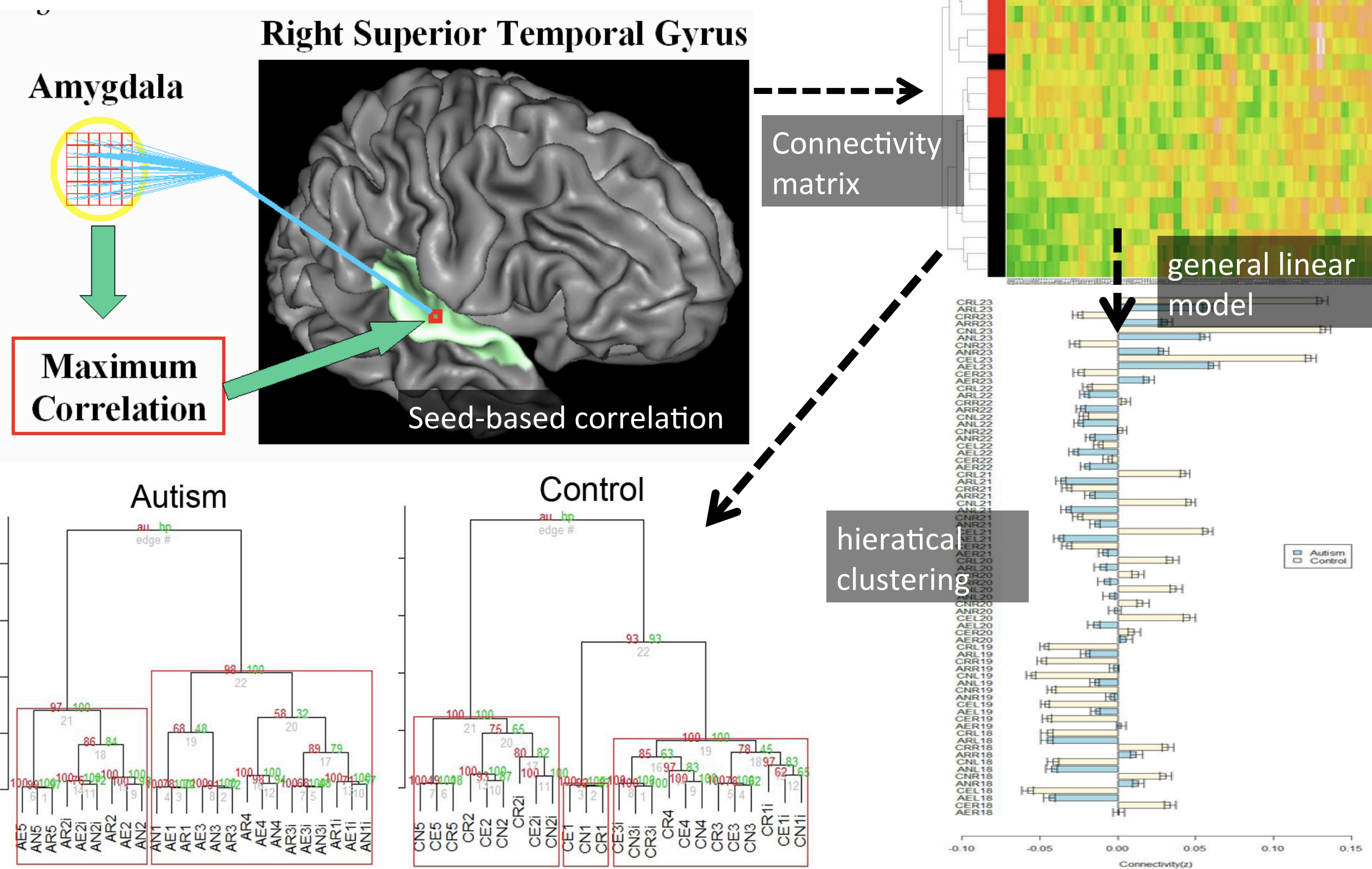
fMRI gives time series data at about 4-8mm image resolution.



Davidson and Irwin, 1999

functional (fMRI) connectivity study

D.J. Kelley 2008 PhD thesis

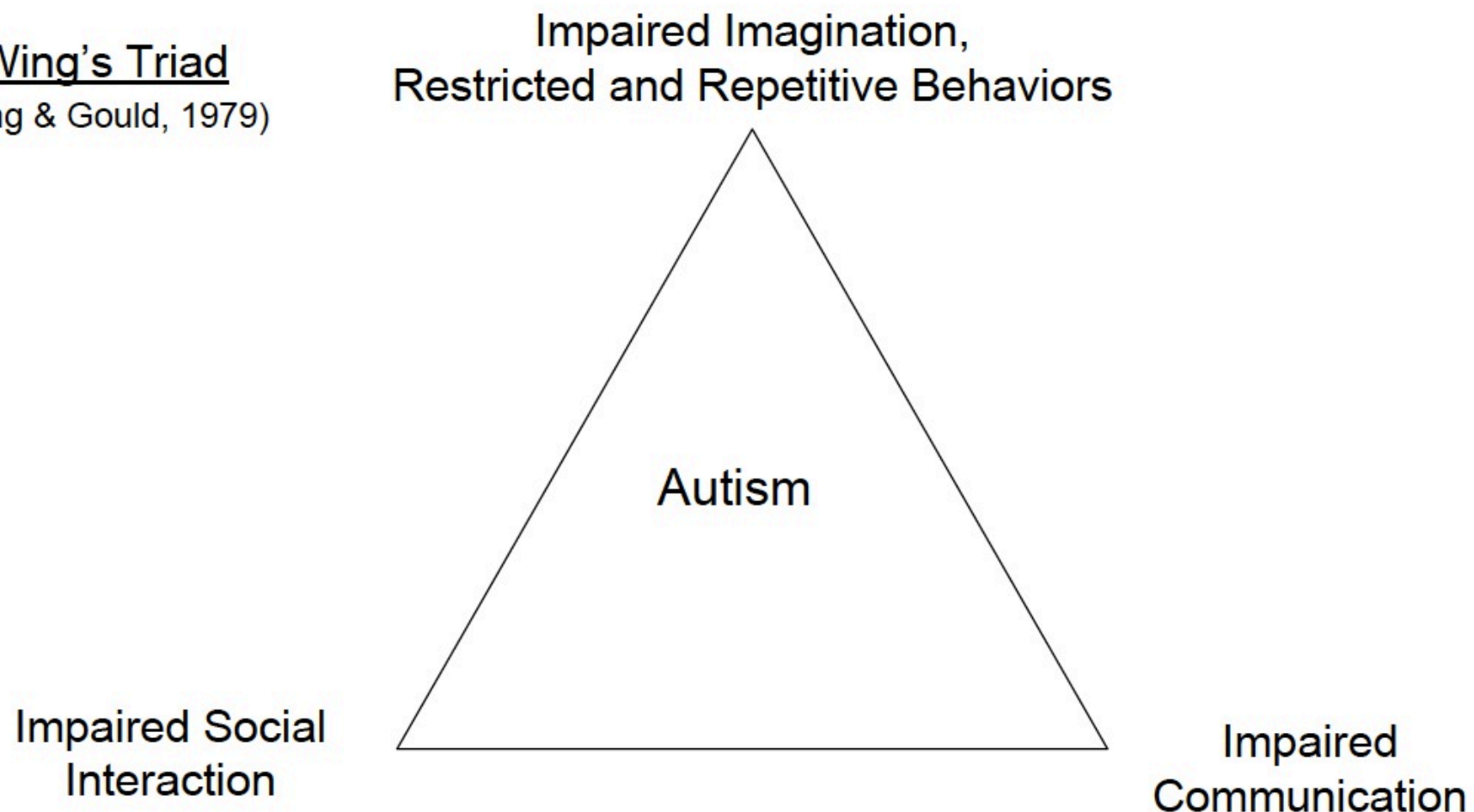


Brain connectivity study in autism

Autism (자폐증) is a developmental disorder.
About 9 per 1000 children in US.

Autism is Behaviorally Defined

Wing's Triad
(Wing & Gould, 1979)



DSM-IV-TR classifies Autism by deficits in these three domains.

Cerebral cortex -

a thin layer of gray matter on the surface of the cerebral hemispheres. Two-thirds of its area is deep in the fissures or folds. Responsible for the higher mental functions, general movement, perception, and behavioral reactions.

Amygdala - responsible for emotional responses, including aggressive behavior.

Hippocampus - makes it possible to remember new information and recent events.

Basal ganglia -

gray masses deep in the cerebral hemisphere that serves as a connection between the cerebrum and cerebellum. Helps to regulate automatic movement.

Major Brain Structures Implicated in Autism

Brain stem -

located in front of the cerebellum, it serves as a relay station, passing messages between various parts of the body and the cerebral cortex. Primitive functions essential to survival (breathing and heart rate control) are located here.

Corpus callosum -

consists primarily of closely packed bundles of fibers that connect the right and left hemisphere and allows for communication between the hemispheres.

Cerebellum -

located at the back of the brain, it fine tunes our motor activity, regulates balance, body movements, coordination, and the muscles used in speaking.

AUTISM

Persons with autism may possess the following characteristics in various combinations and in varying degrees of severity.



Inappropriate laughing or giggling



No real fear of dangers



Apparent insensitivity to pain



May not want cuddling



Sustained unusual or repetitive play; Uneven physical or verbal skills



May avoid eye contact



May prefer to be alone



Difficulty in expressing needs; May use gestures



Inappropriate attachments to objects



Insistence on sameness



Echoes words or phrases



Inappropriate response or no response to sound



Spins objects or self



Difficulty in interacting with others

1-800-3AUTISM

Autism Society of America

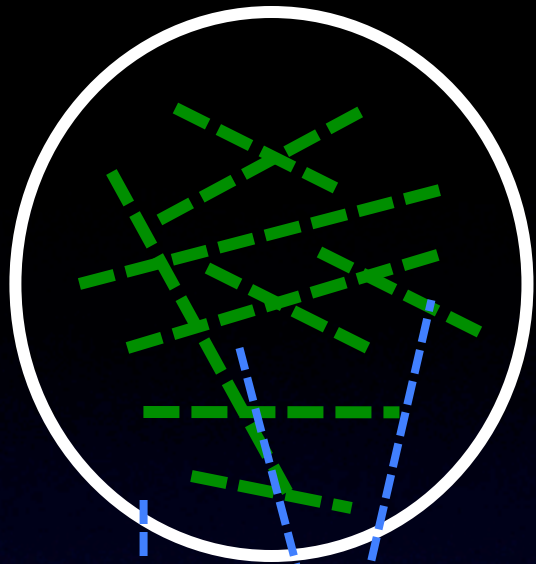
7910 Woodmont Avenue, Suite 650 Bethesda, MD 20814-3015

January is National Autism Awareness Month.

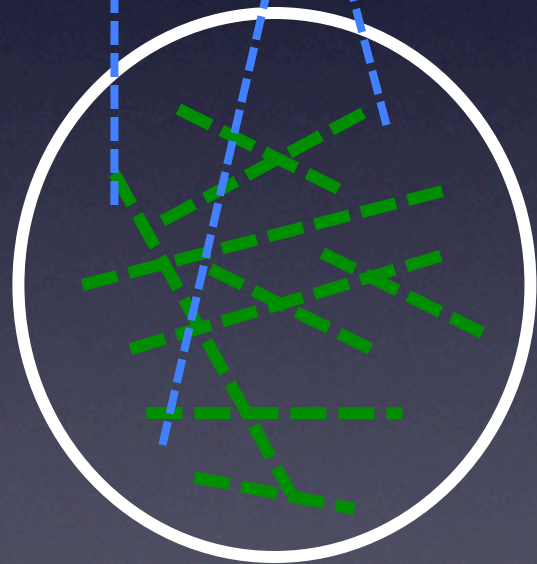
Adapted from original by: Professor Rennie-Short, University of Queensland, Brisbane Children's Hospital, Australia.

Known connectivity hypothesis in autism

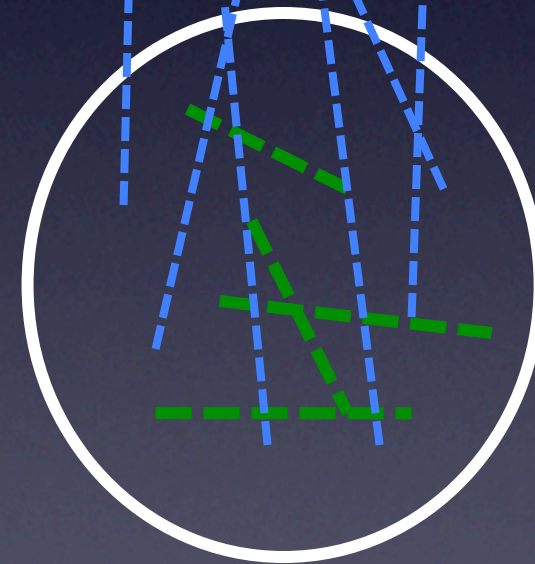
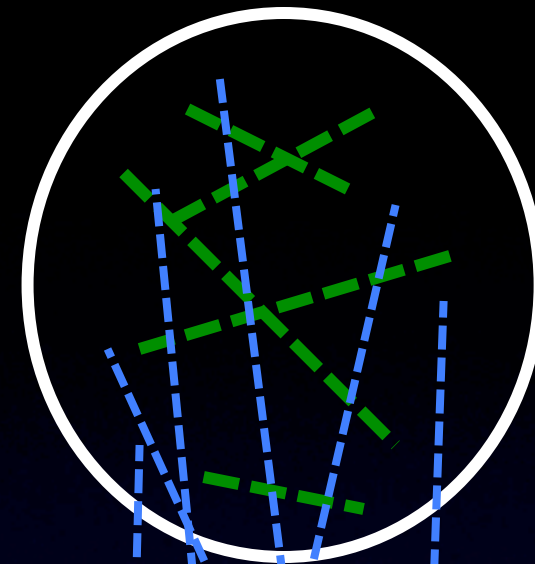
Lobe 1



Lobe 2



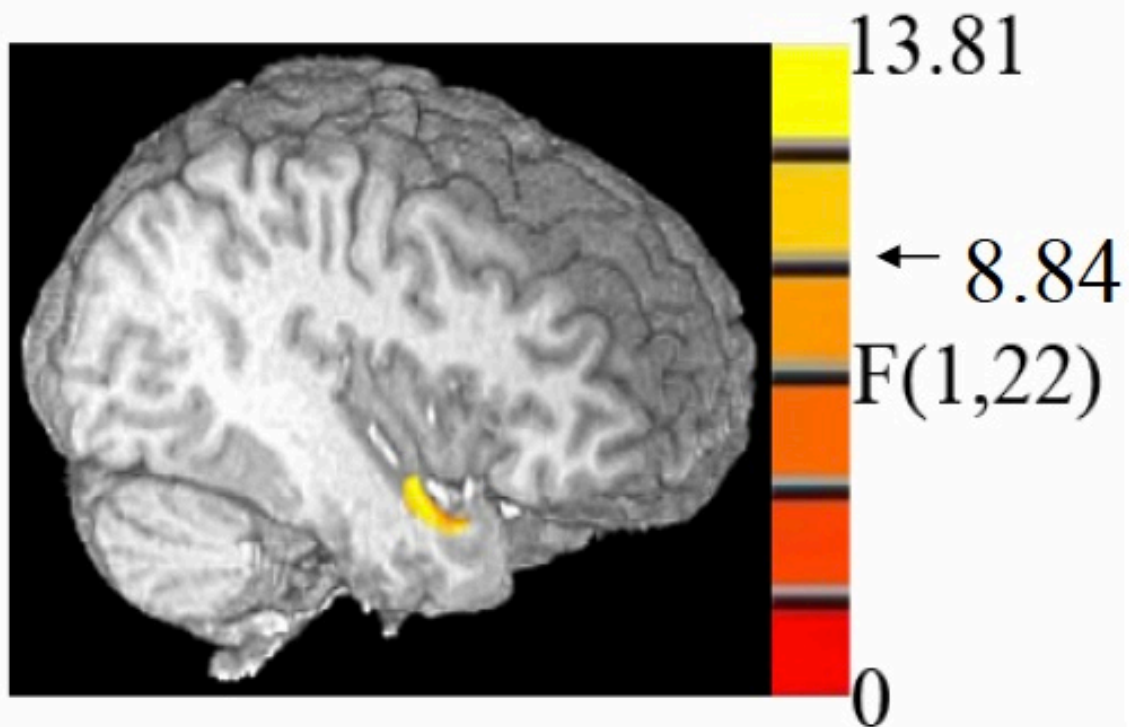
Local overconnectivity
global underconnectivity



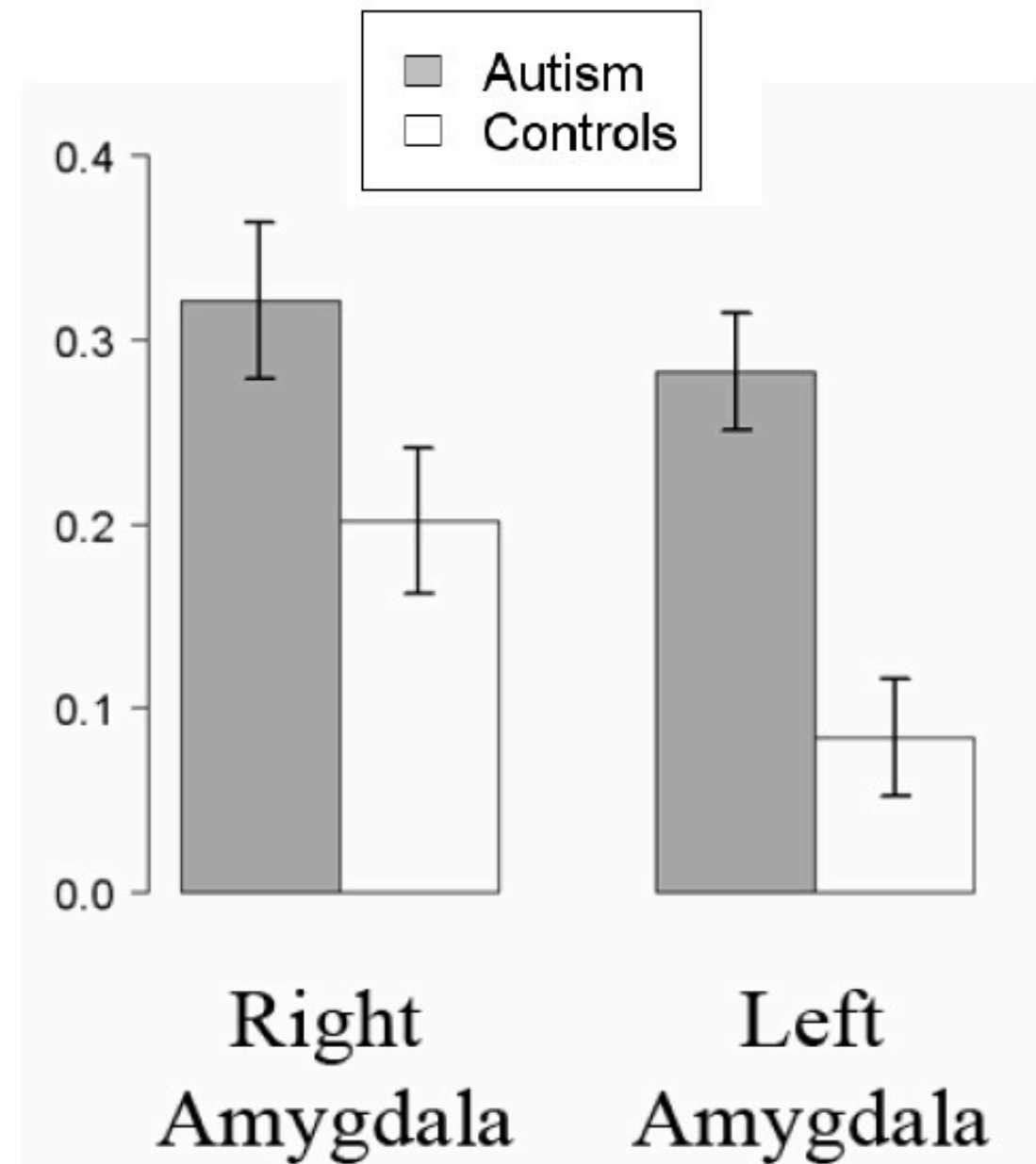
Normal controls

Abnormal functional (fMRI) connectivity in autism

Right Superior Temporal Gyrus



Functional Connectivity



$t(22)=2.06, p=0.052$

$t(22)=4.425, p=0.0021$

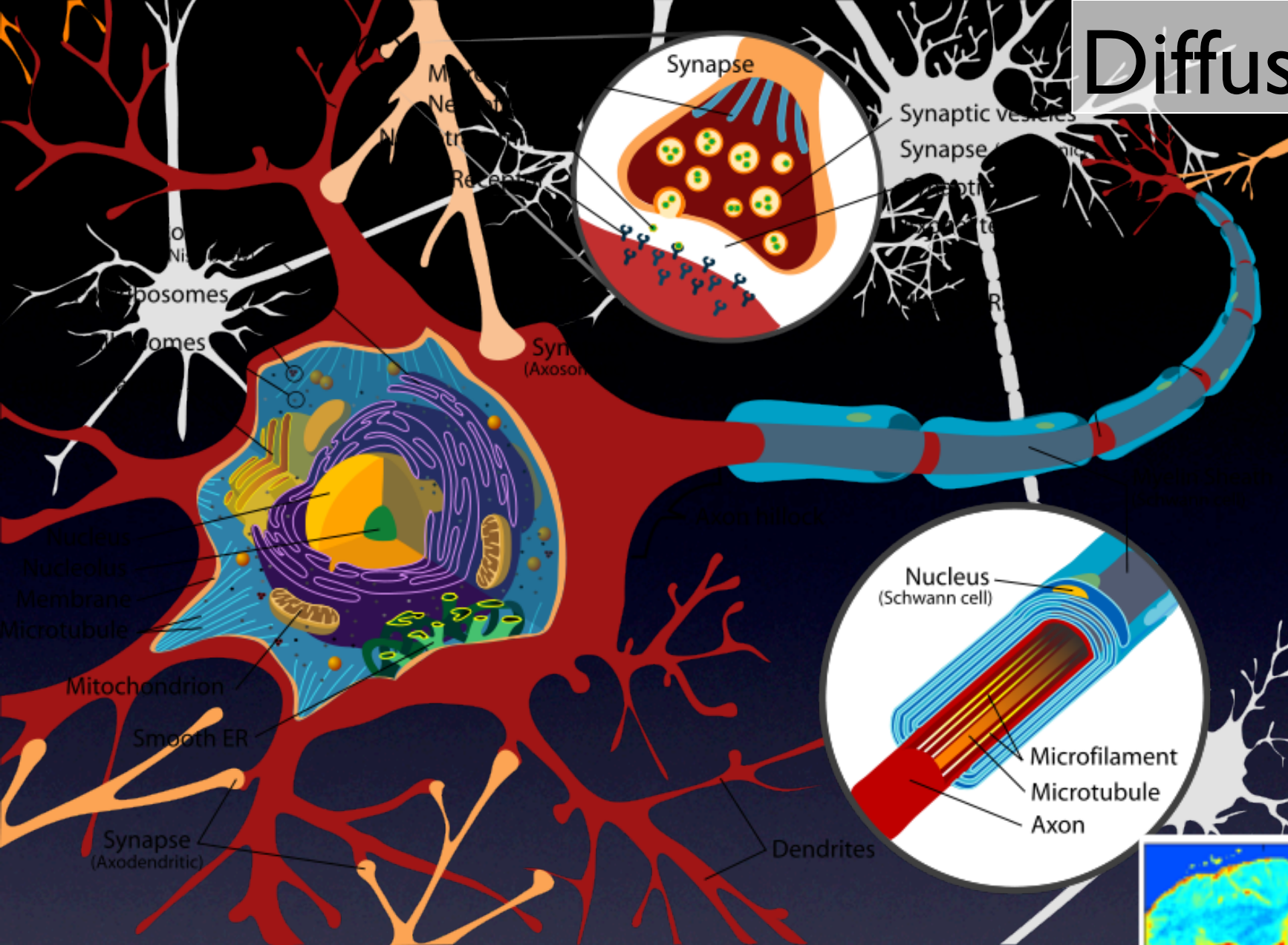
What is wrong with functional connectivity studies?

Where is the physical evidence of connection?
Lack of underlying biological mechanism

What do we really need?

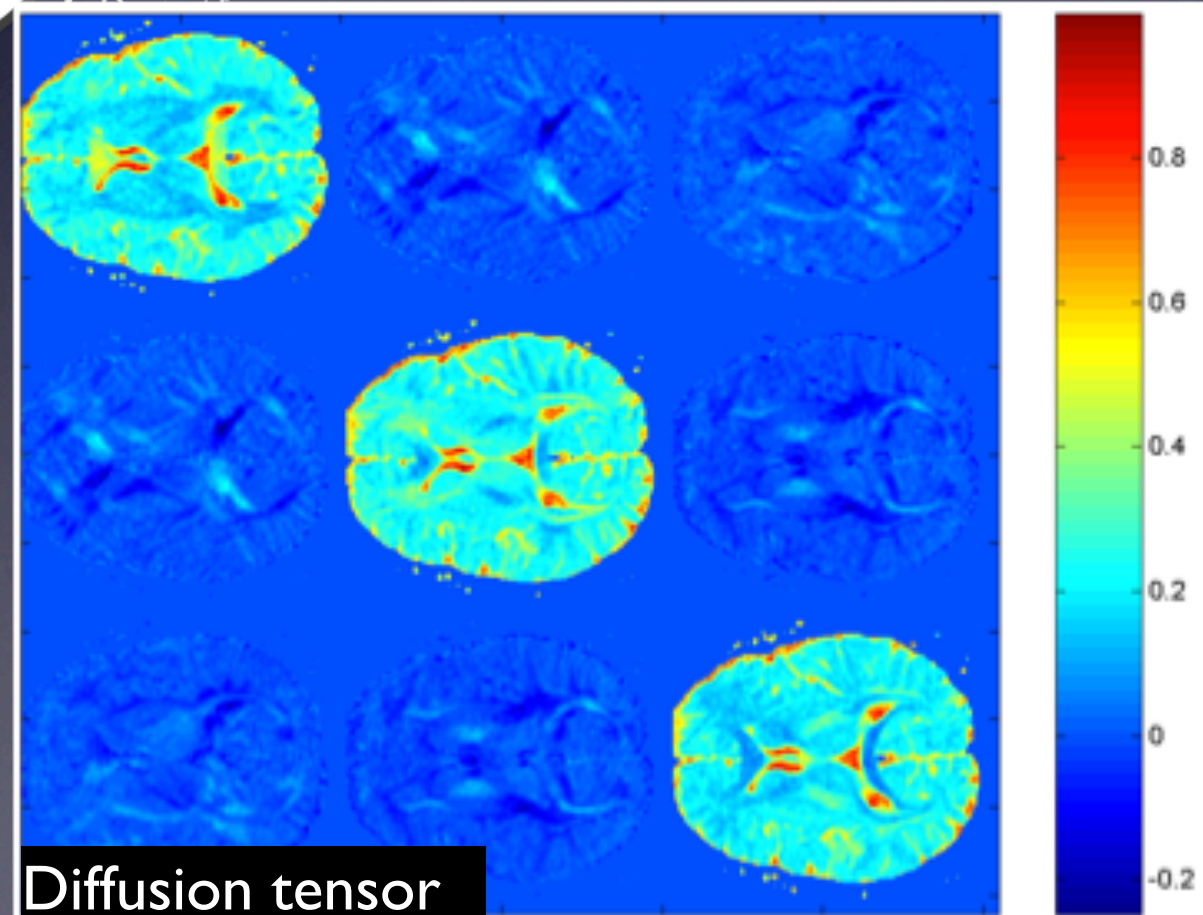
-- Anatomical basis of connections

Diffusion Tensor Imaging

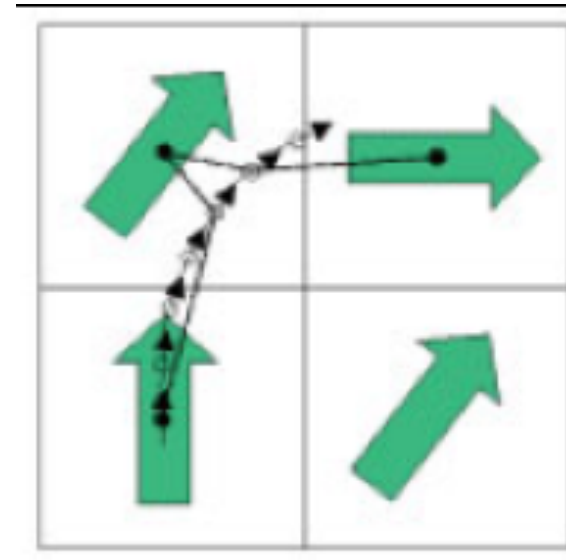
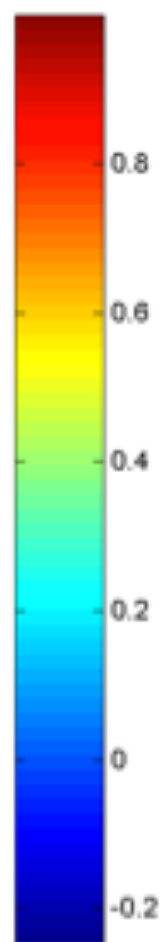
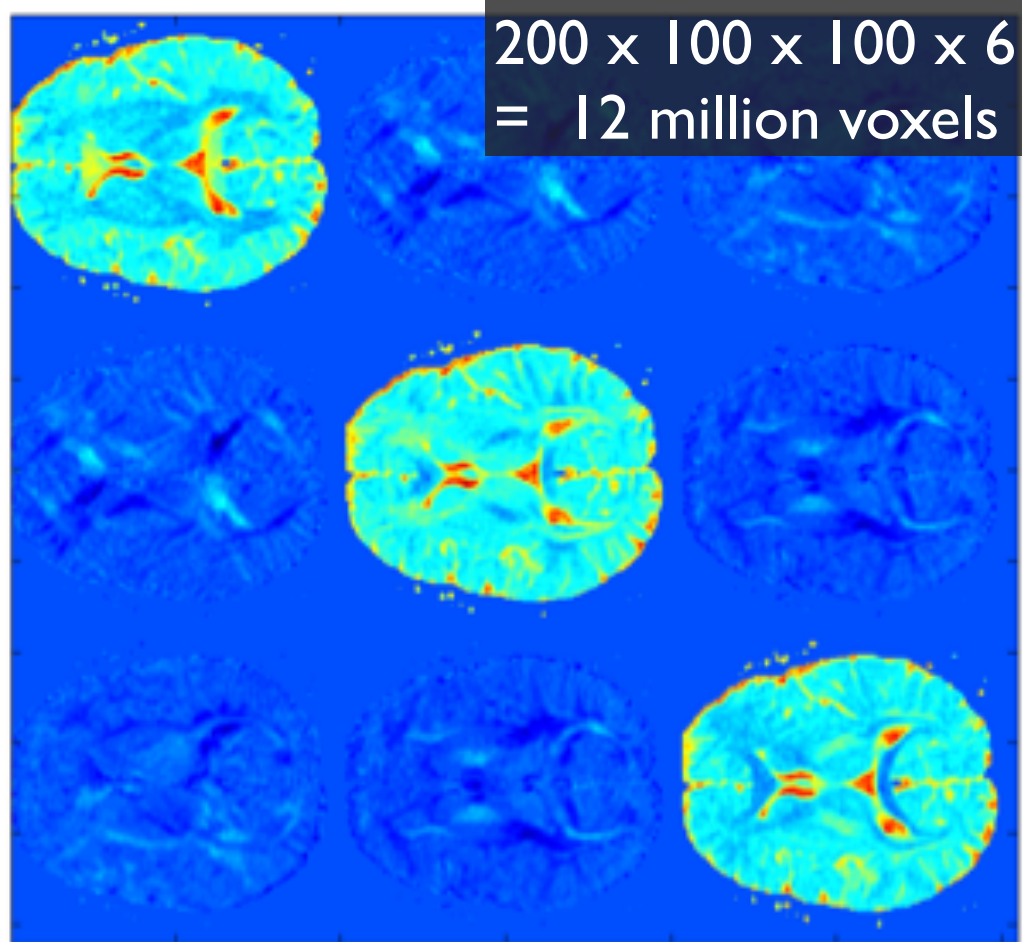


The movement of anisotropic water diffusion can be measured using DTI.

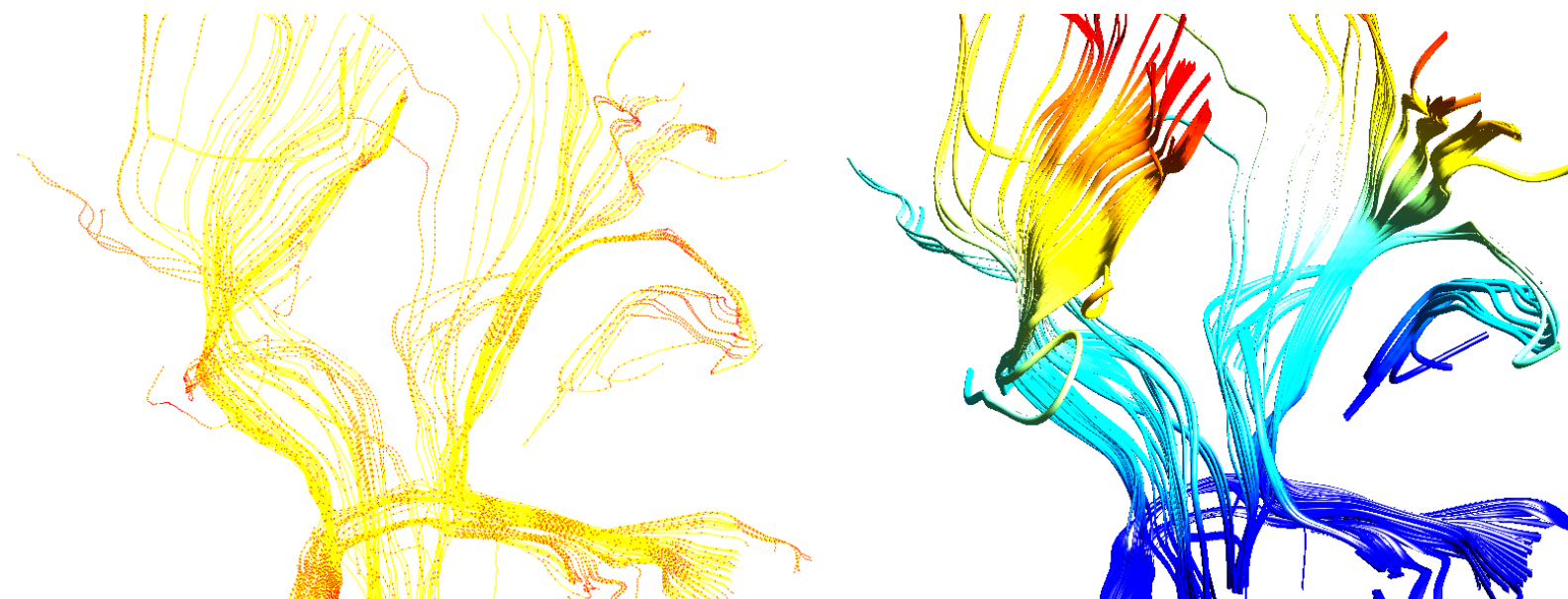
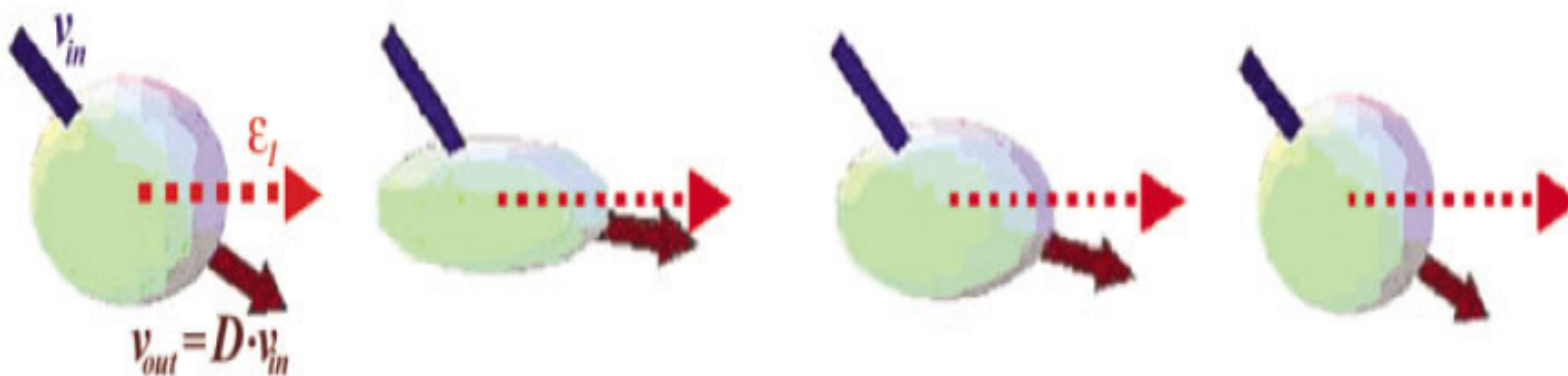
The direction of neuronal filaments in the axon dictates the movement of water diffusion.



Fiber Tractography



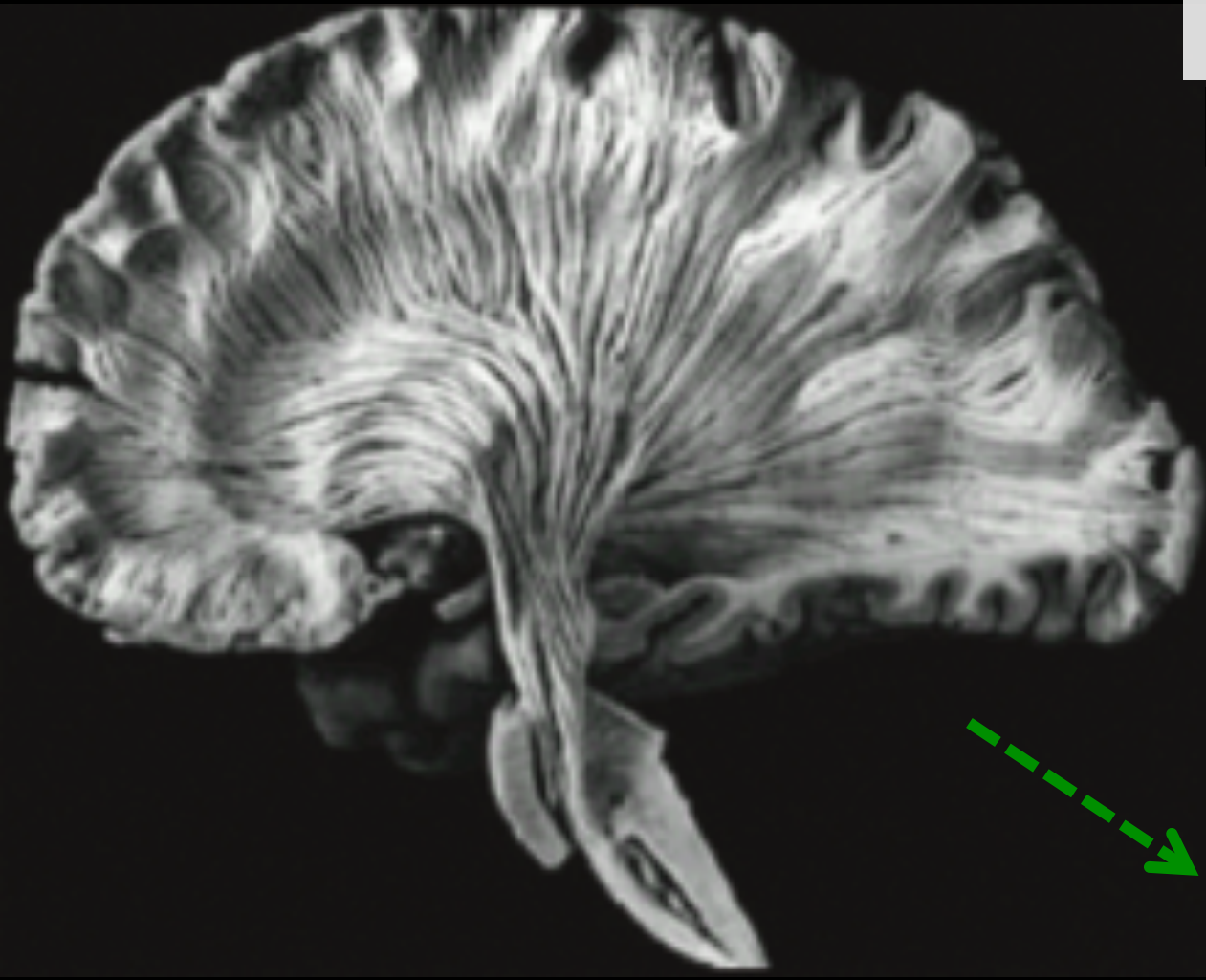
TENsor
Deflection
(TEND)
algorithm



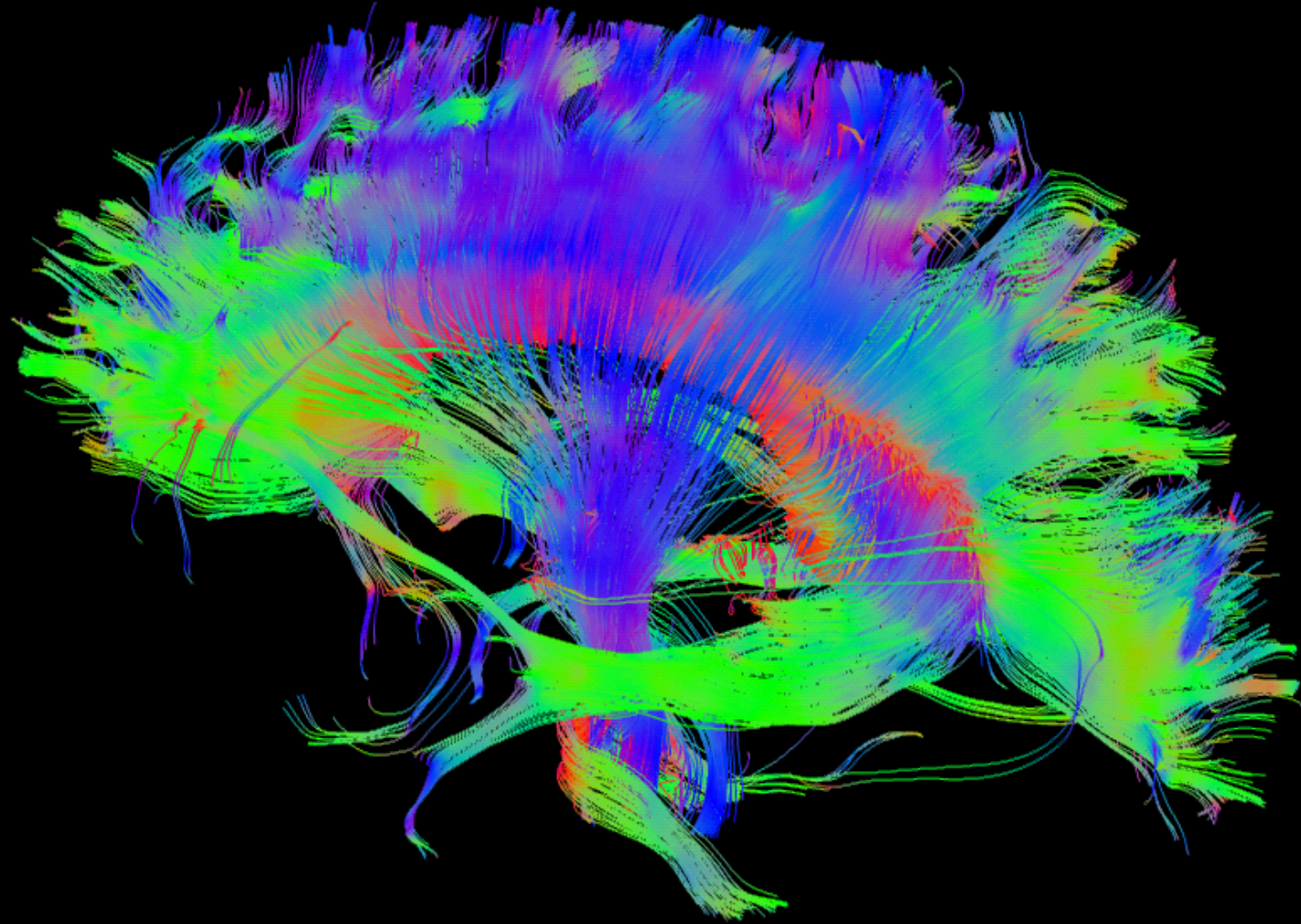
Second order Runge-
Kutta algorithm with
TEND

Lazar et al., HBM 2003

White Matter Fibers in Brain

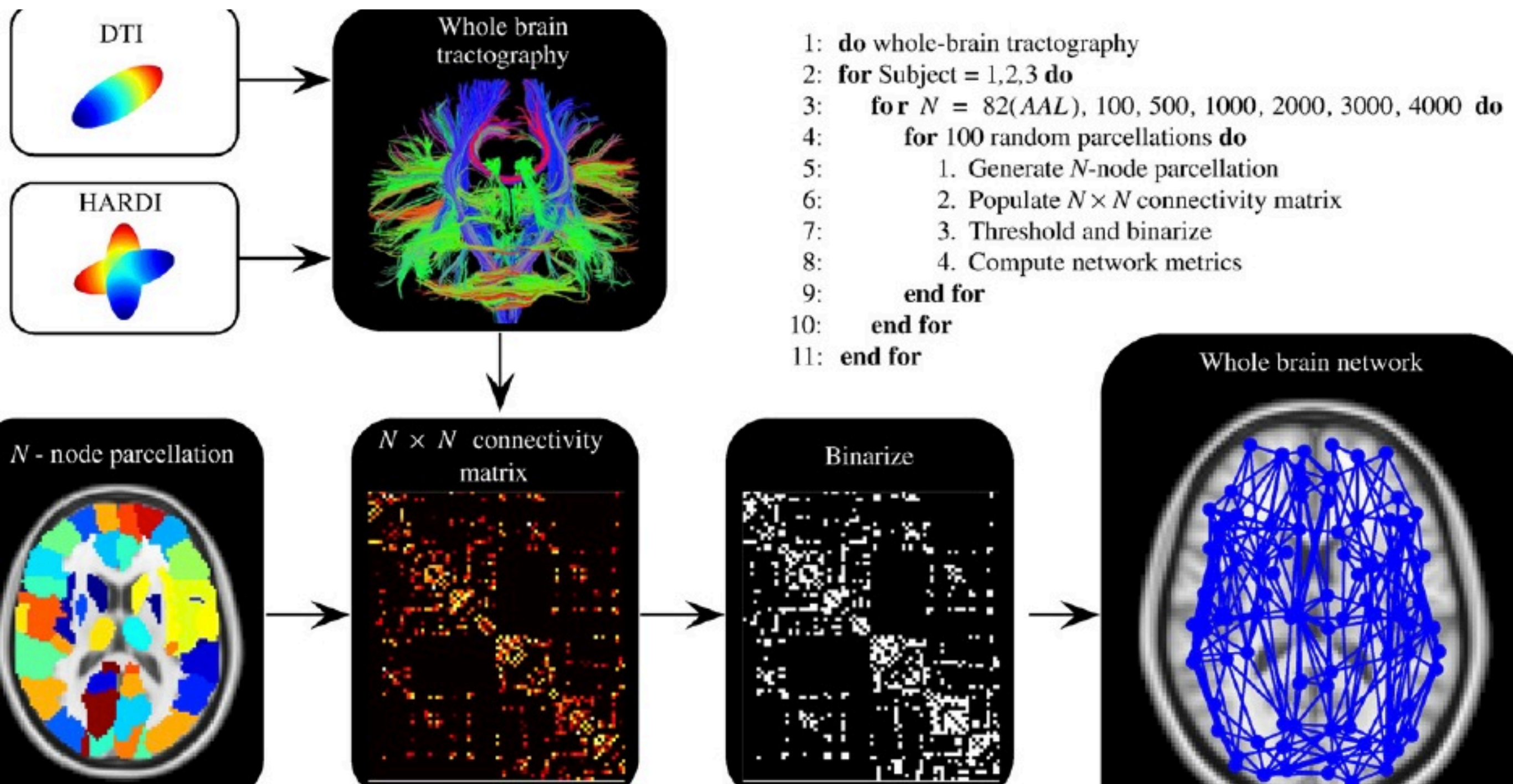


Postmortem

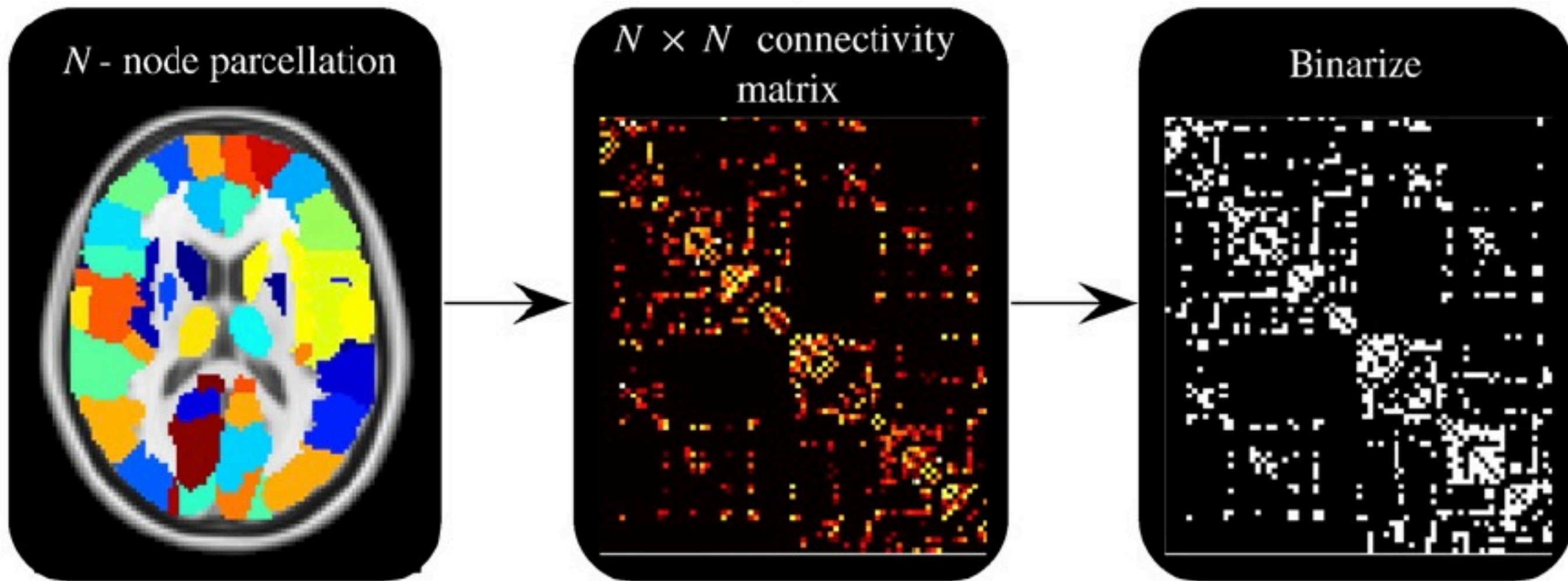


Half million tracts
600MB image per subject

Traditional brain network modeling flow



Two problems with the standard framework



Parcellation
70-100 regions

Arbitrary thresholding

Brain Network Modeling without parcellation and thresholding

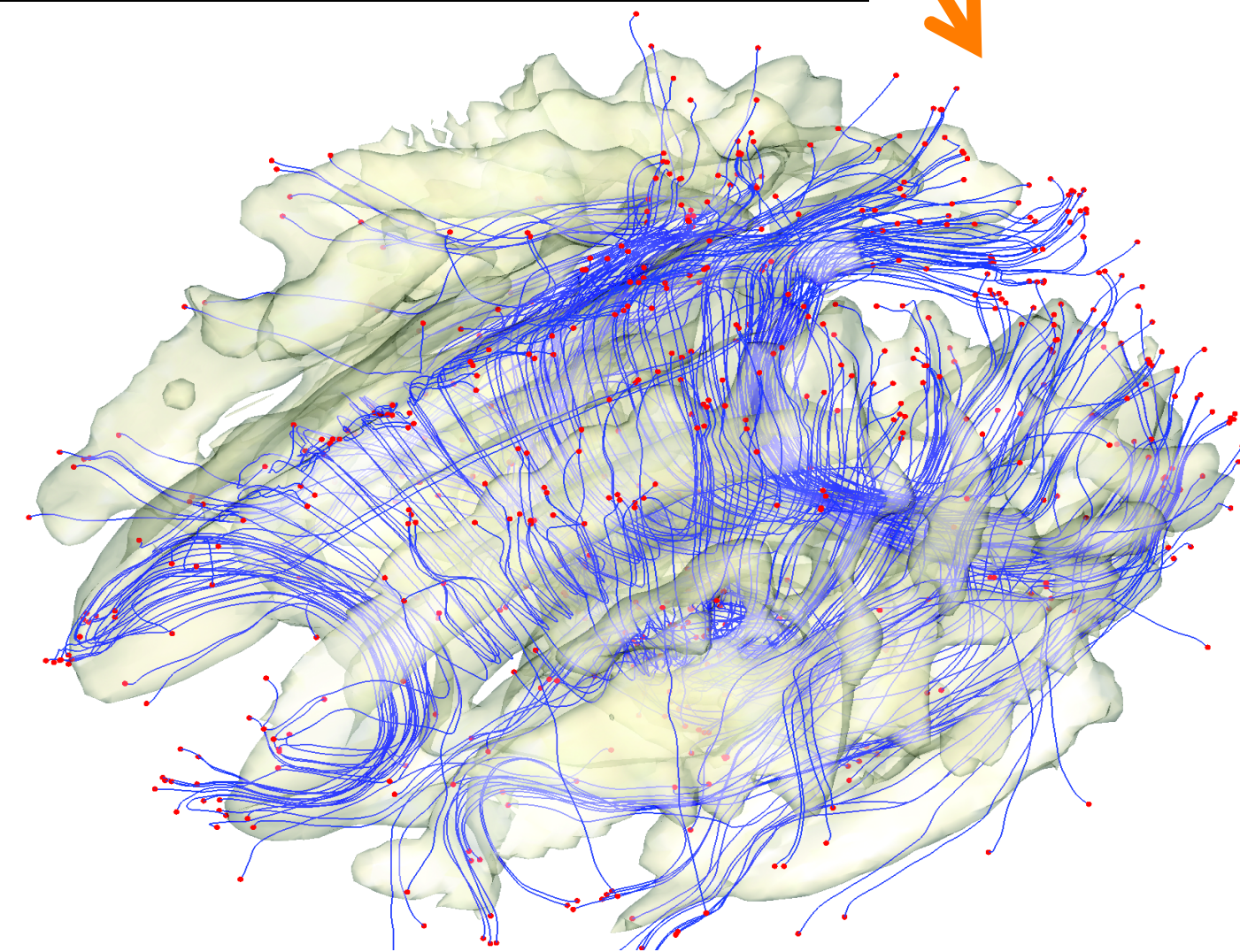
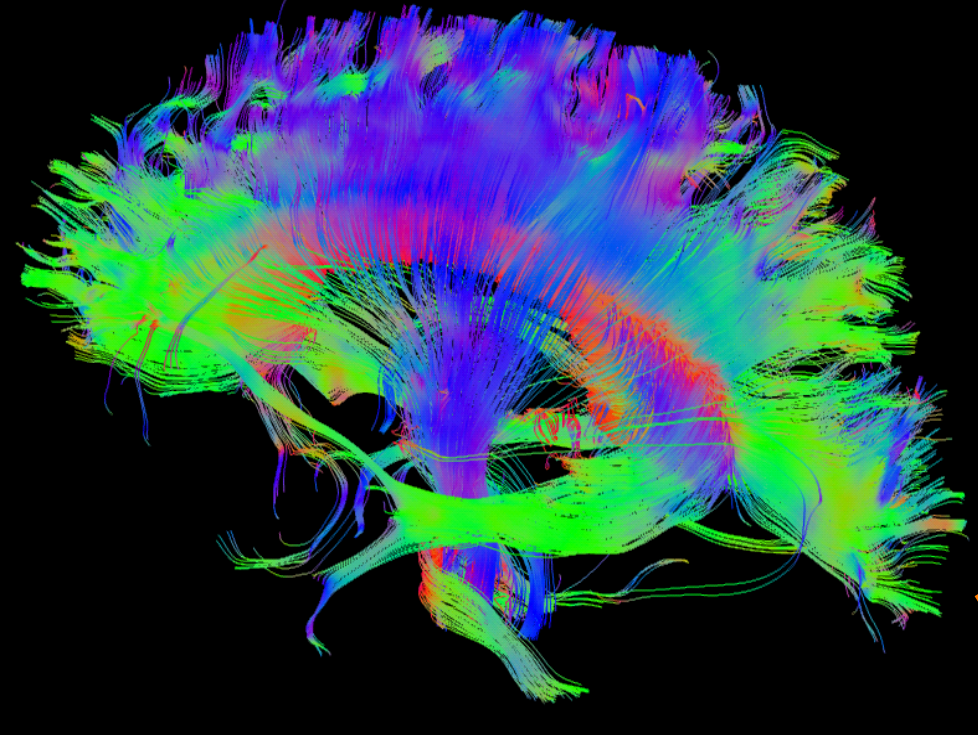
Epsilon-neighbor method

A different simplex construction technique

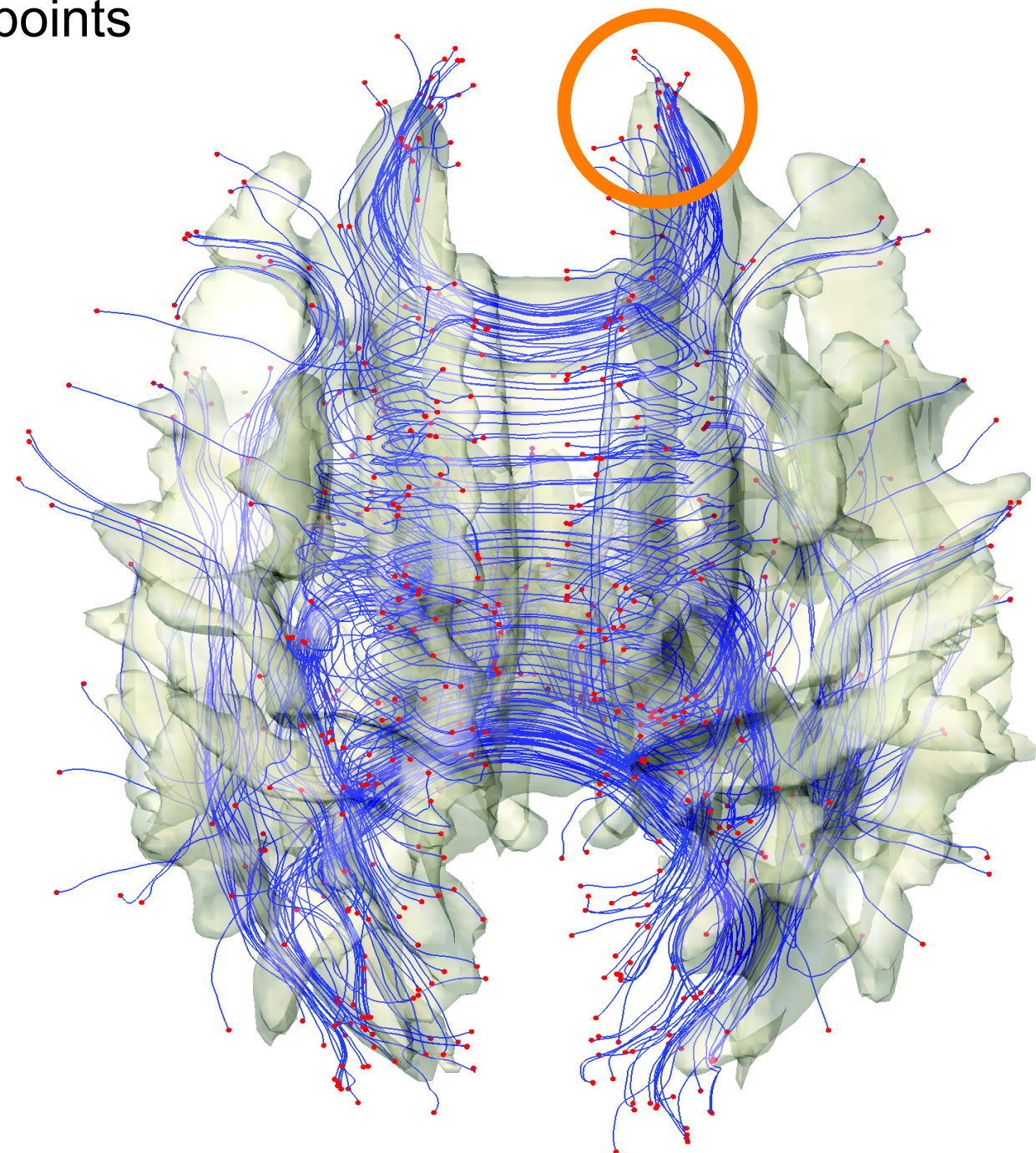
ϵ -neighbor graph simplification

All points in the ϵ -neighbor are identified as a single node in a graph

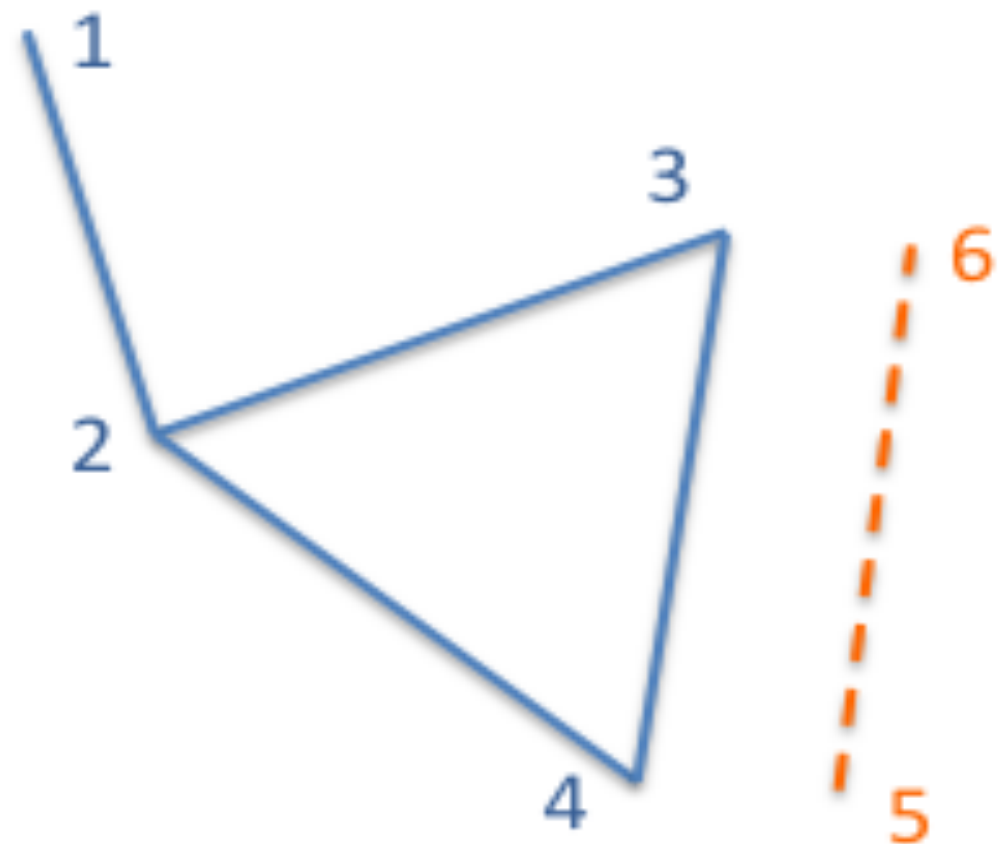
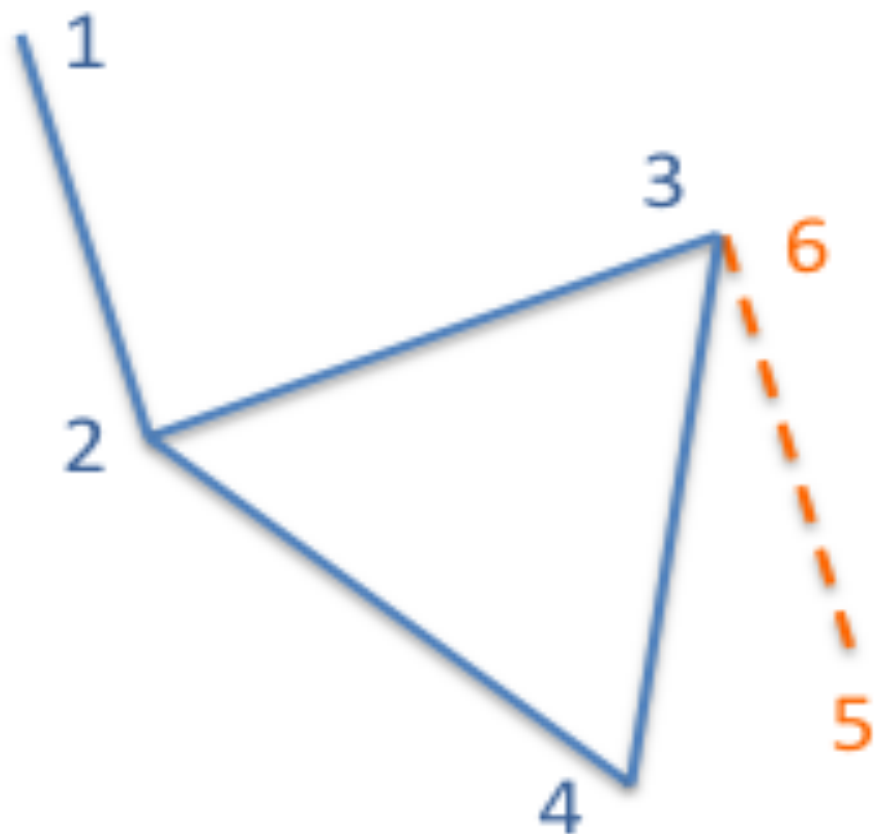
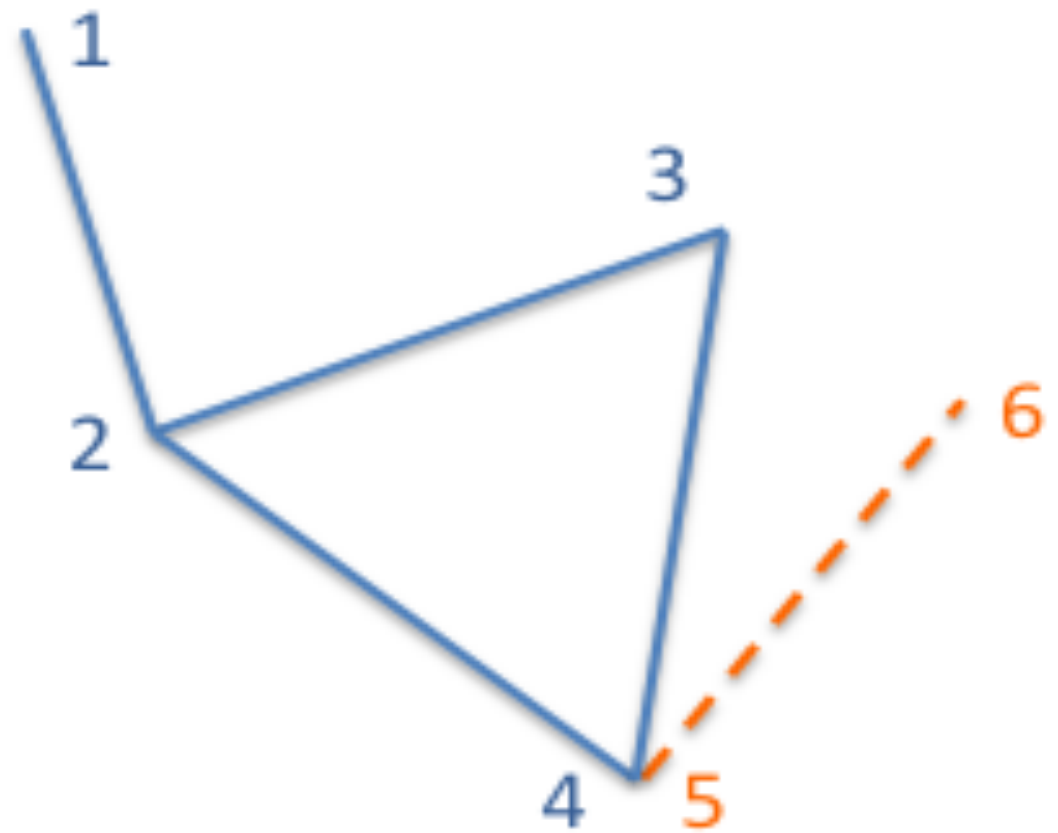
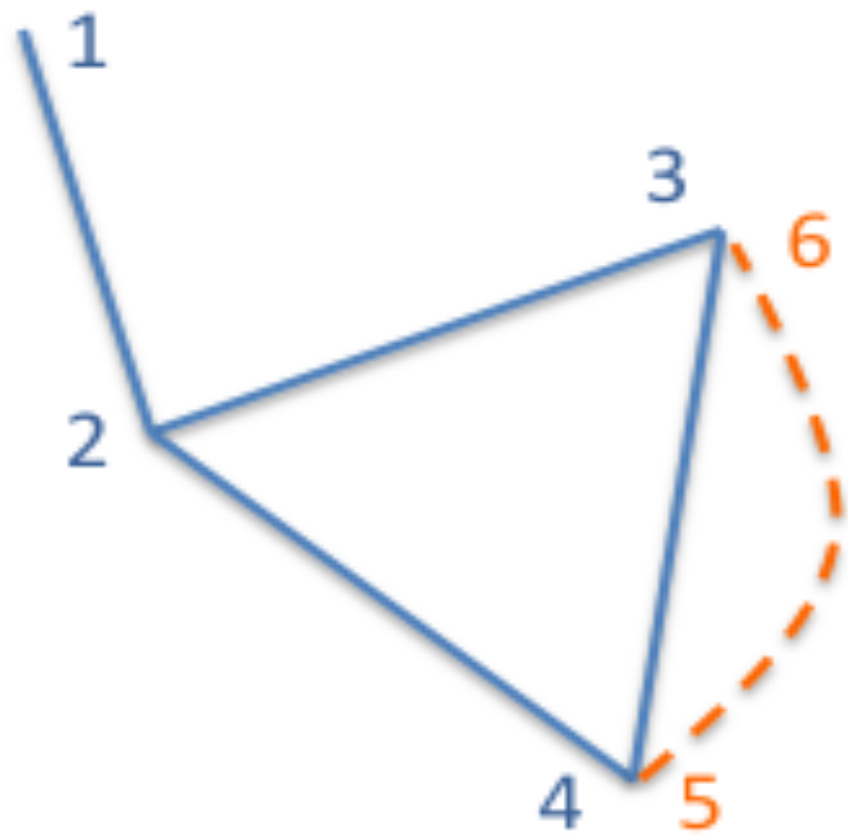
Identify end points



The first data-driven DTI structural network construction framework without any parcellation.

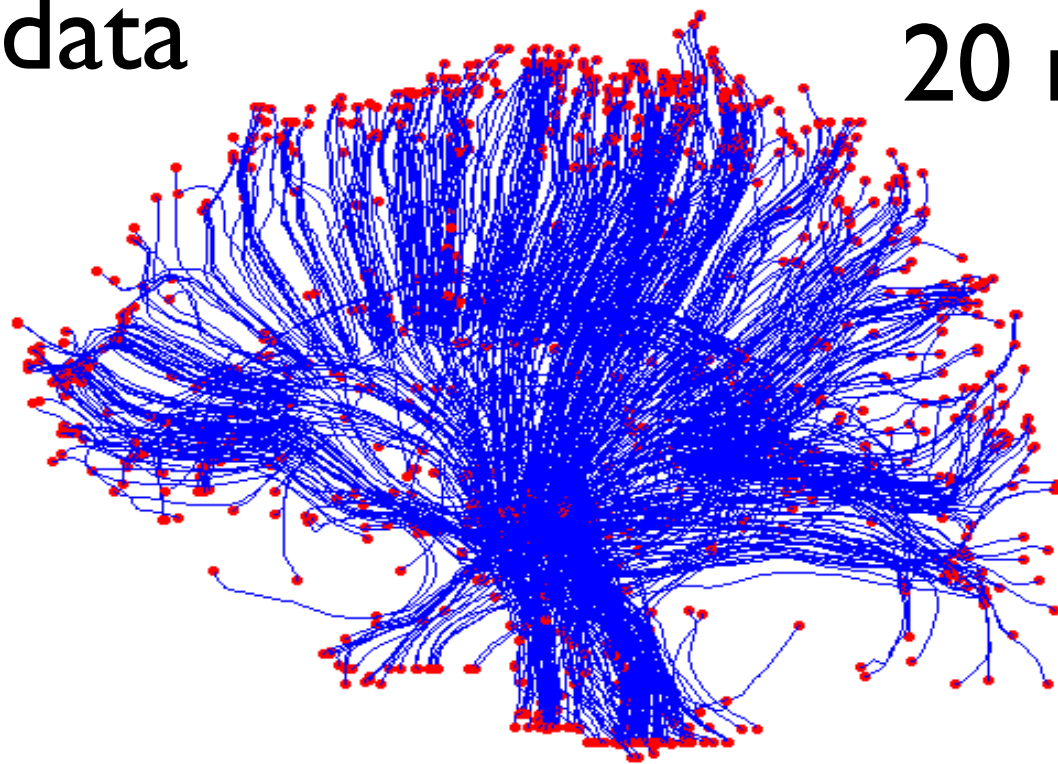


Iterative graph construction

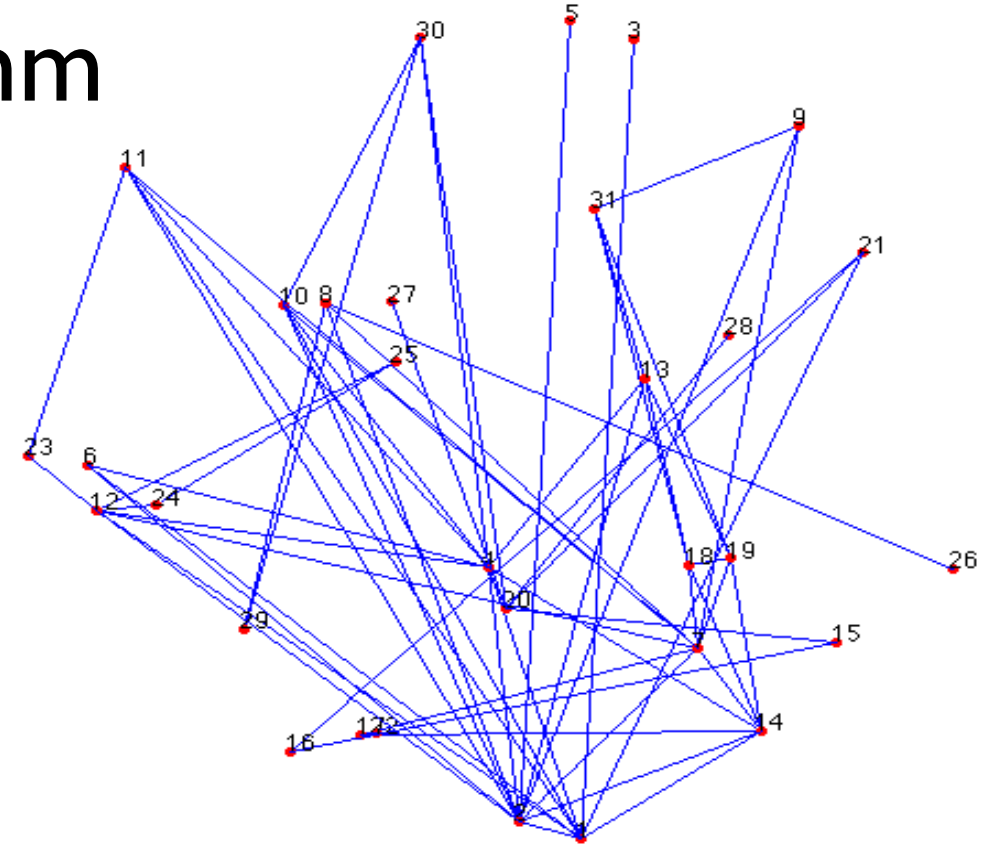


ϵ -neighbor graphs with different ϵ

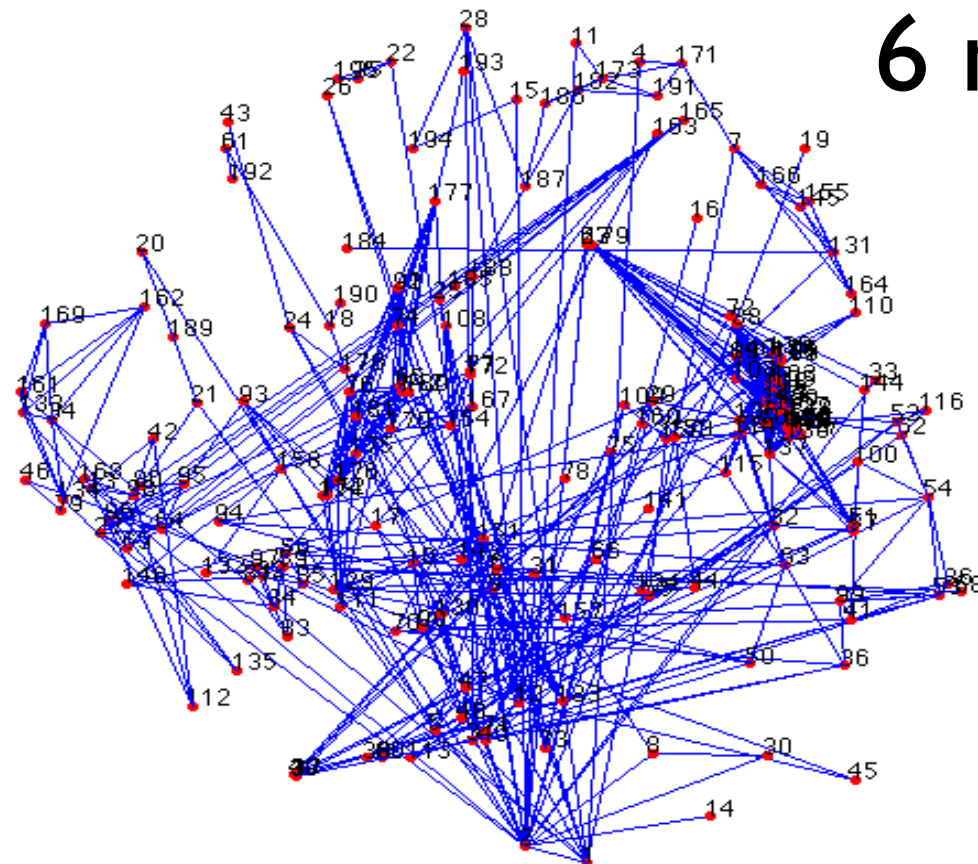
original data



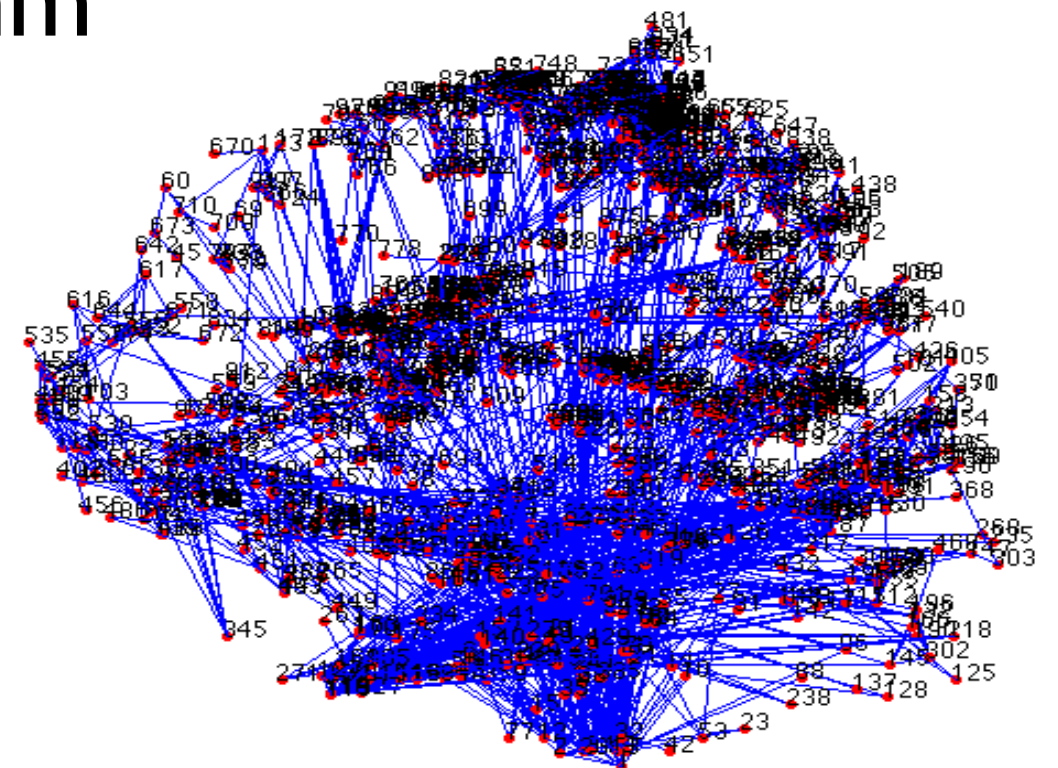
20 mm



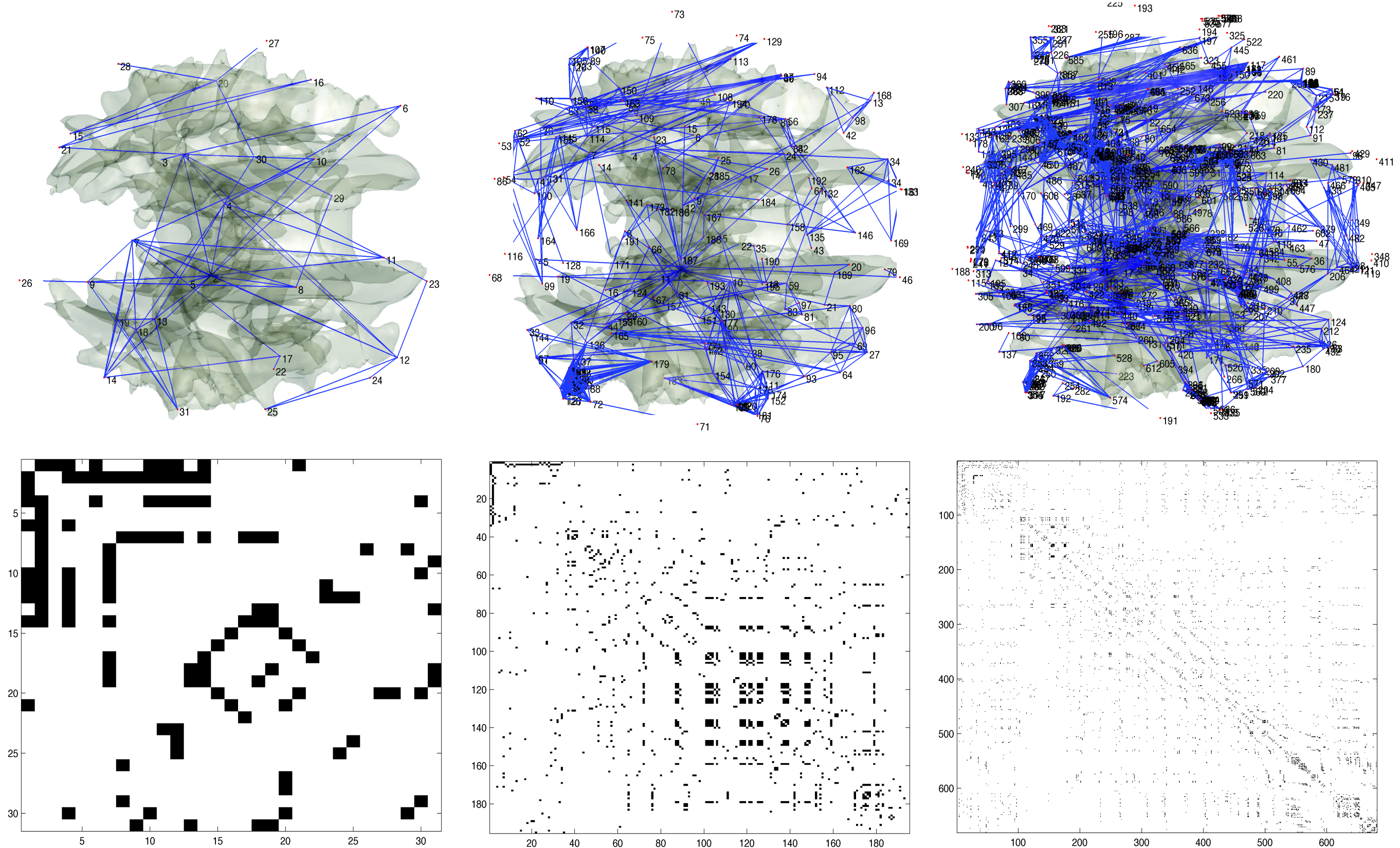
10 mm



6 mm



Adjacency matrix



MATLAB DEMO

Epsilon Neighbor method

Application to autism

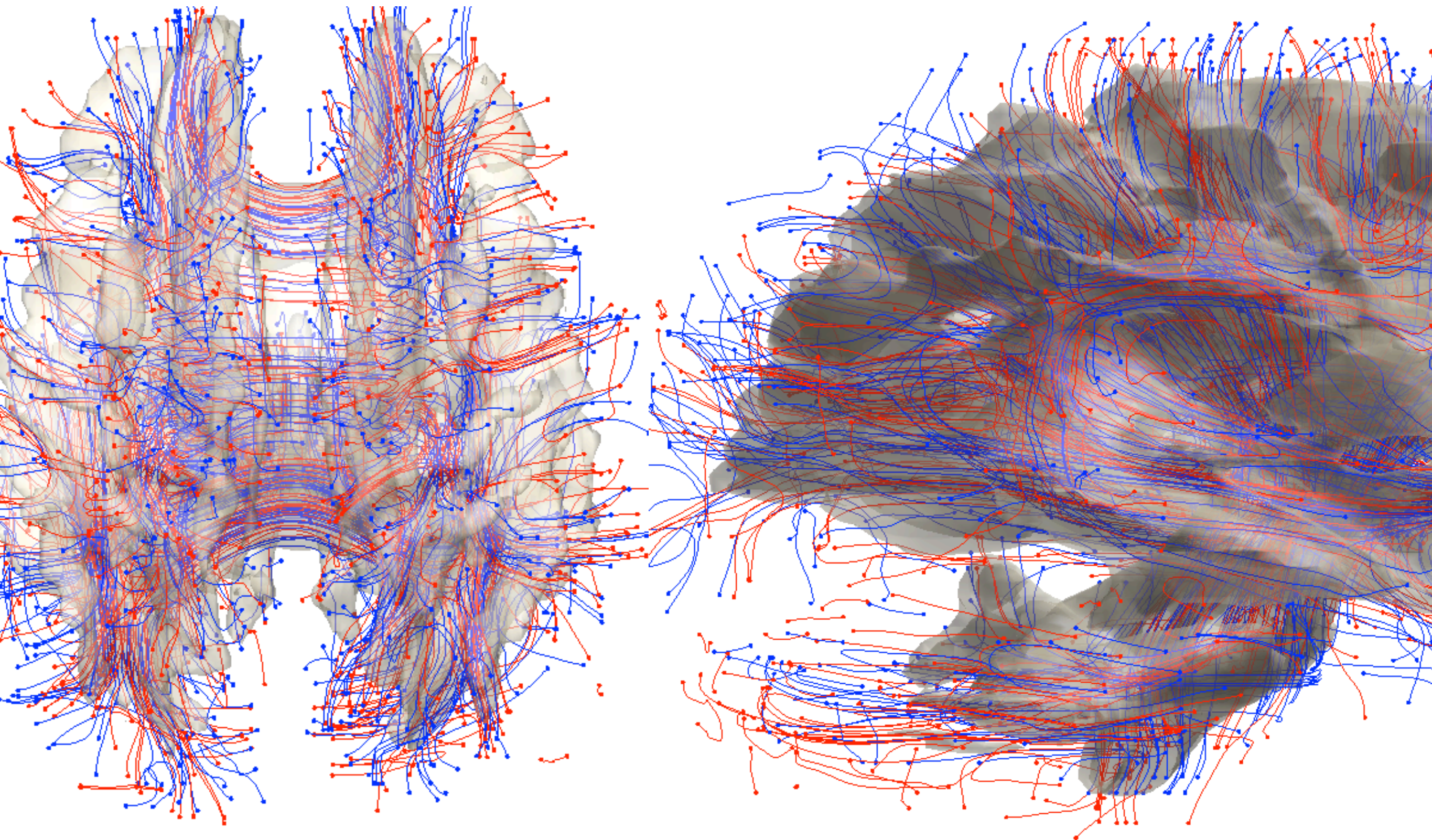
Autistic children (n=17)

Control subjects (n=14)

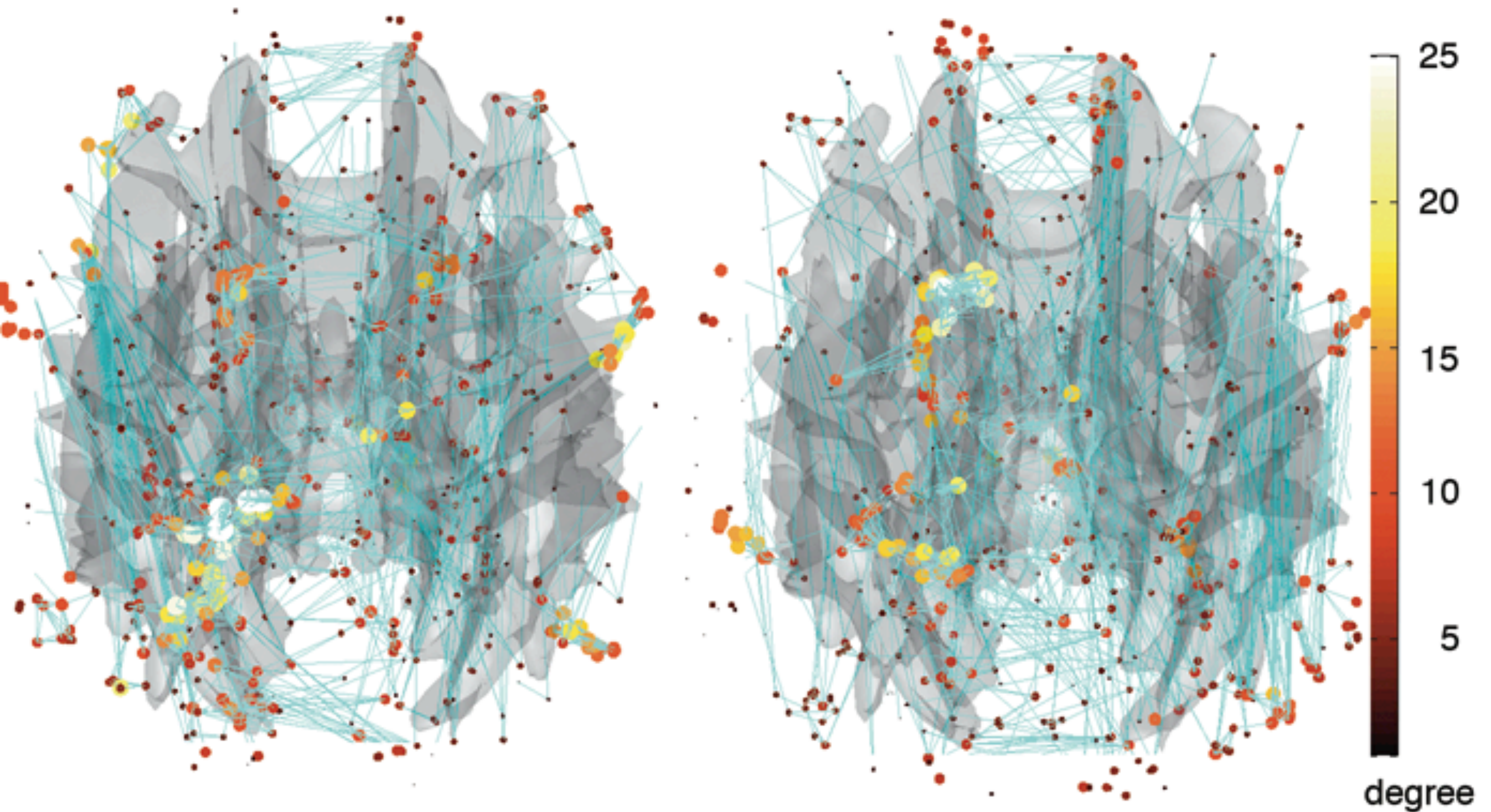
Matched for age, handedness, IQ and head size

Abnormal connectivity in autism ?

DTI registration



Degree of nodes for a single subject

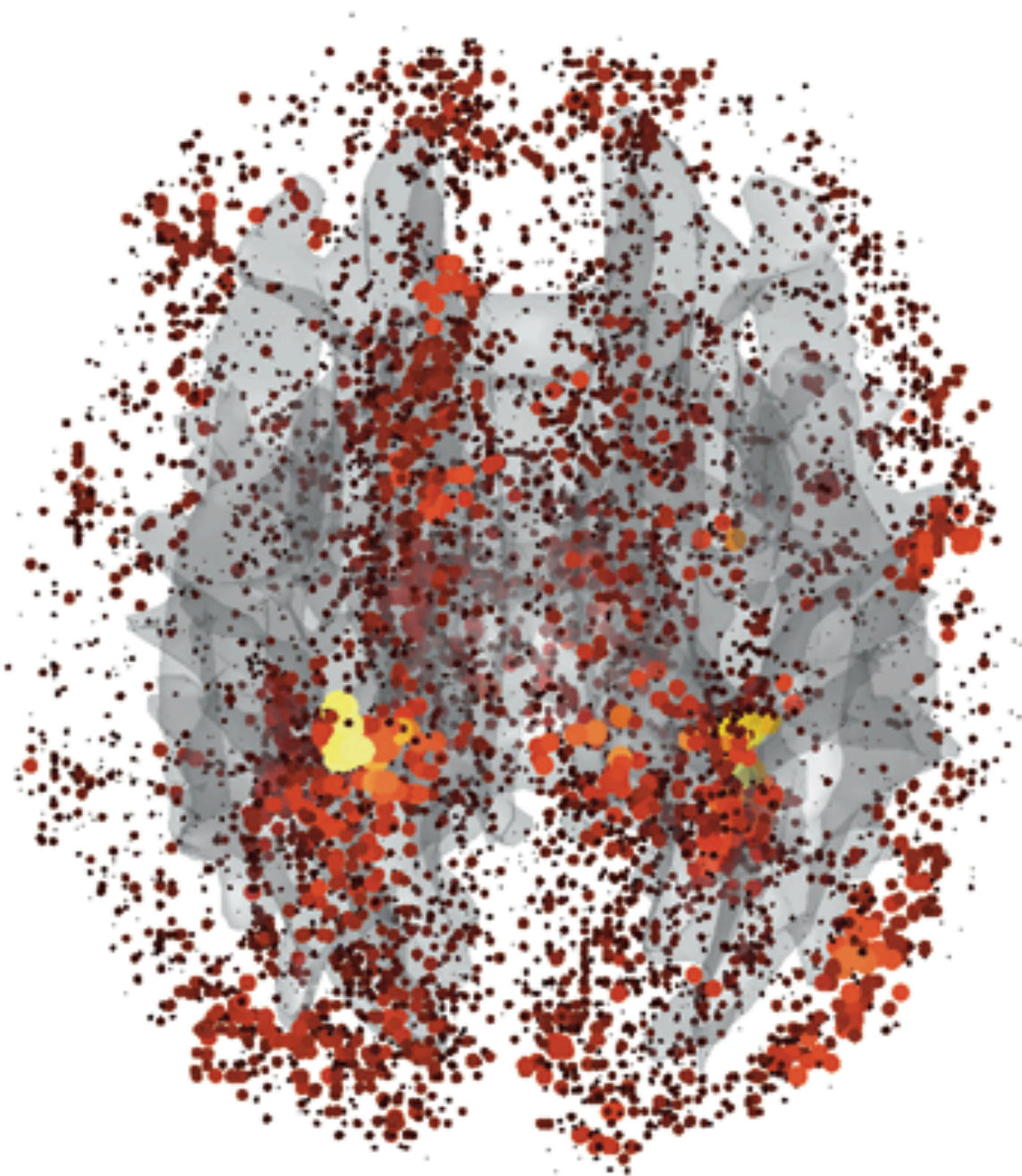


control #001

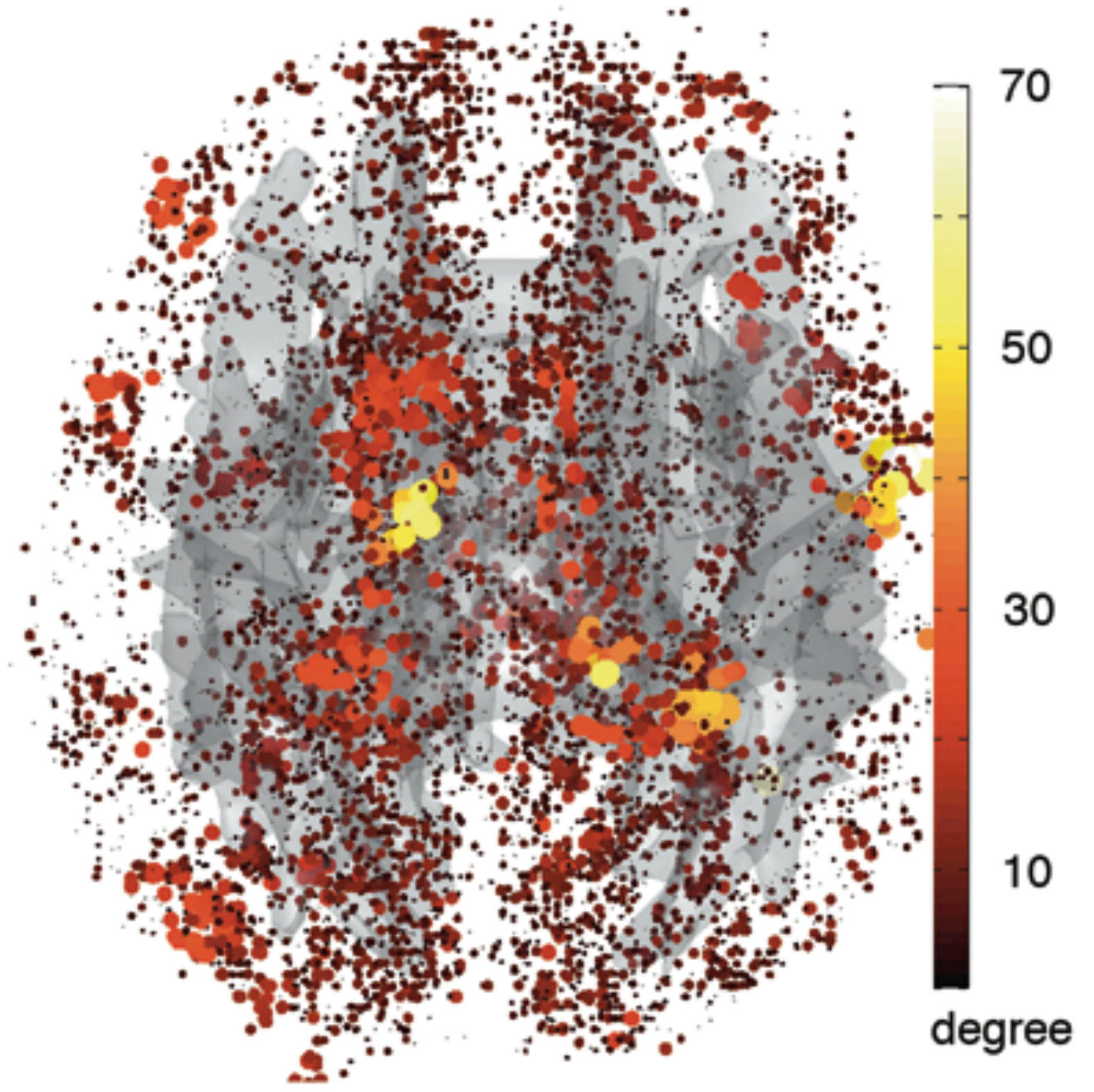
autism #120

Local inference on degree

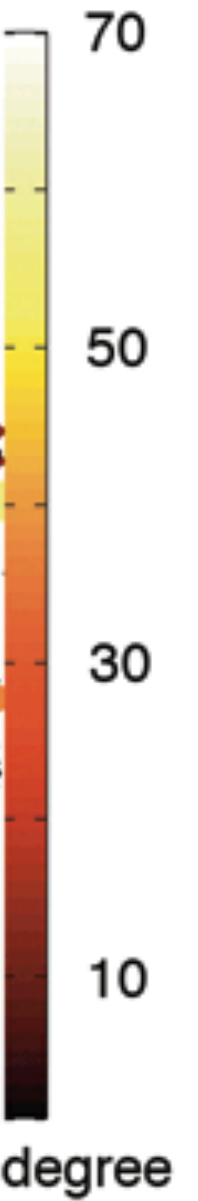
Superimposition of every subjects



Control

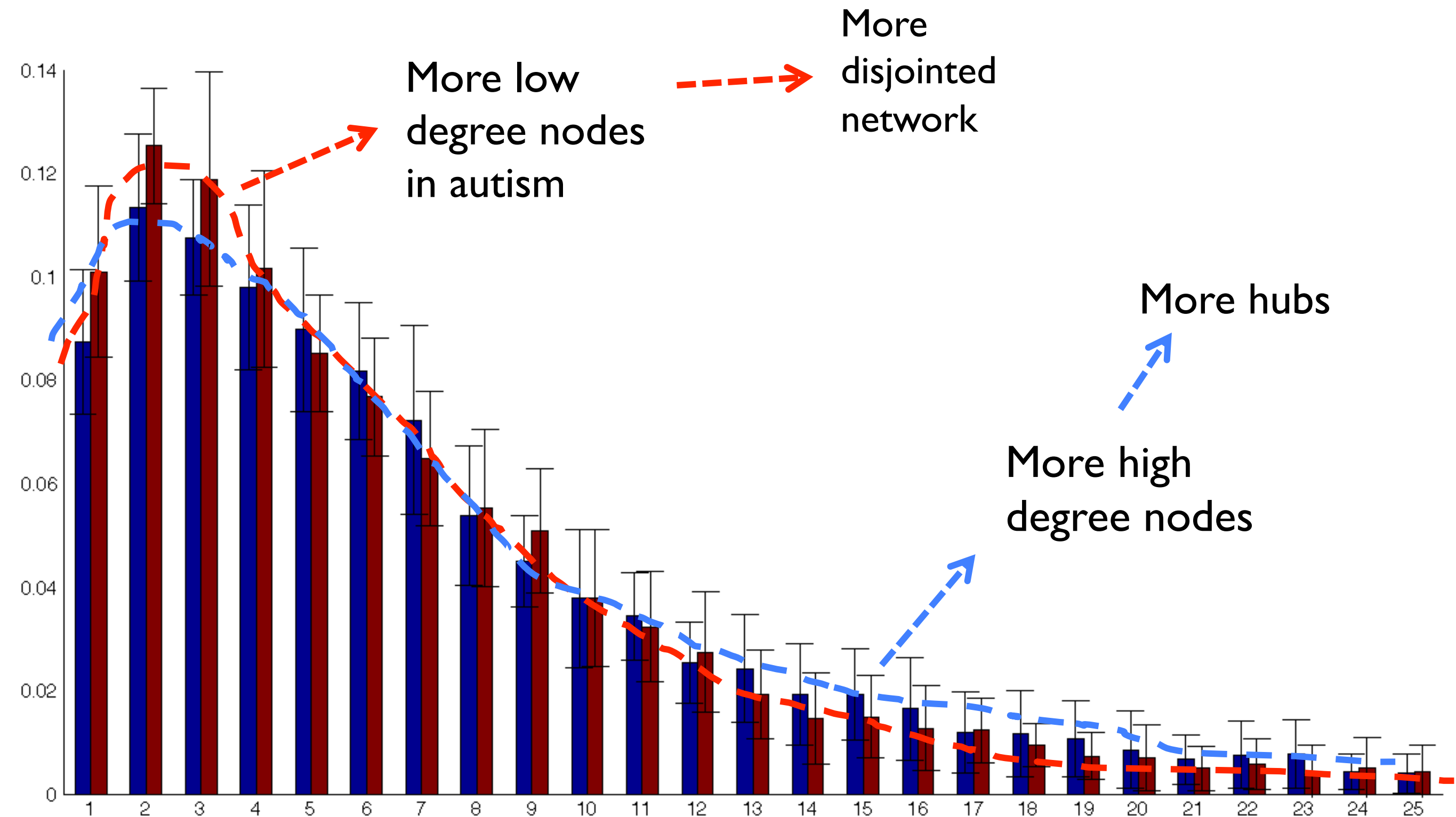


Autism



Degree distribution

red: autism
blue: control

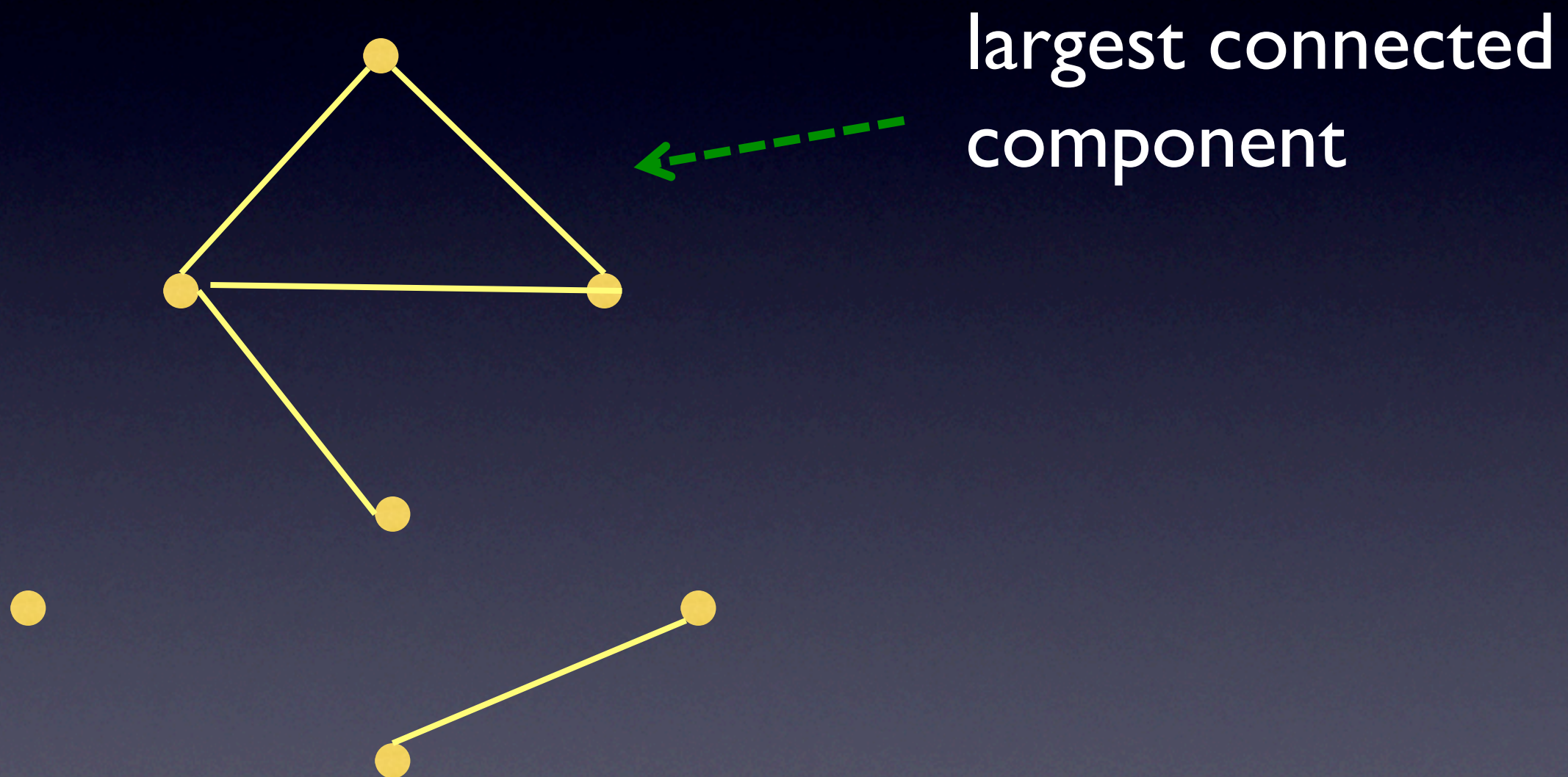


pvalues = 0.024, 0.015 and 0.080 for degrees 1, 2 and 3.

Persistent homological approach

Graph Filtration

Connected component



Filtration on ε -neighbor graphs

ε -neighbor graph at the i -th iteration $\mathcal{G}_i$

$$\mathcal{G}_1 \subset \mathcal{G}_2 \subset \mathcal{G}_3 \subset \cdots$$

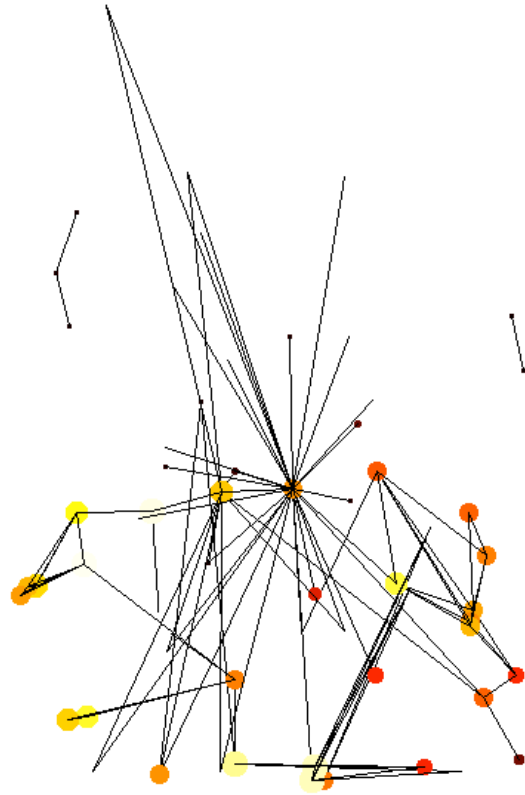
The size of the i -th graph is an increasing function:

$$\#\mathcal{G}_1 < \#\mathcal{G}_2 < \#\mathcal{G}_3 < \cdots$$

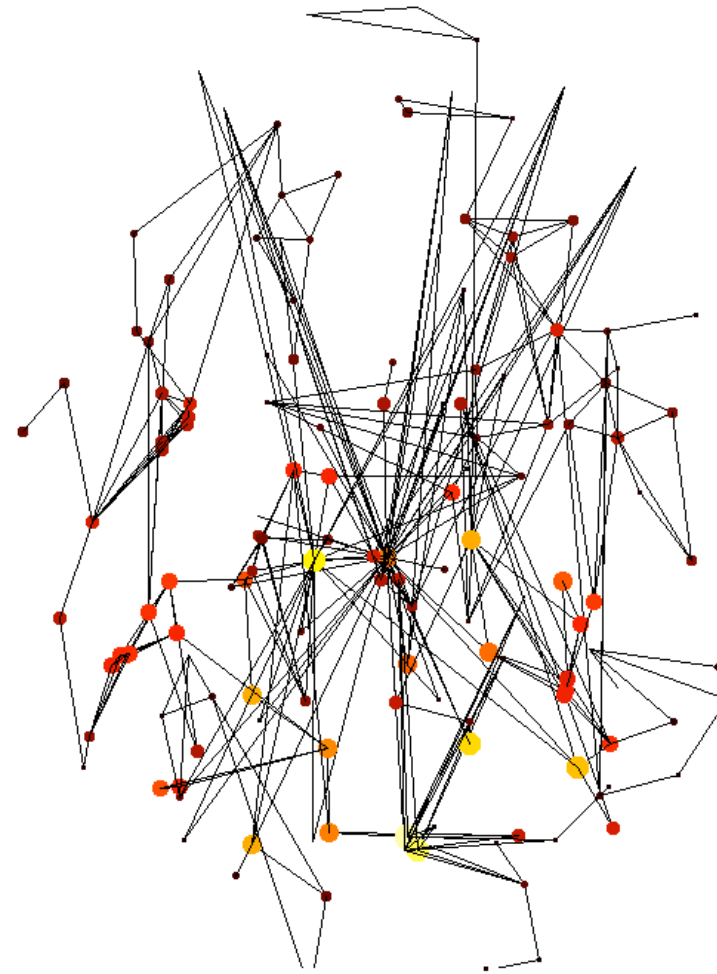
Filtration on ε -neighbor graphs



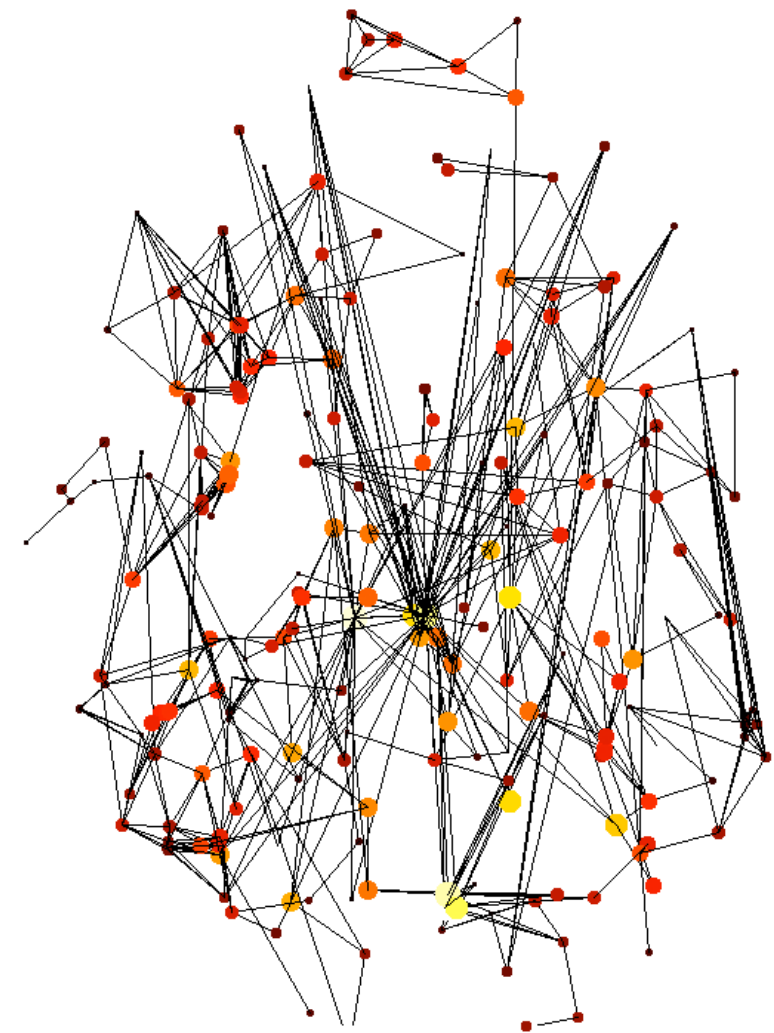
10



4000

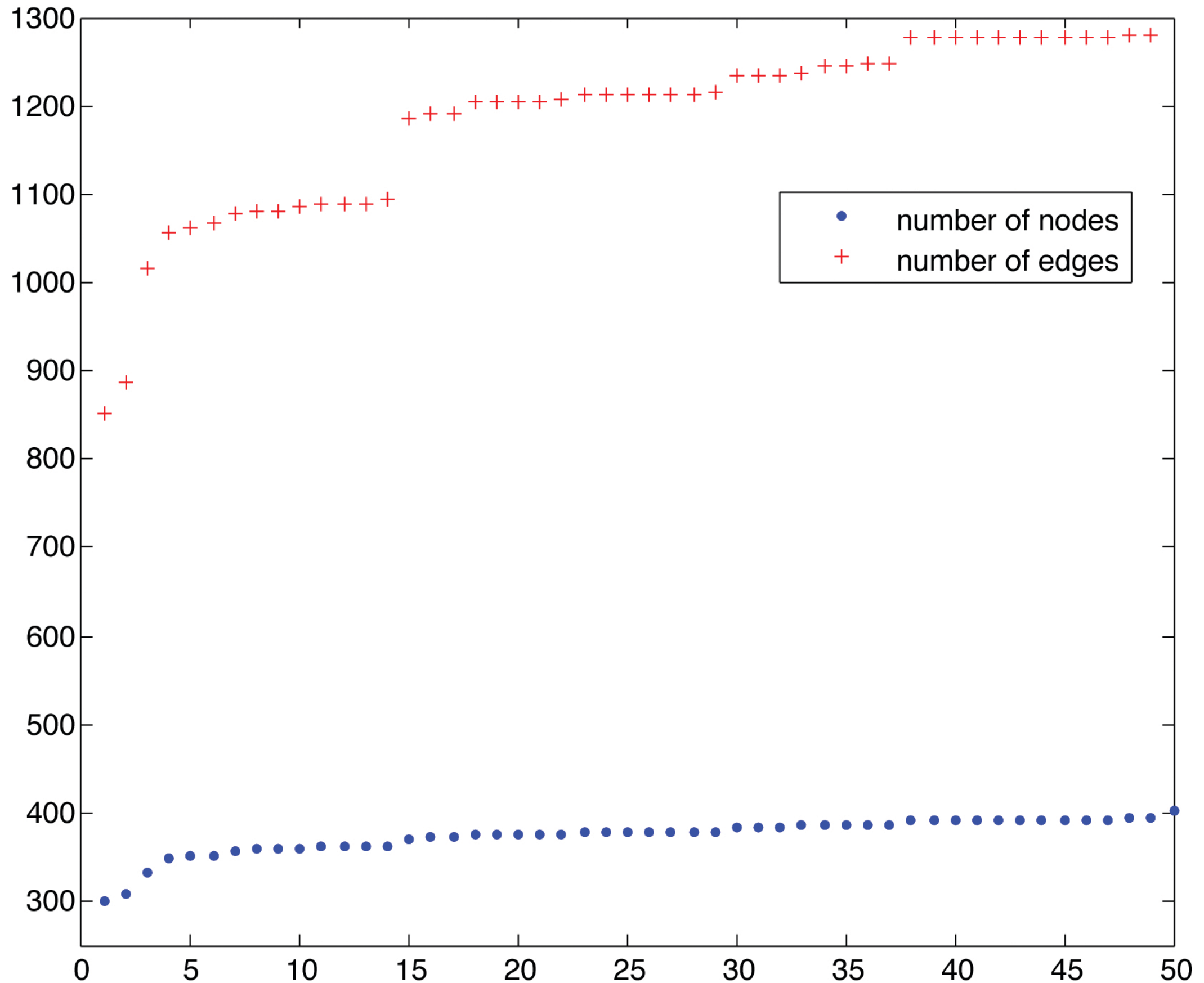


20000



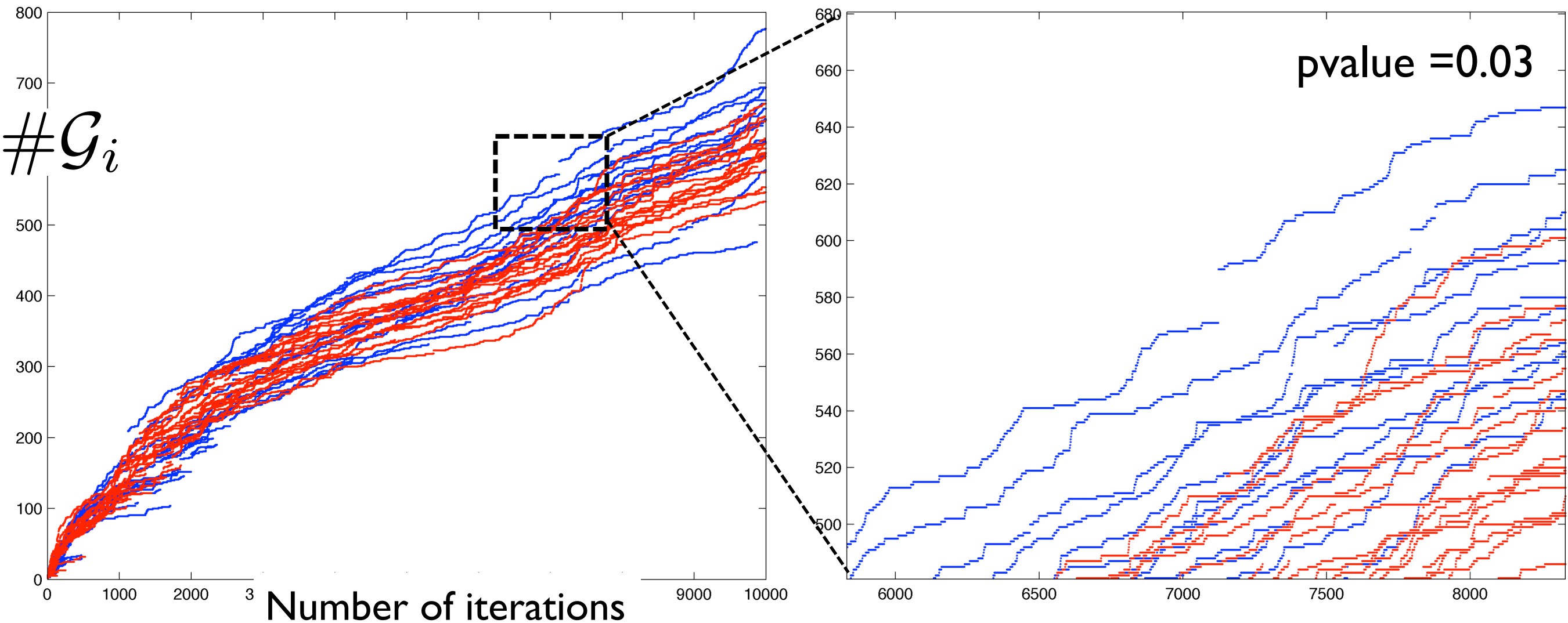
40000

Number of edges and nodes in filtration



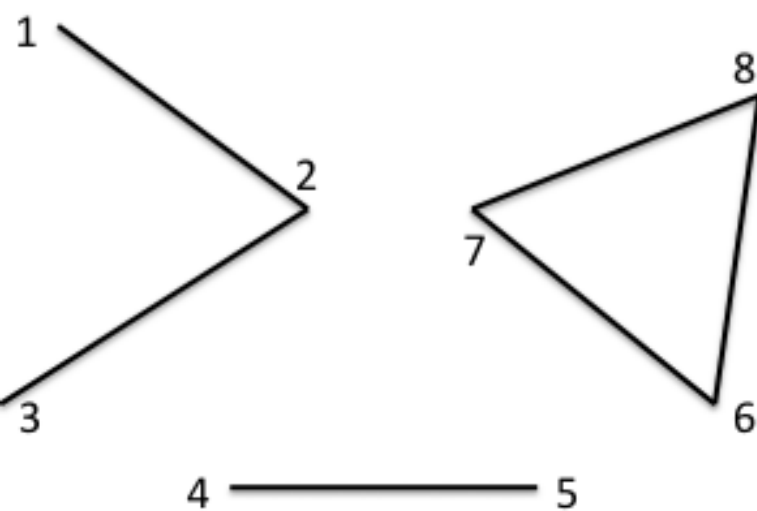
Network integration difference

Control=blue
Autism=red

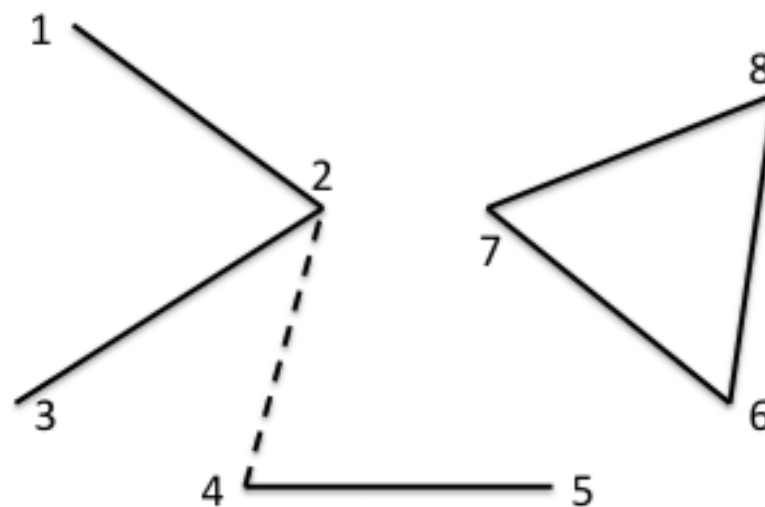


The brain network in control subjects merges to a single component faster than other populations.

The size of the largest connected component

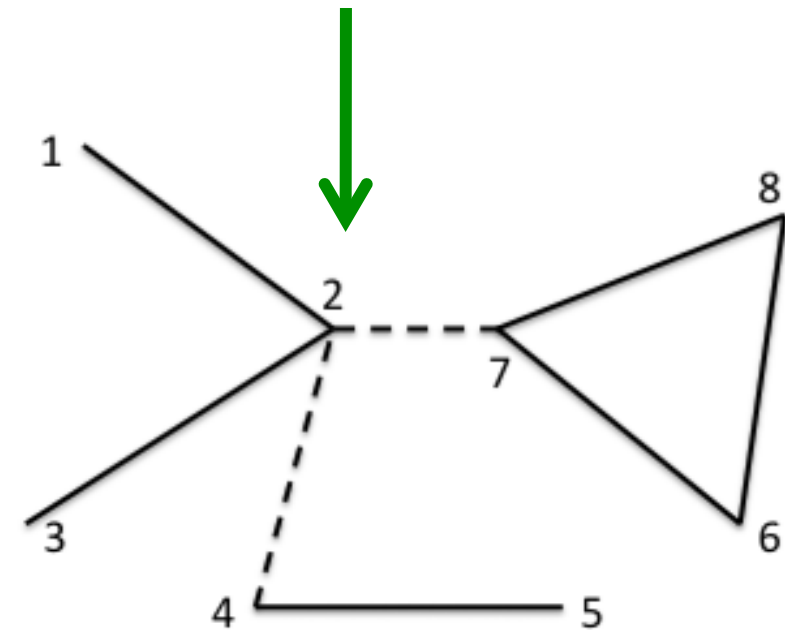


Size: 3



5

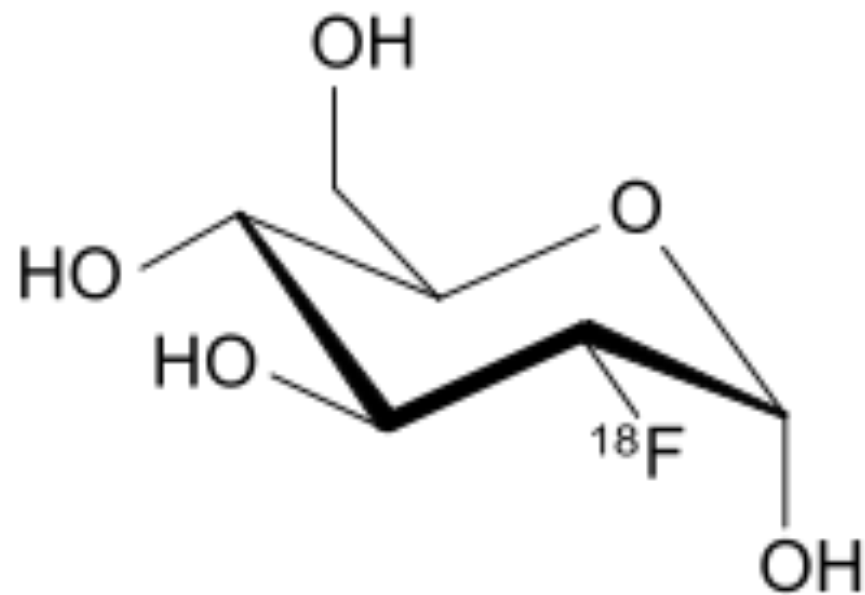
emergence of a linking node



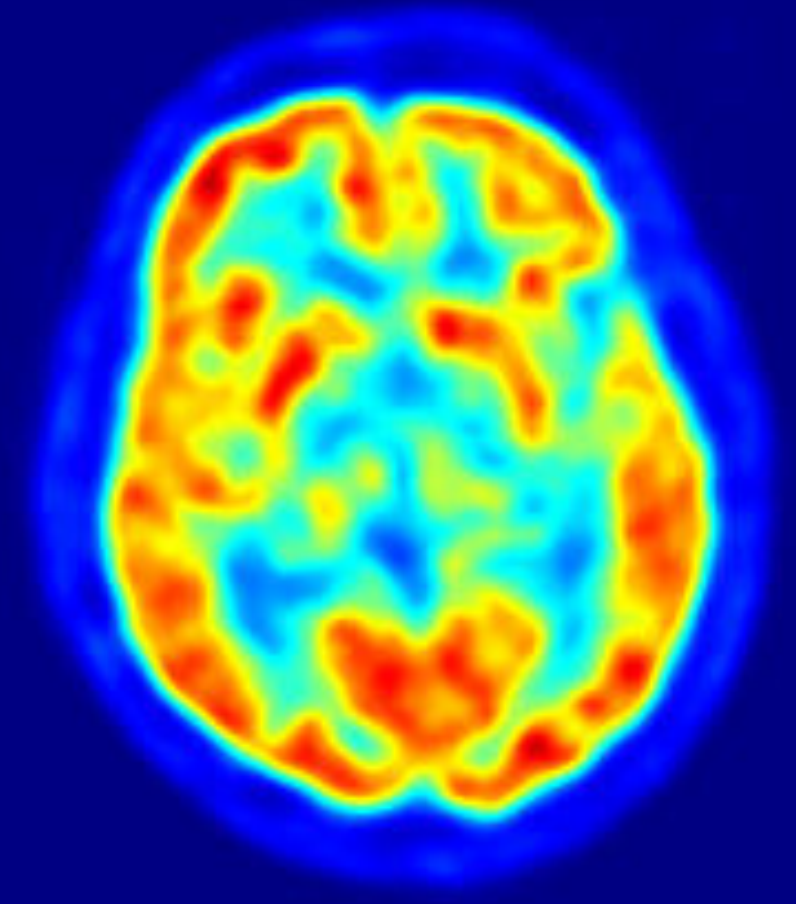
8

FDG-PET imaging

The PET scanner detects pairs of gamma rays emitted from a positron-emitting radioactive tracer.

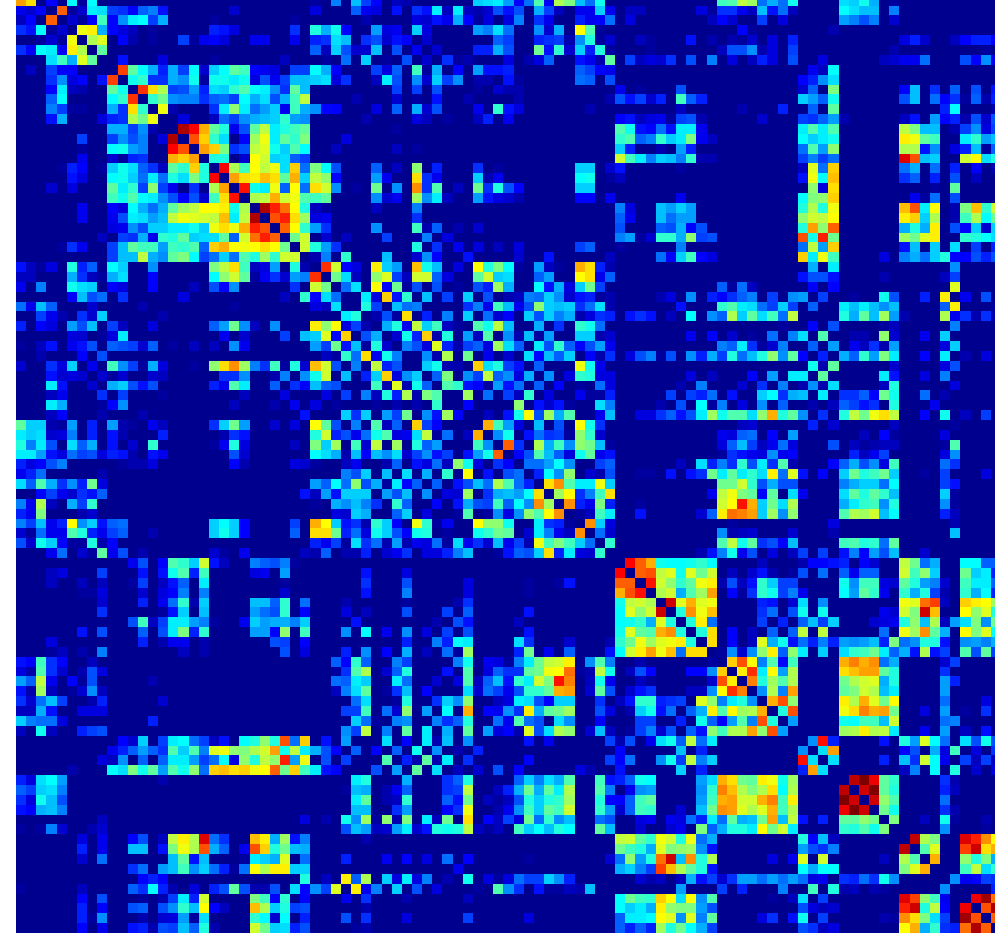
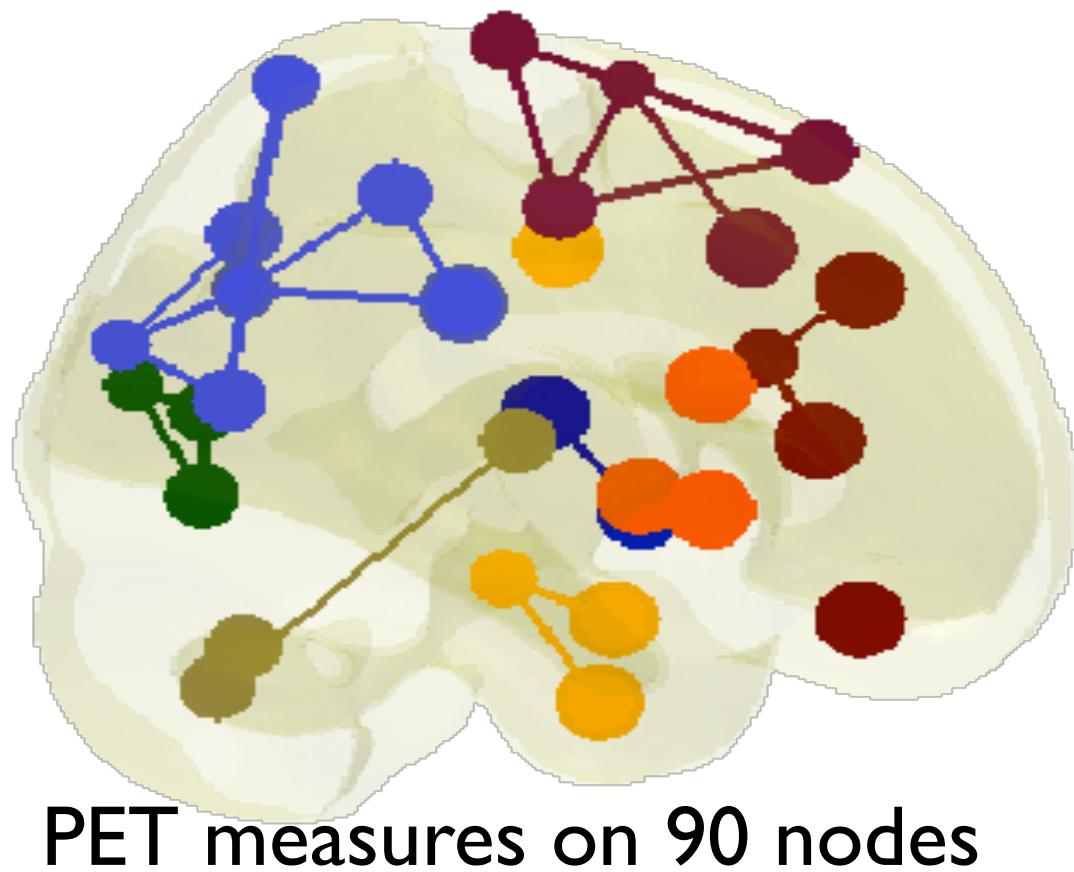


^{18}F -FDG is the most widely used tracer used for measuring tissue metabolic activity, in terms of regional glucose uptake in the brain.

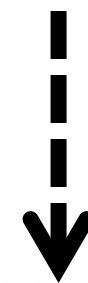


Pet metabolic connectivity

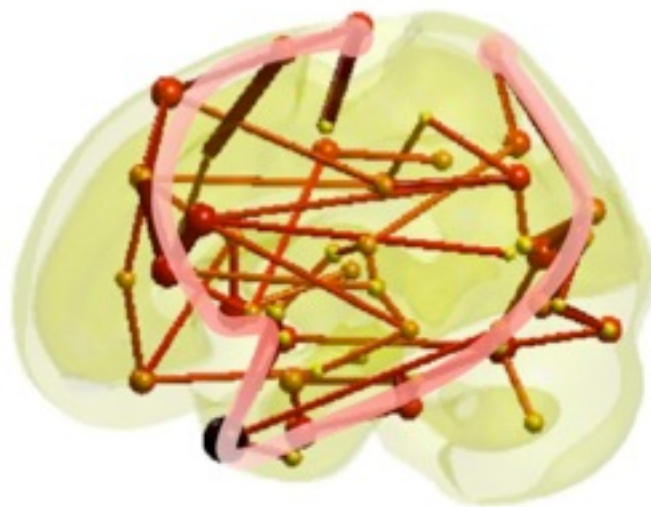
Lee et al., 2011 MICCAI



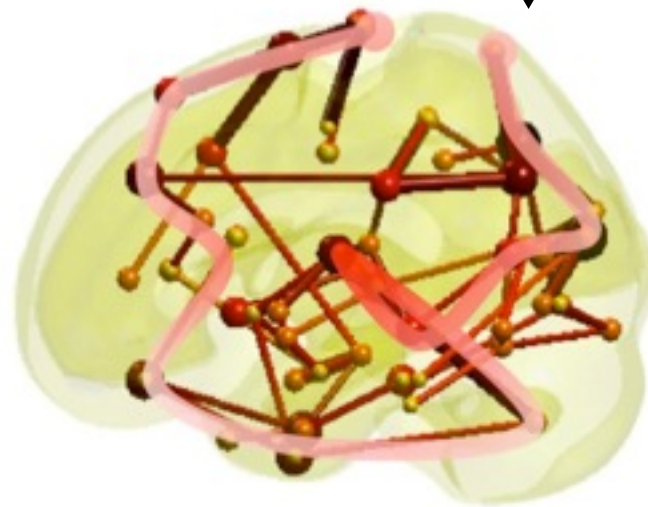
90 x 90 correlation map



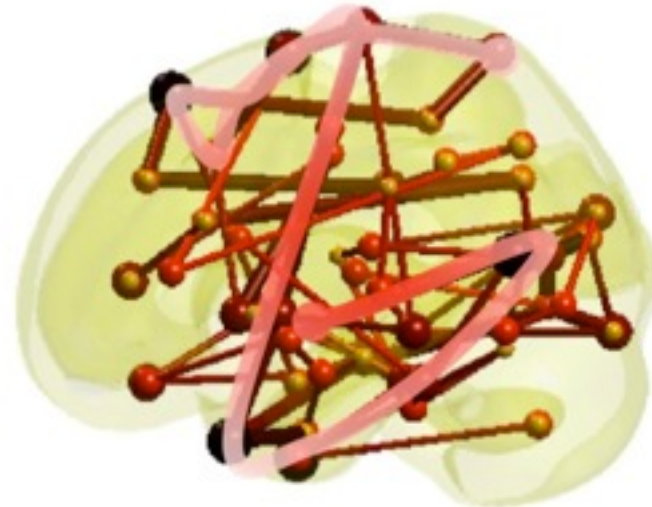
Graph filtration



Attention deficit



Autism



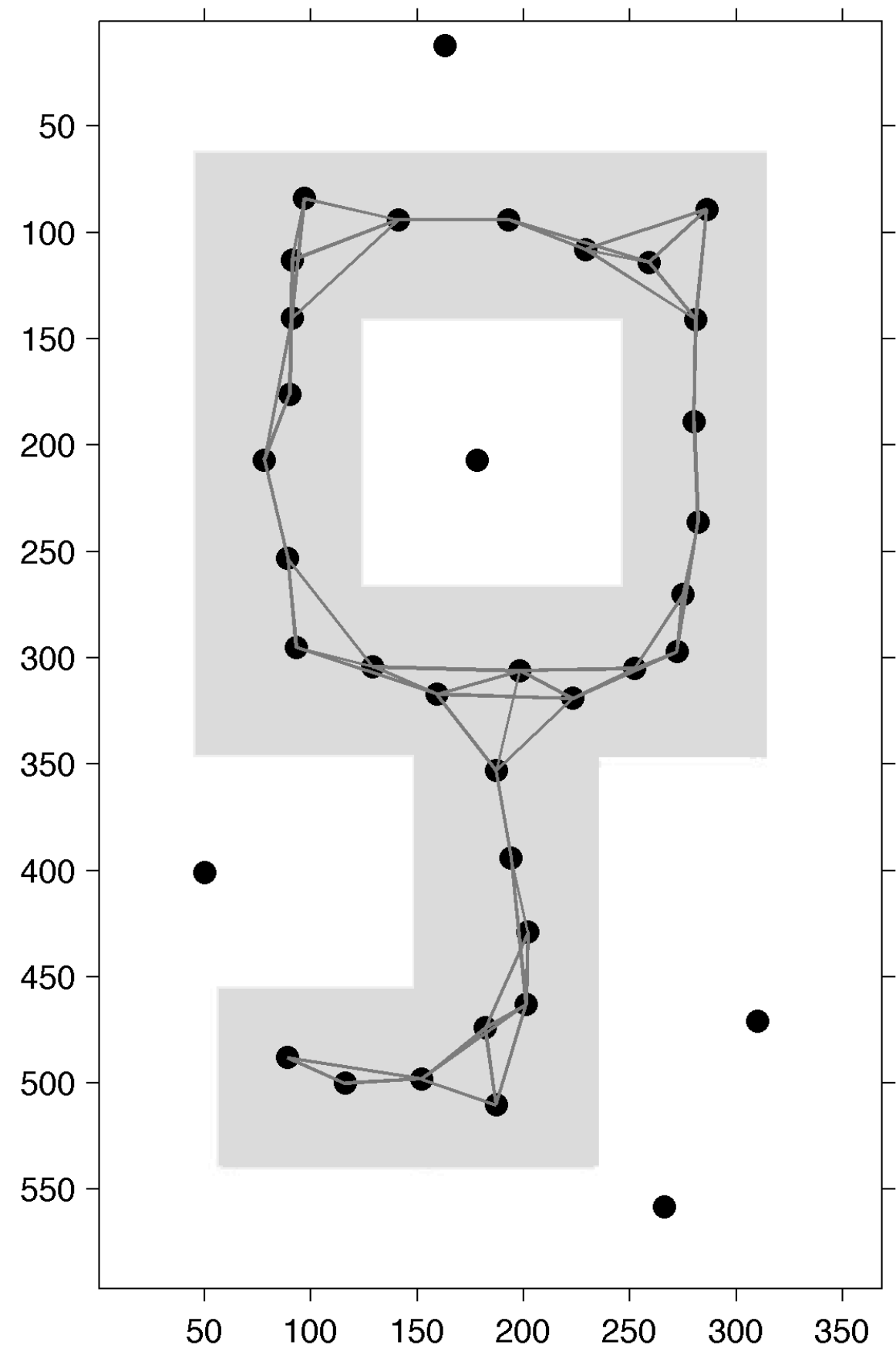
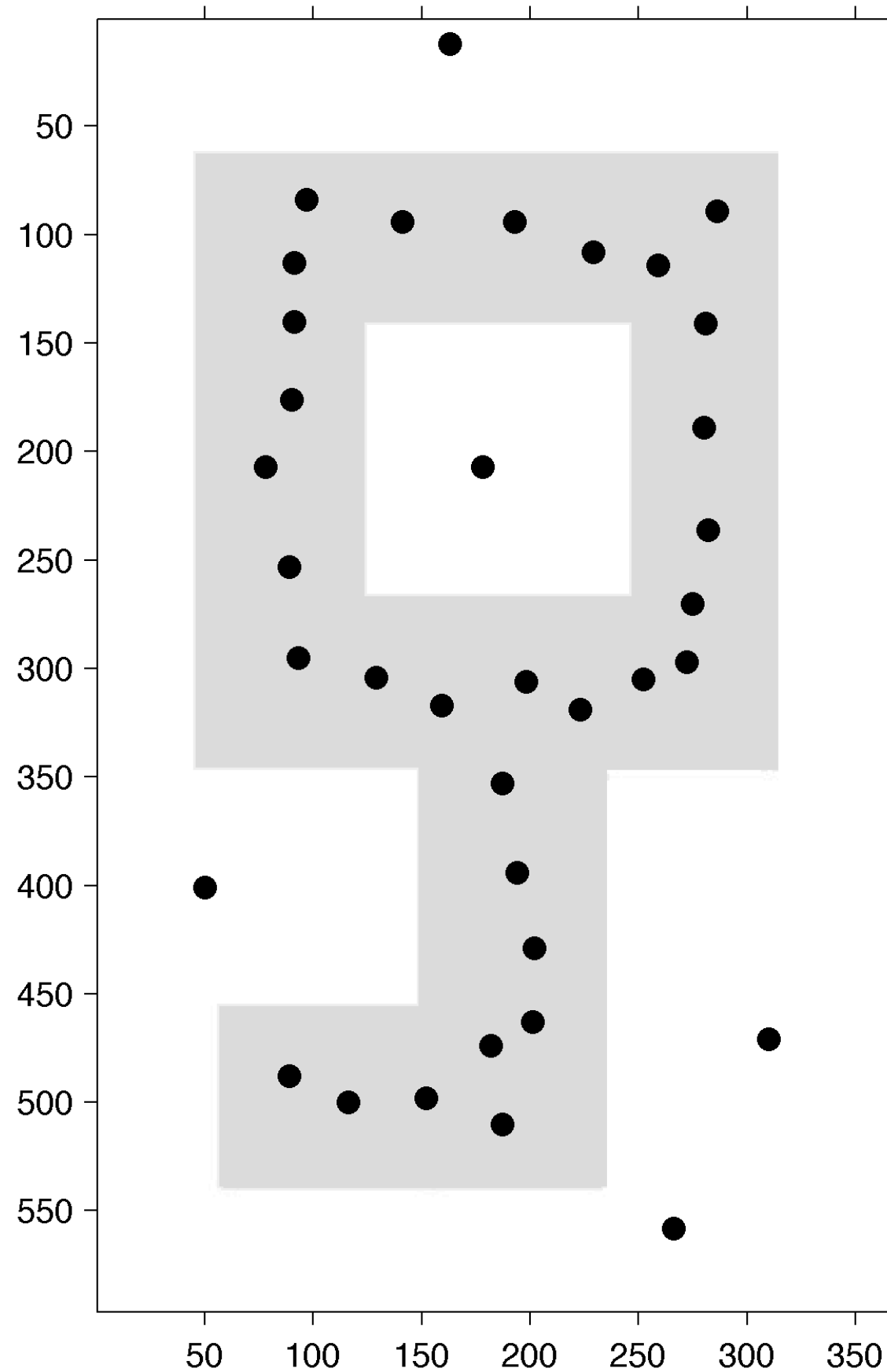
Control

Rips complex of point cloud data

Rips complex approximates the topology of the point cloud data by connecting two point cloud data, x_i and x_j , if $d(x_i, x_j) < \varepsilon$

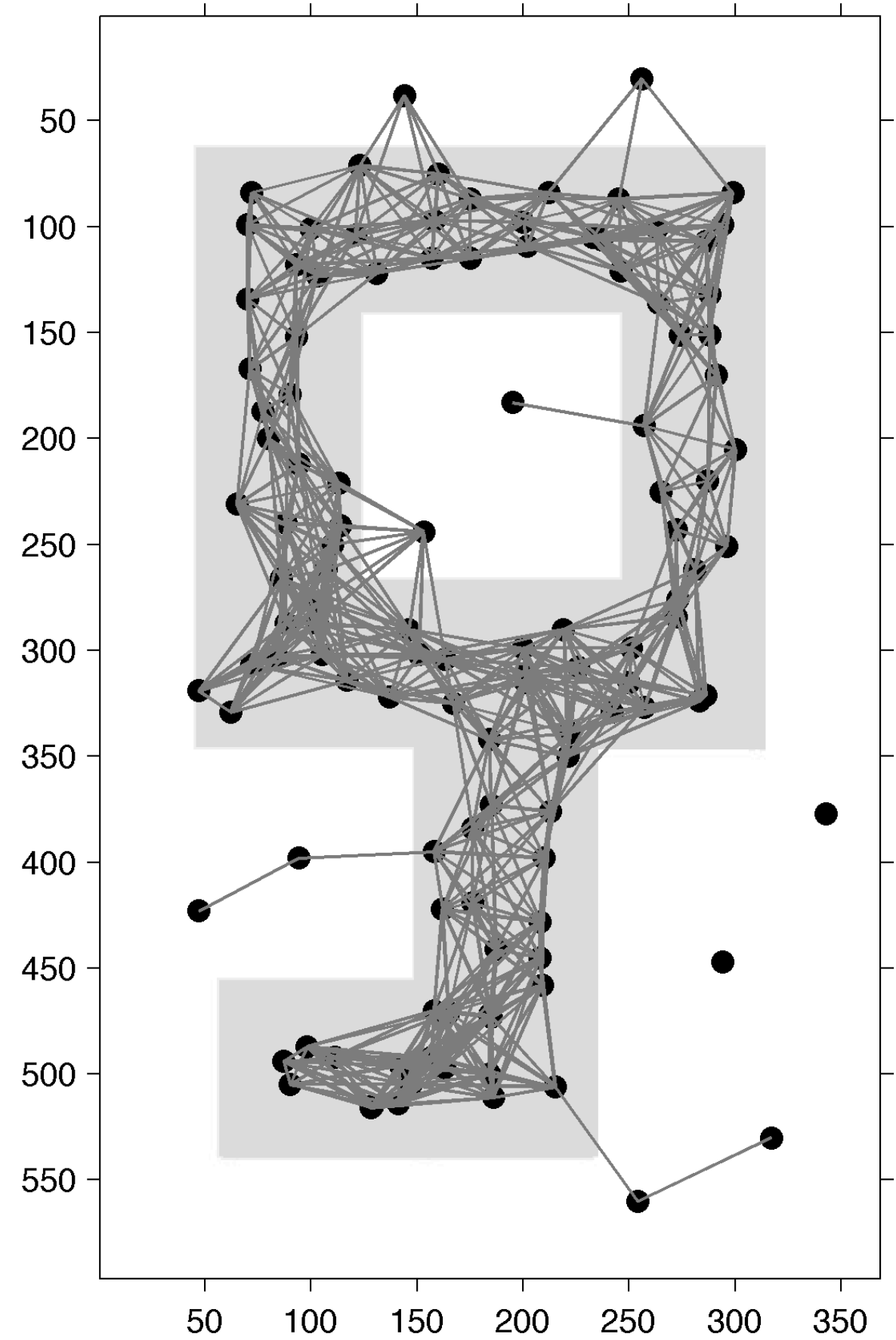
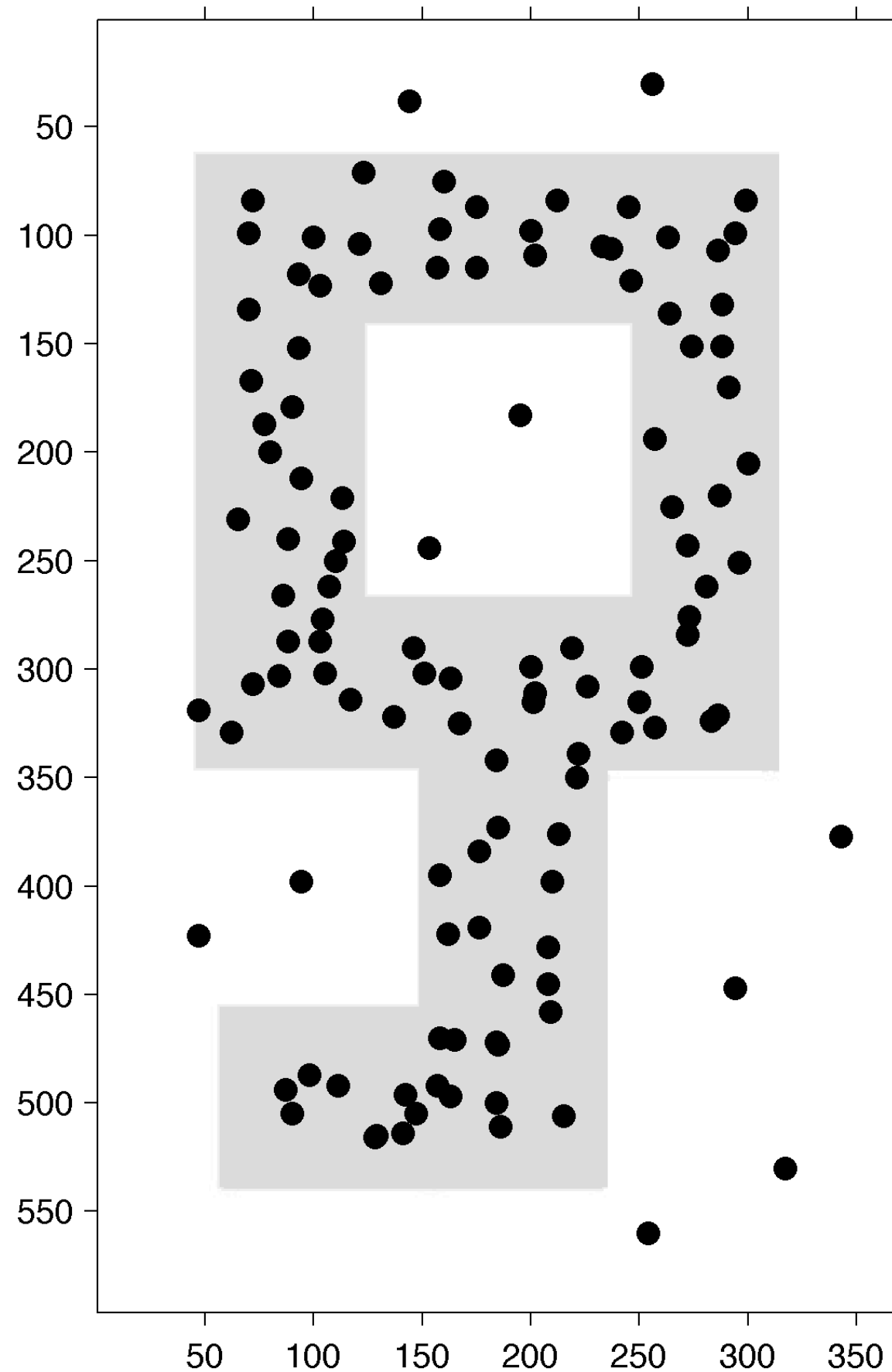
Rips complex of point cloud data

$\varepsilon = 70\text{mm}$



What's wrong with Rips complex

$\varepsilon = 70\text{mm}$

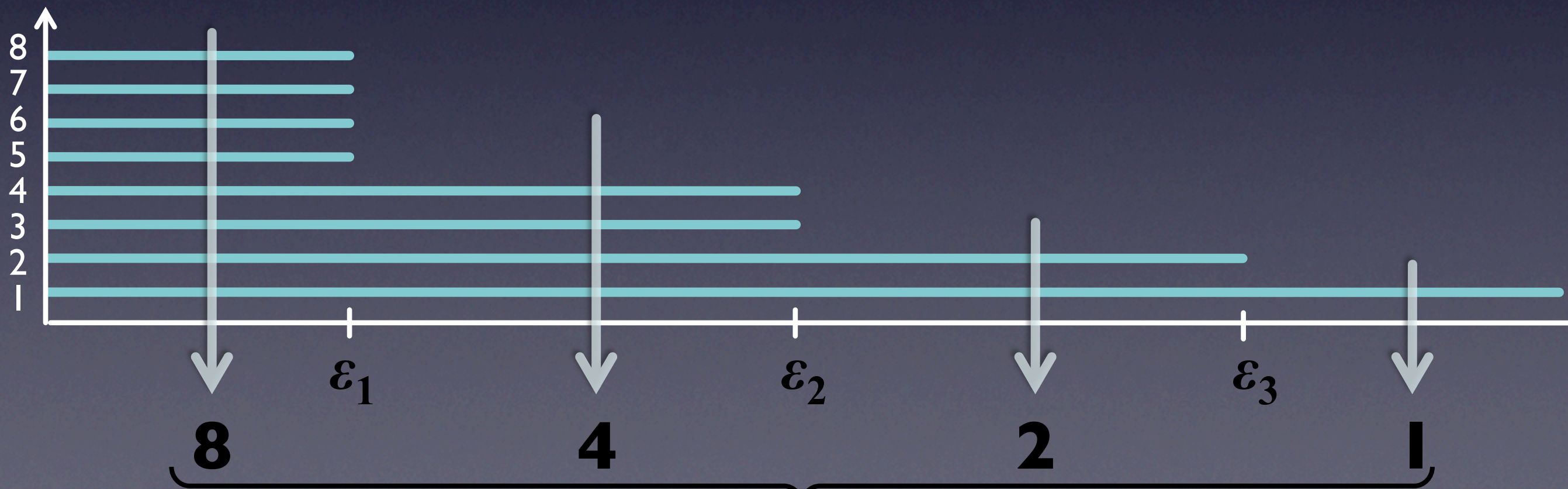
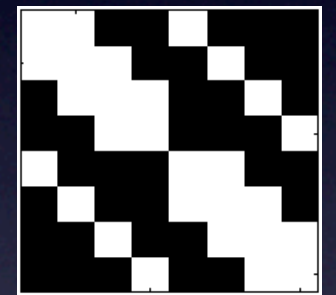
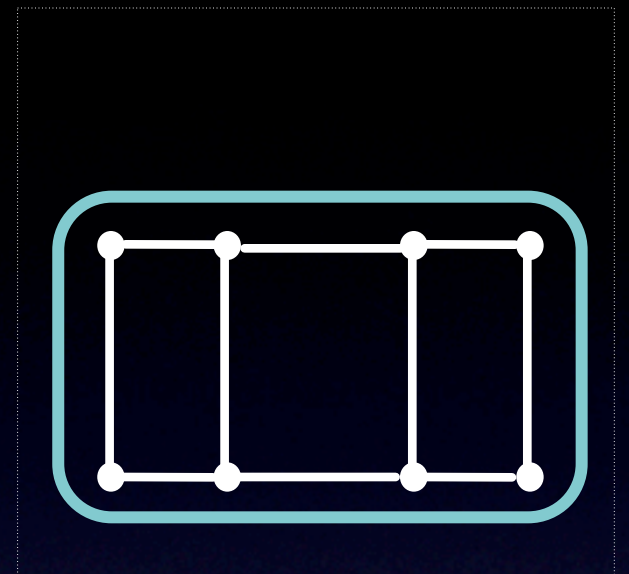
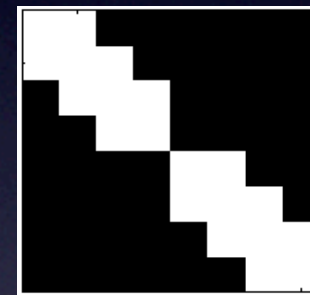
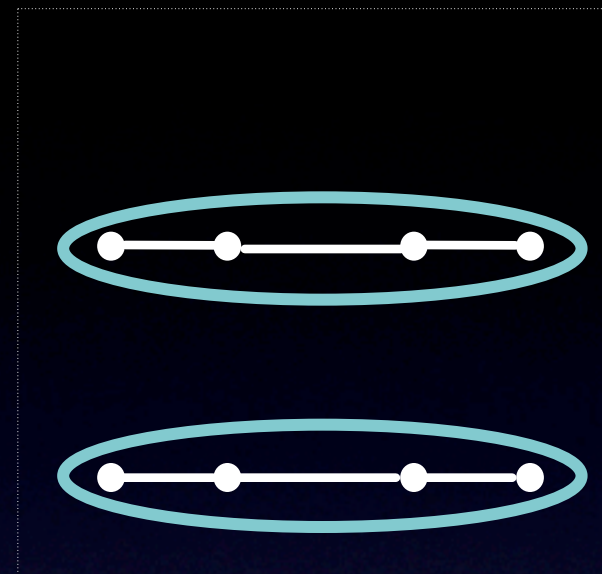
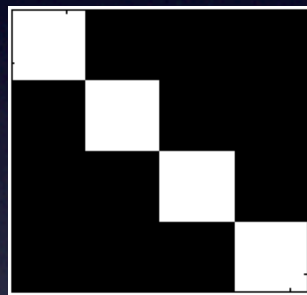
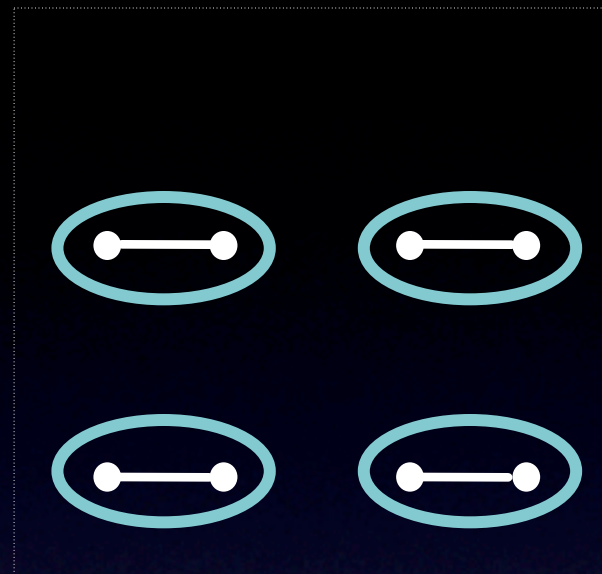
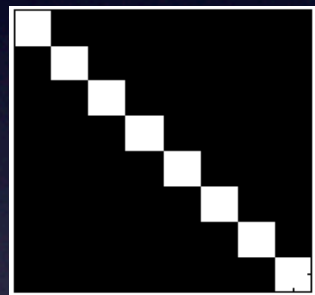
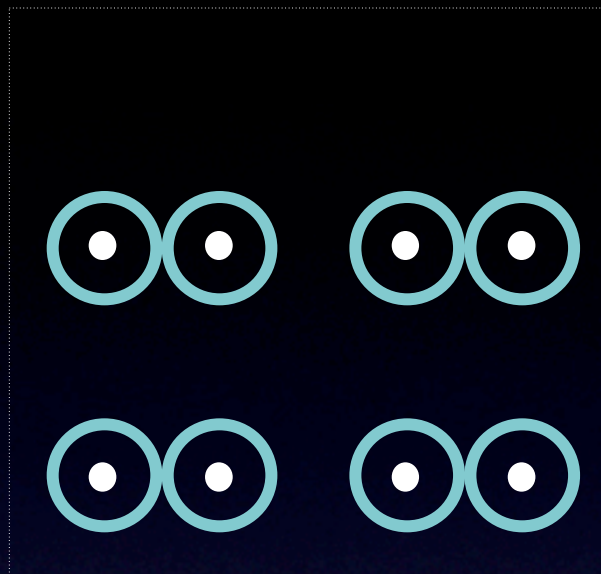


MATLAB DEMO

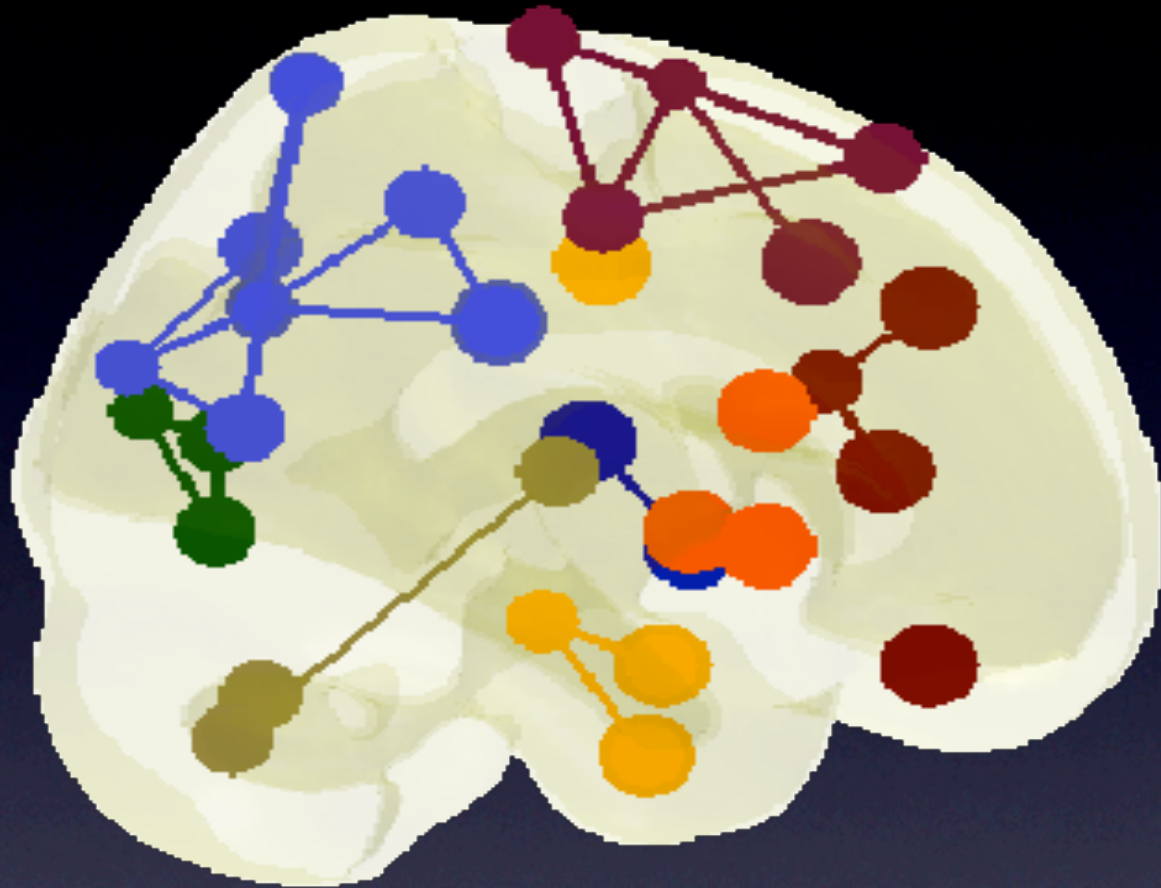
Epsilon Neighbor method

Rips Complex

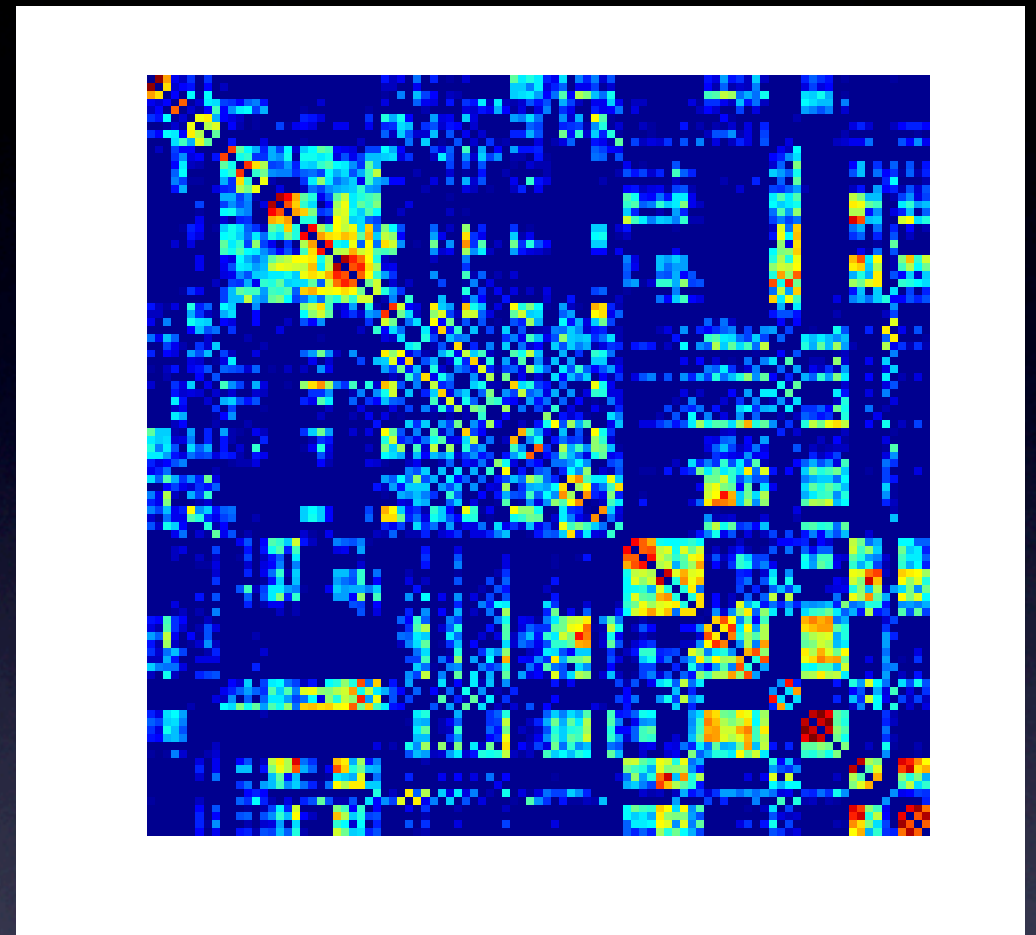
0-th Betti number over epsilon



Bar codes for brain network



PET measures on nodes

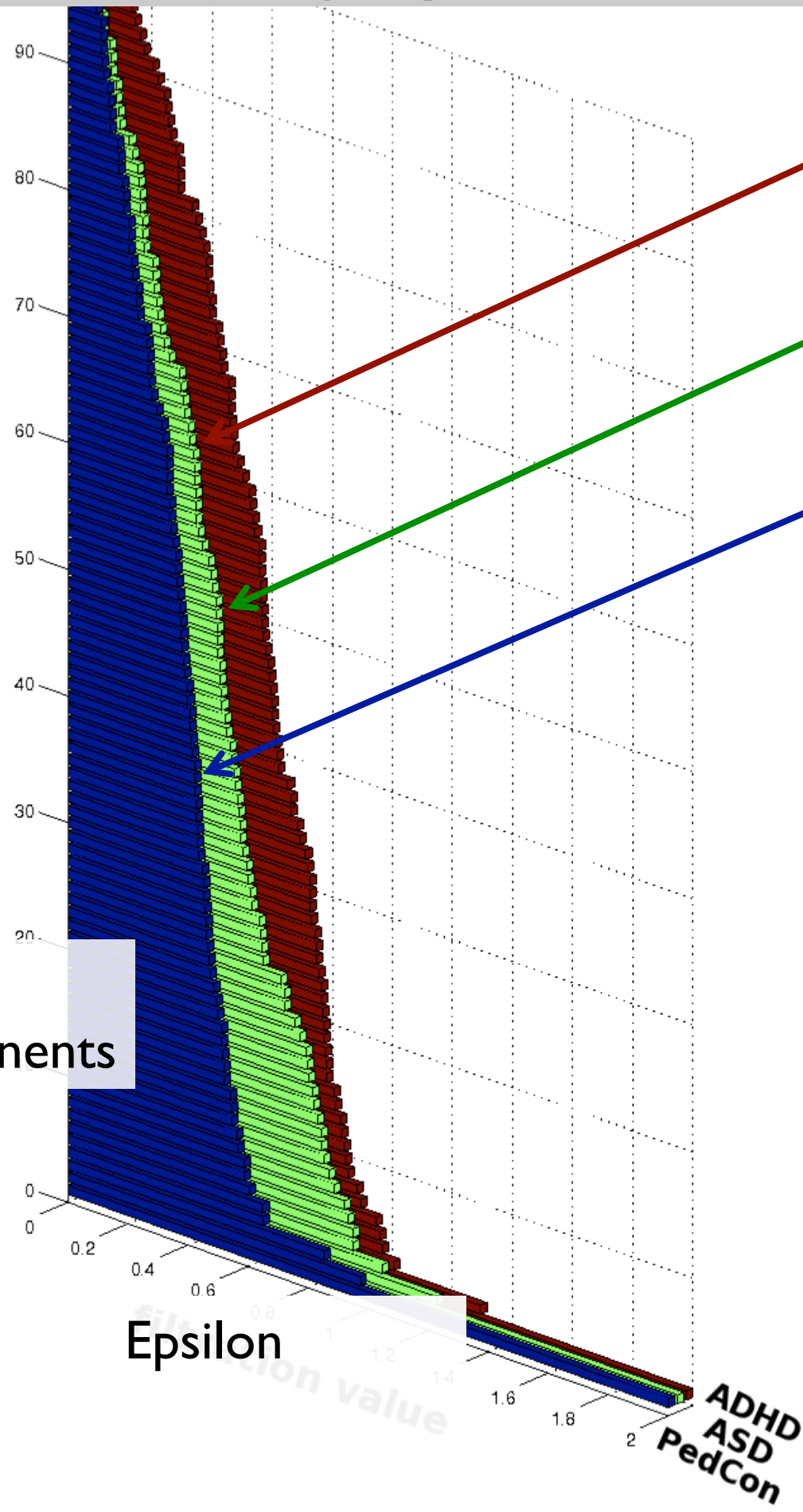


Correlation

$$\text{Distance} = 1 - \text{correlation}$$

Bar code on graph filtration

of components



24 attention deficit hyperactivity disorder (ADHD) children

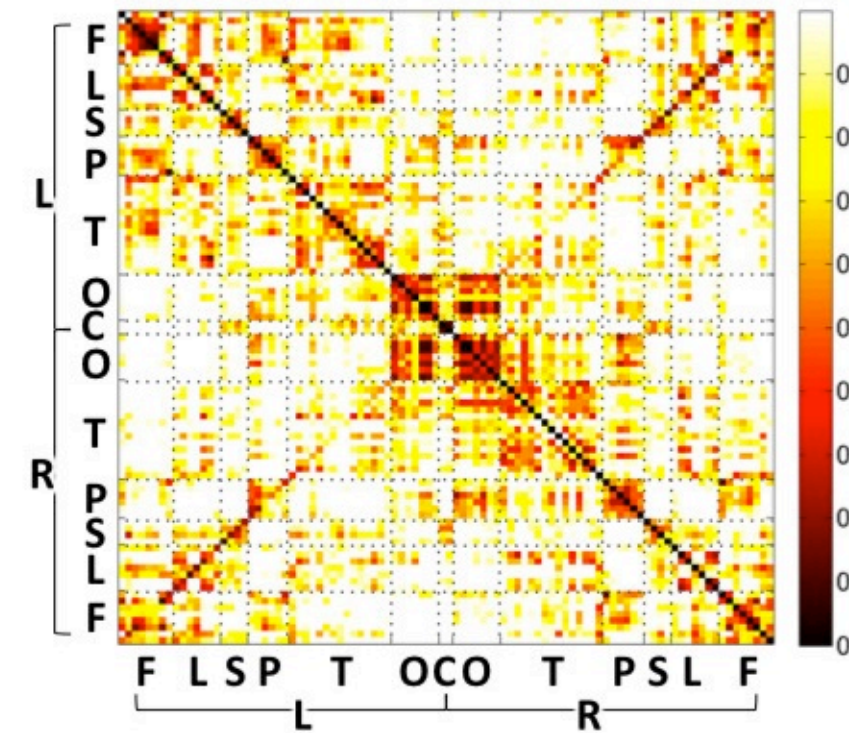
26 autism spectrum disorder (ASD) children

11 pediatric control subjects

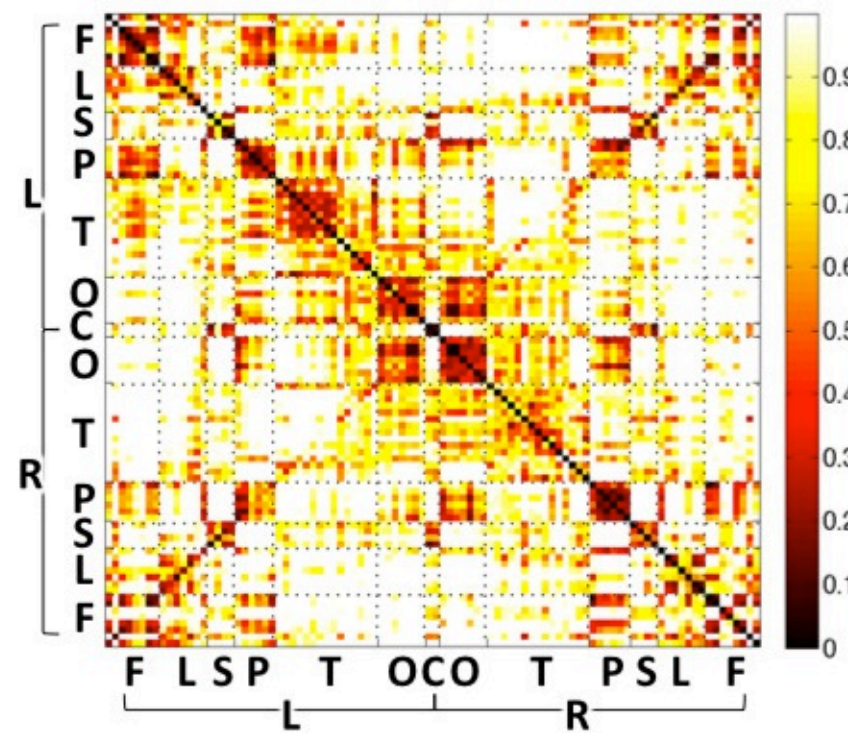
The brain network in control subjects merges to a single component faster than other populations!

Connectivity matrix of brain network

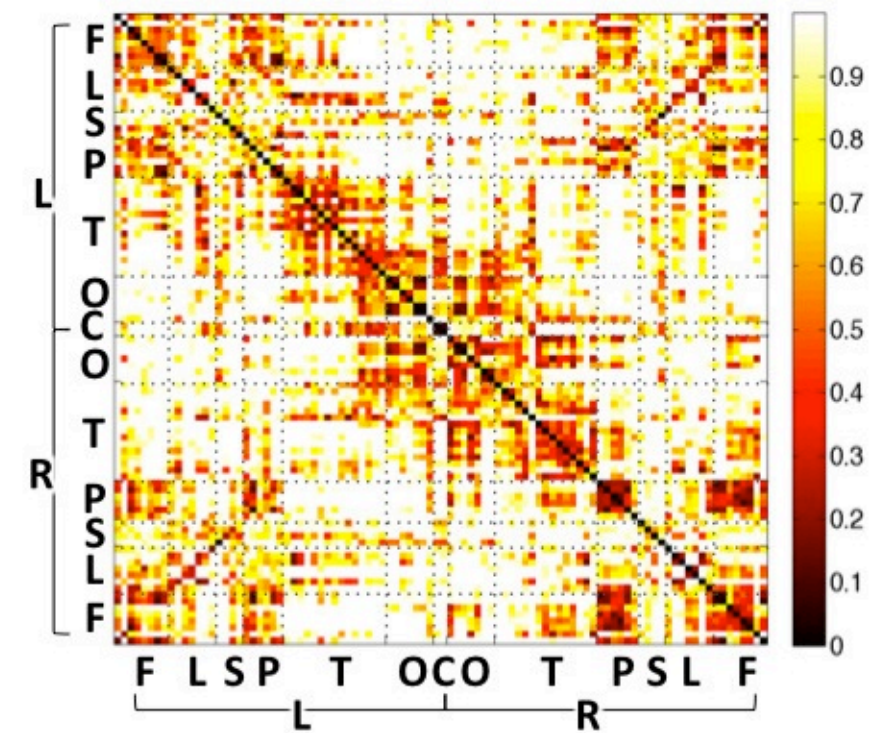
(a) ADHD



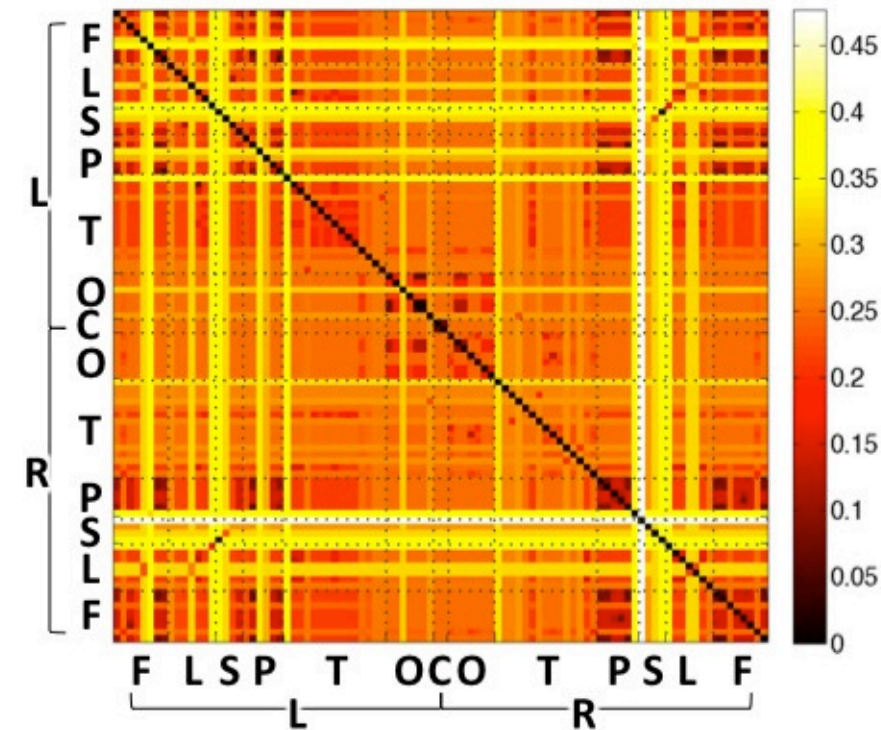
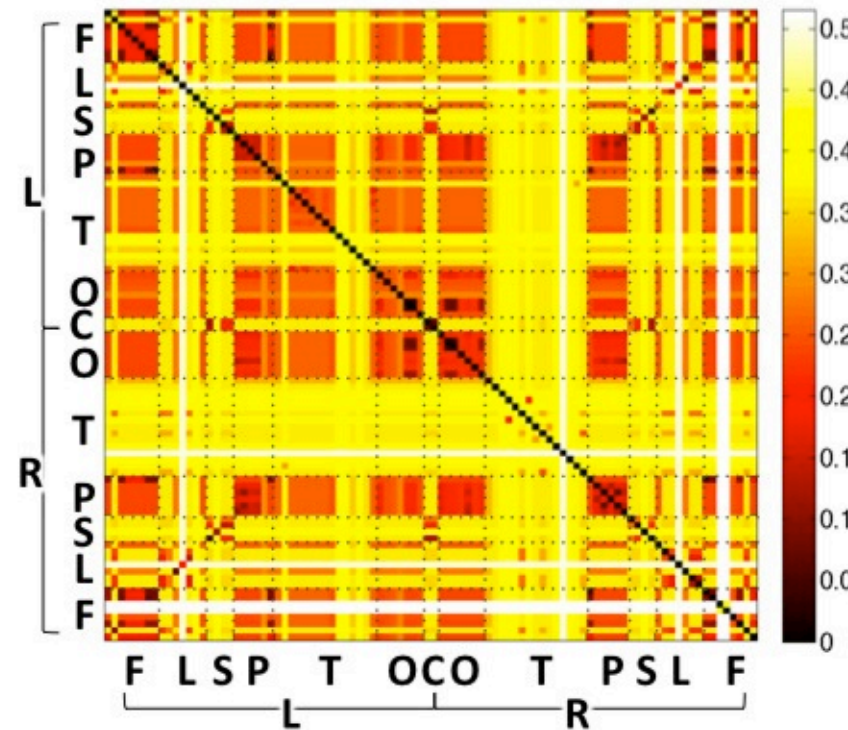
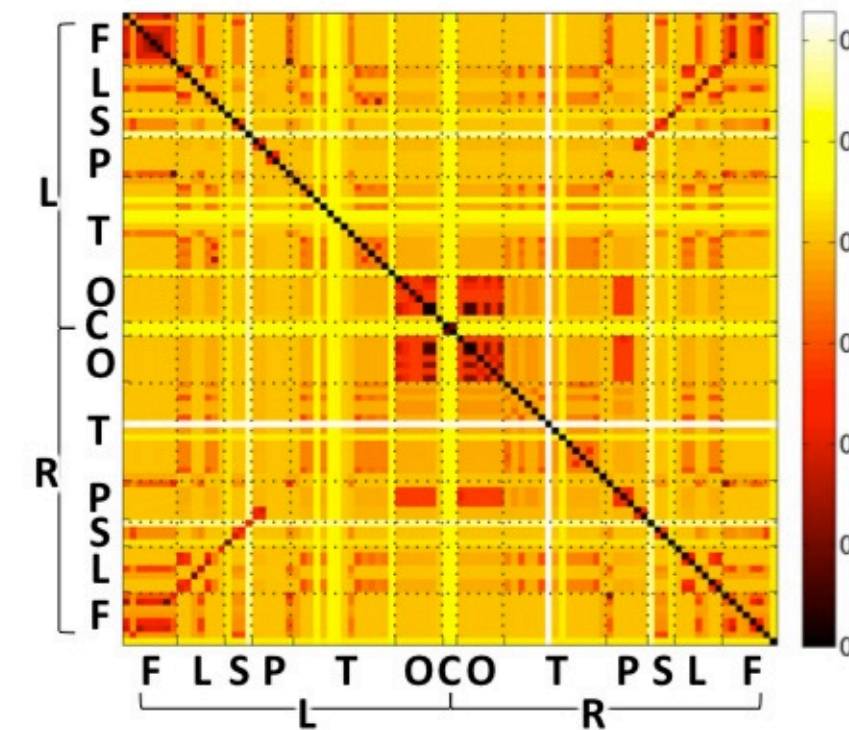
(b) ASD



(c) PedCon



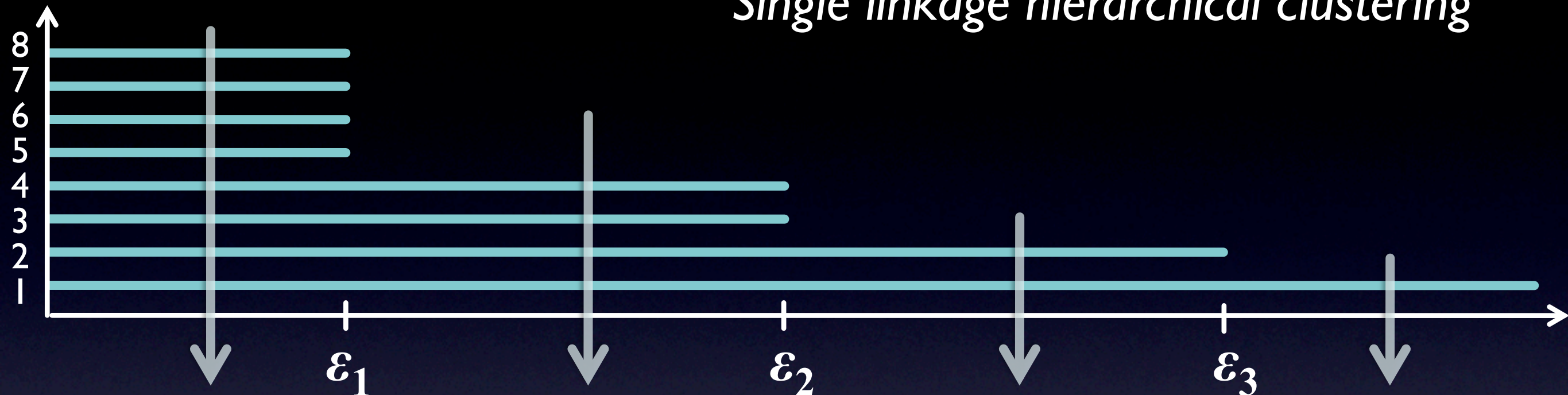
(d) Pairwise Distance Matrix = 1 - correlation



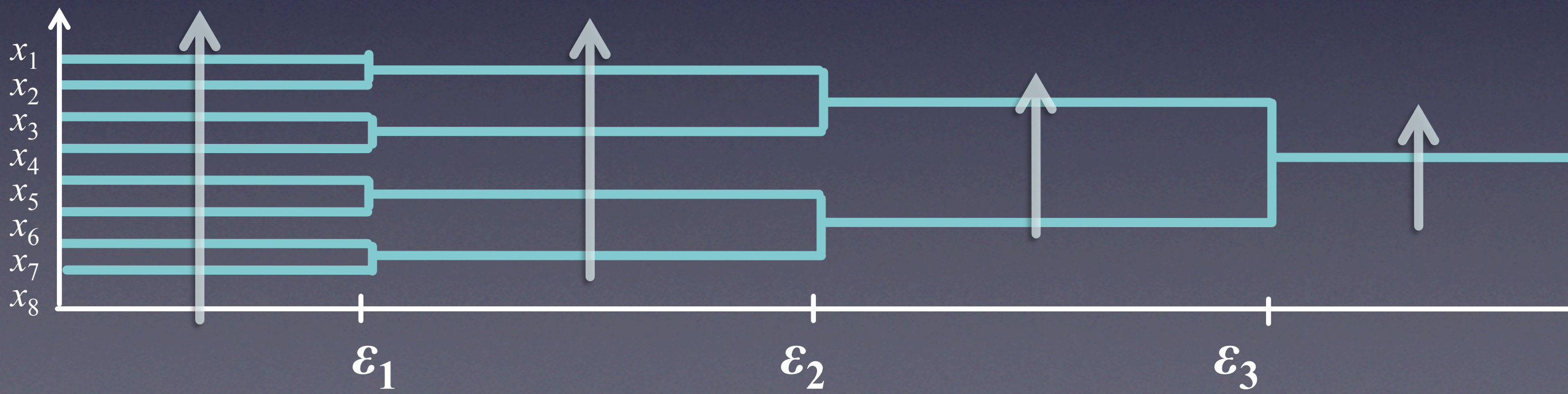
(e) Single Linkage Connectivity matrix

Permuted bar code = Dendrogram

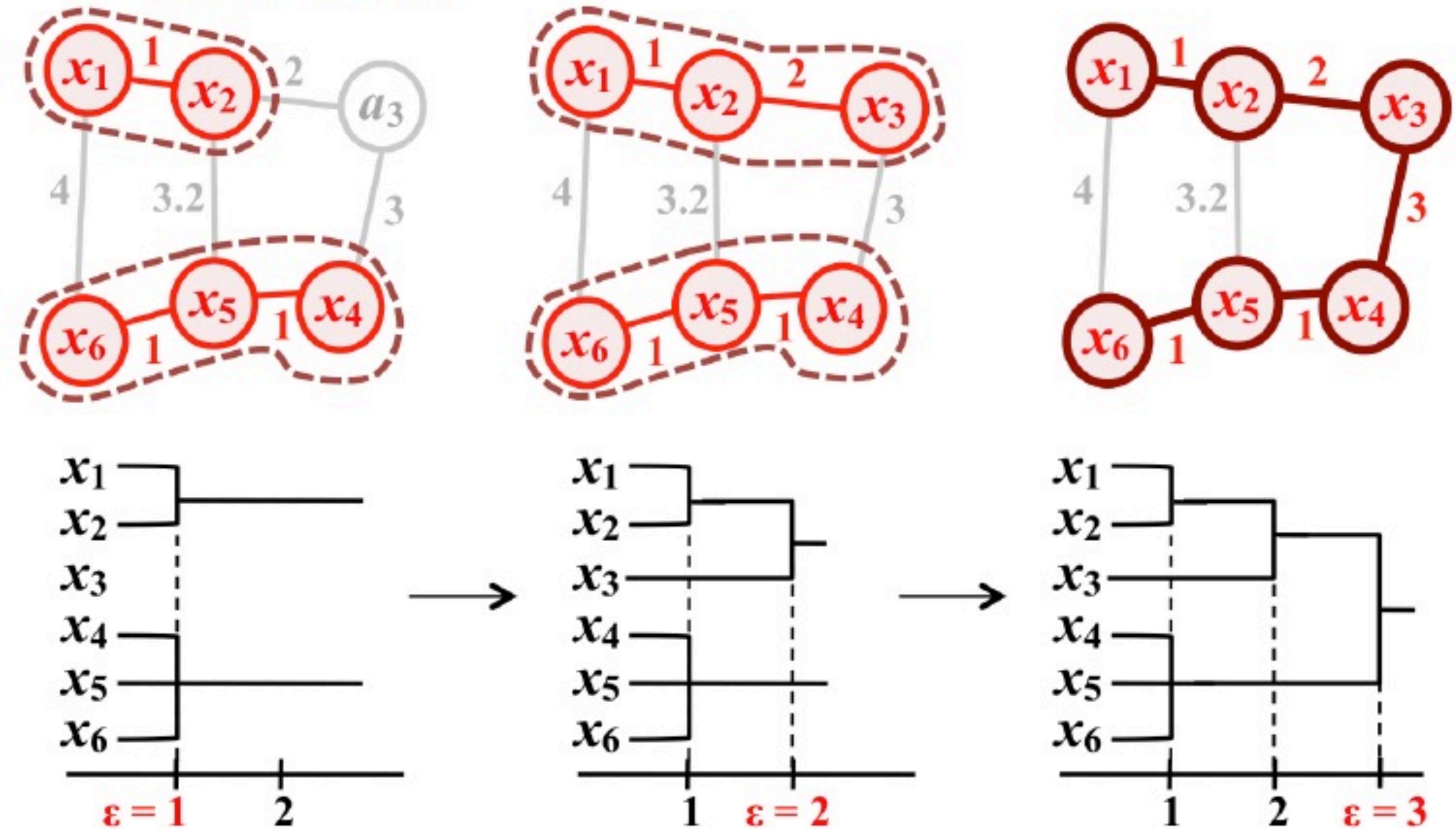
Single linkage hierarchical clustering



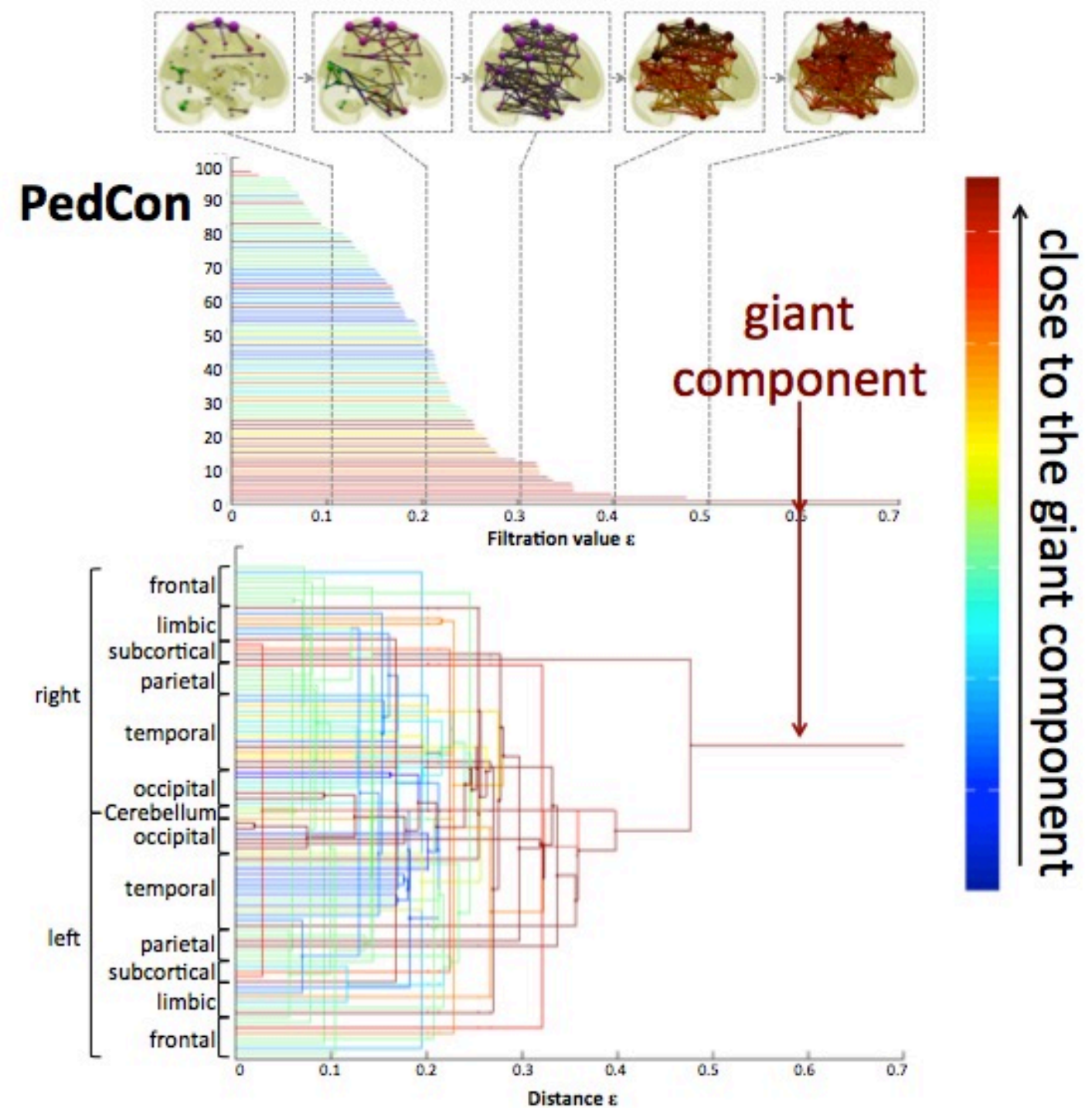
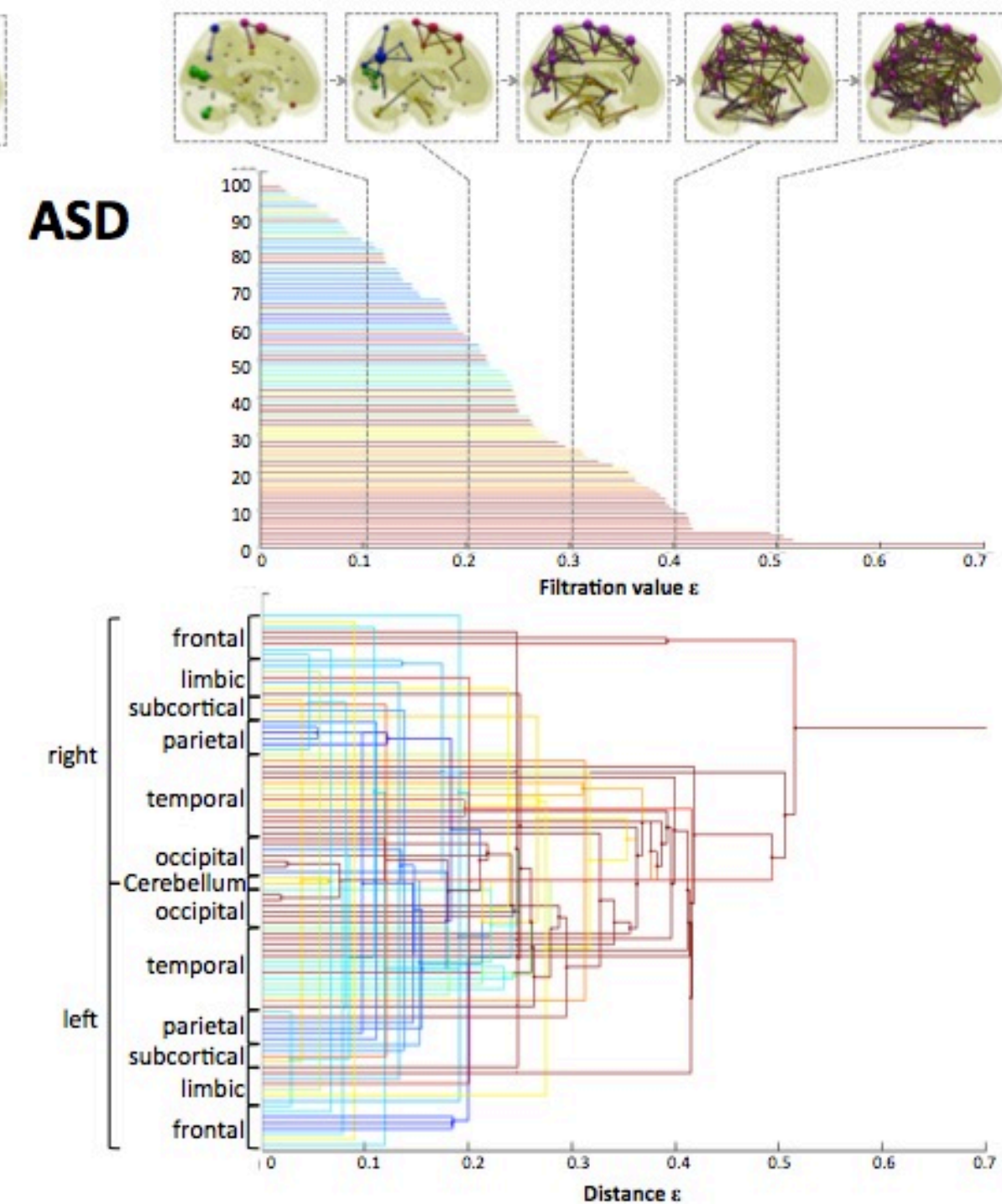
Rearrange the barcode according to the node index



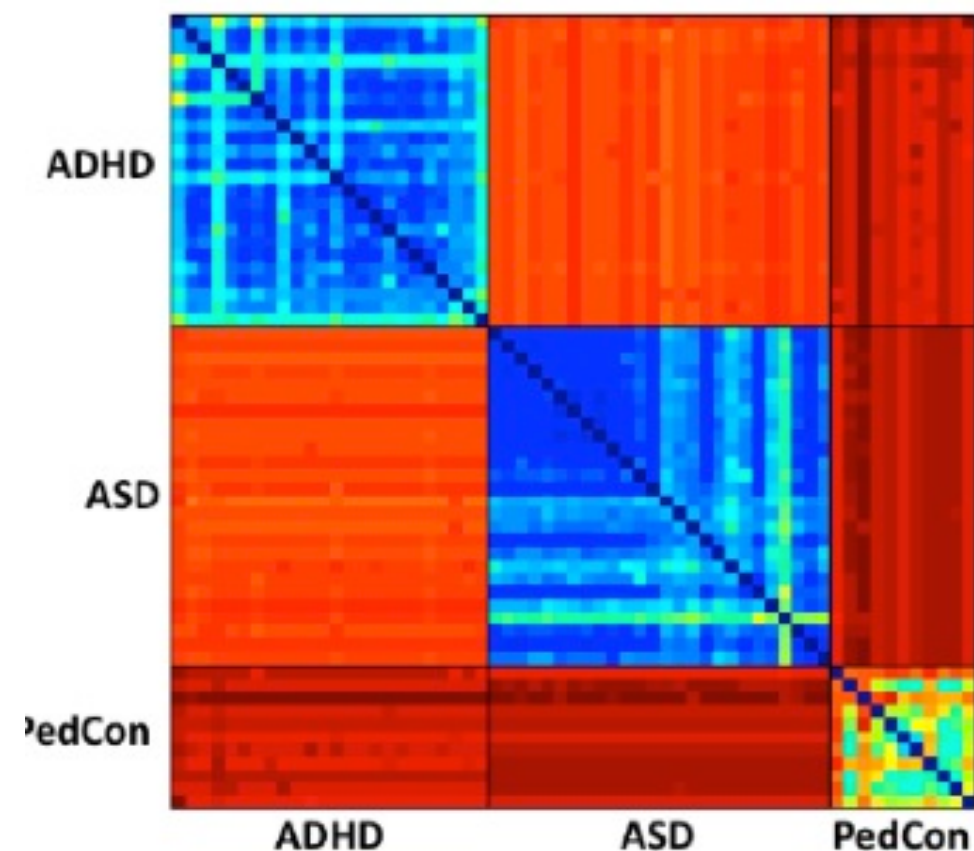
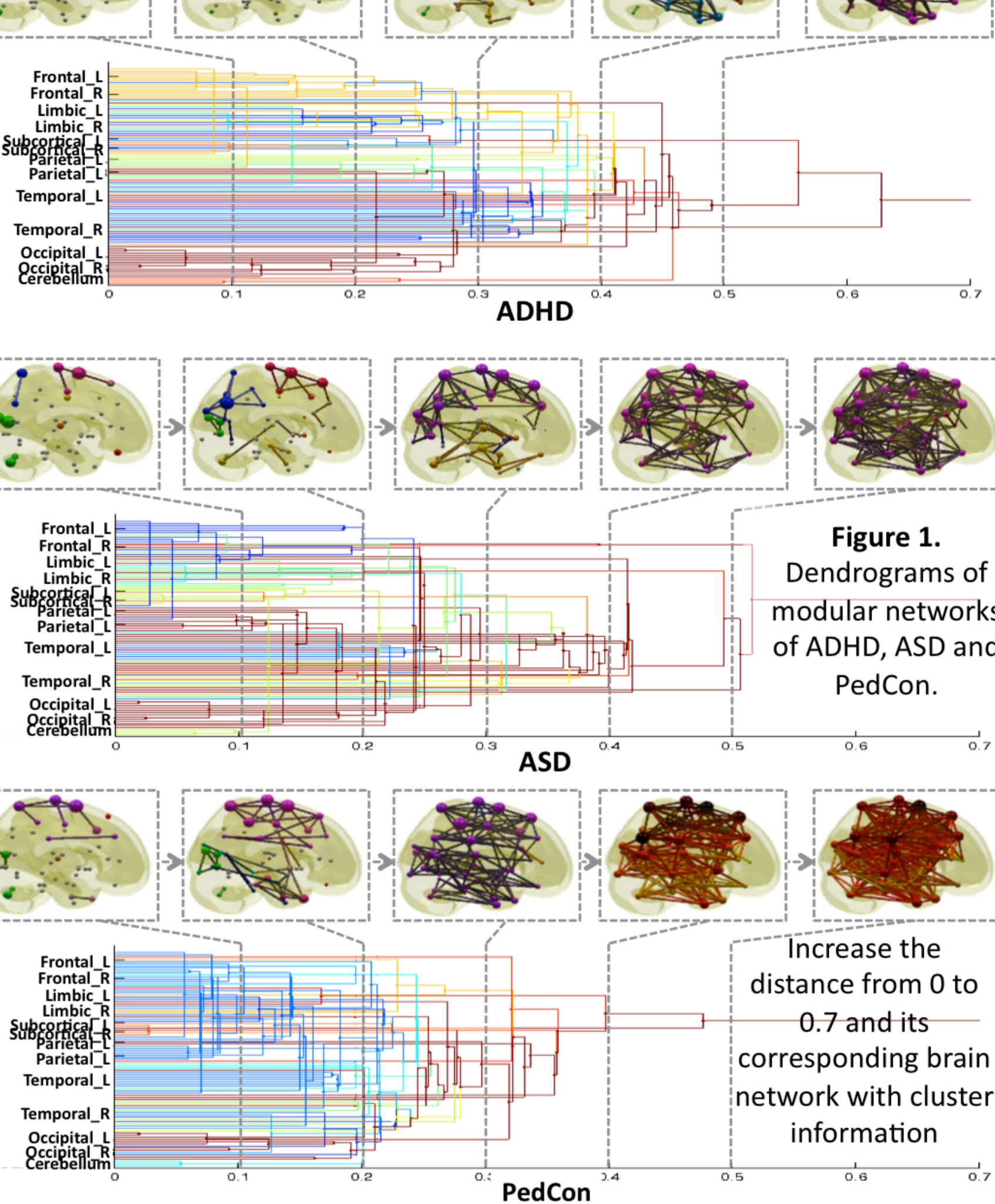
Network filtration = dendrogram construction



Brain network as dendrogram

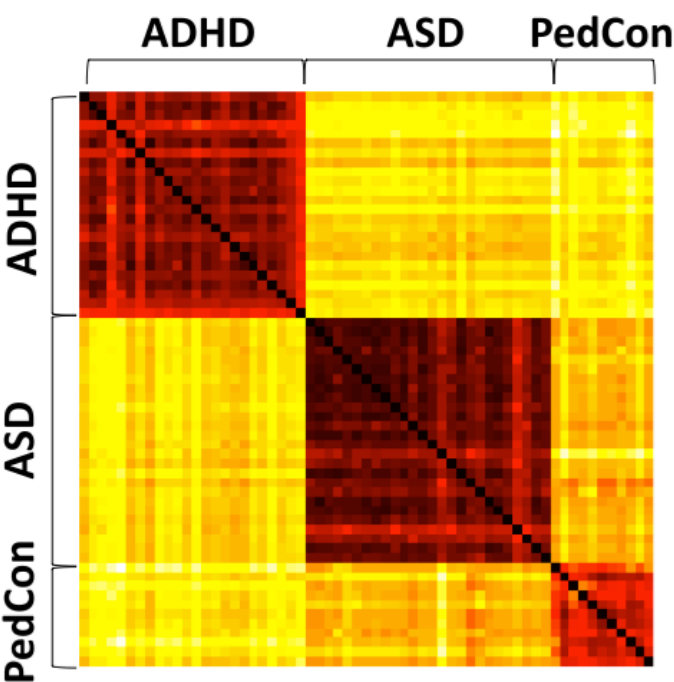


The network difference can be measured in terms of the dendrogram shape difference.

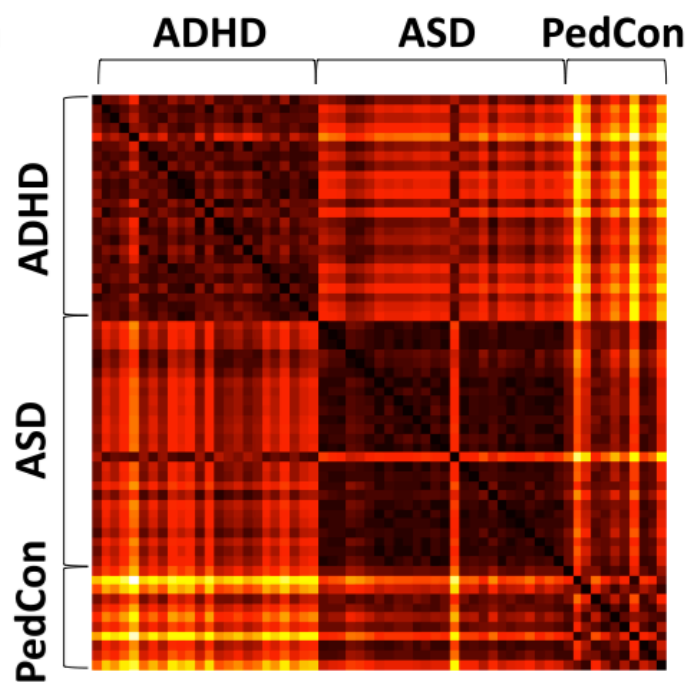


Gromov-Hausdorff distance

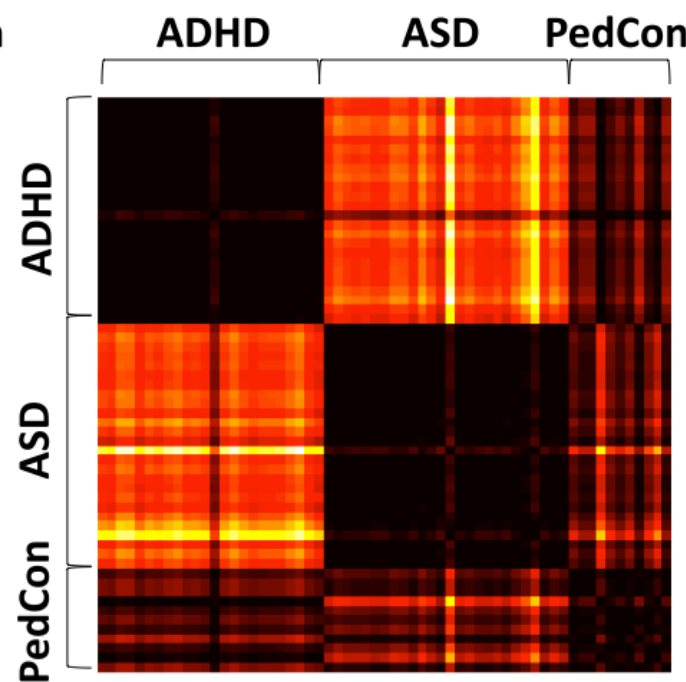
Discrimination Accuracy



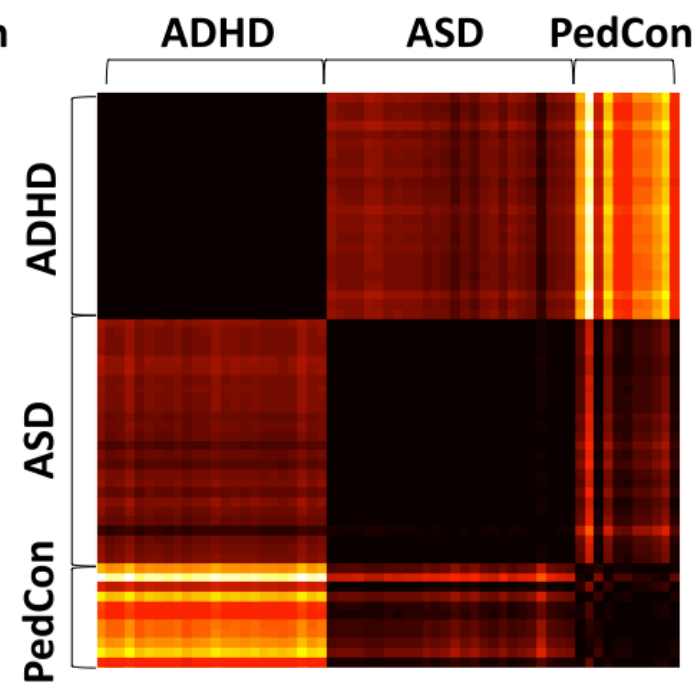
(a) GH distance
cluster_acc = 100 %
 $|w-b| = 0.4904$



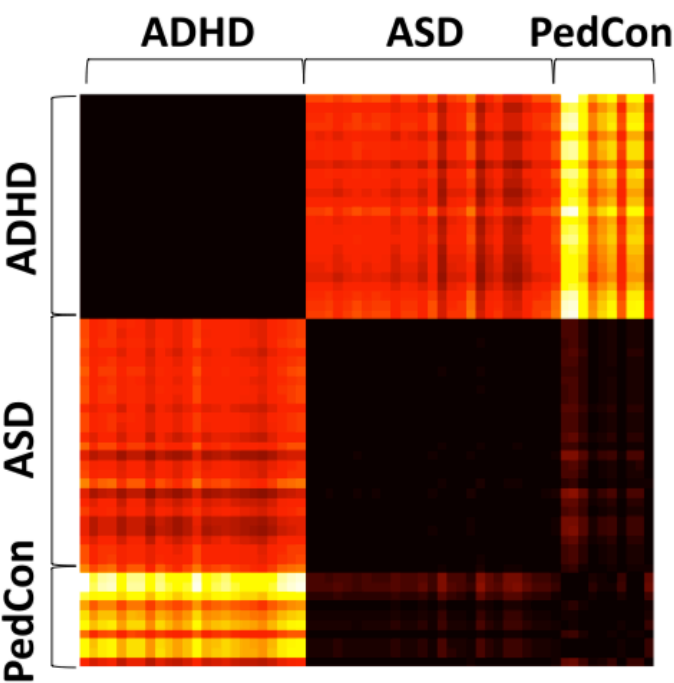
(b) Bottleneck distance
cluster_acc = 52.46 %
 $|w-b| = 0.1879$



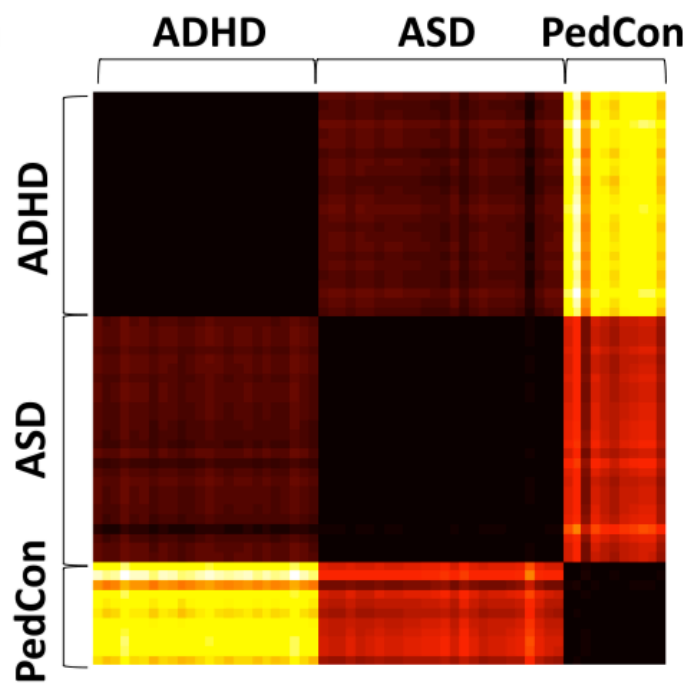
(c) Assortativity
cluster_acc = 77.05 %
 $|w-b| = 0.2982$



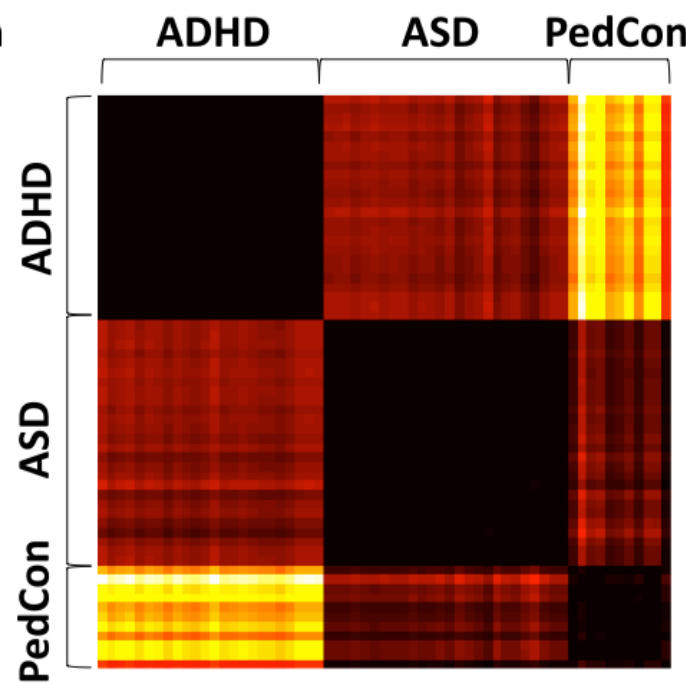
(d) Betweenness Centrality
cluster_acc = 83.61 %
 $|w-b| = 0.2321$



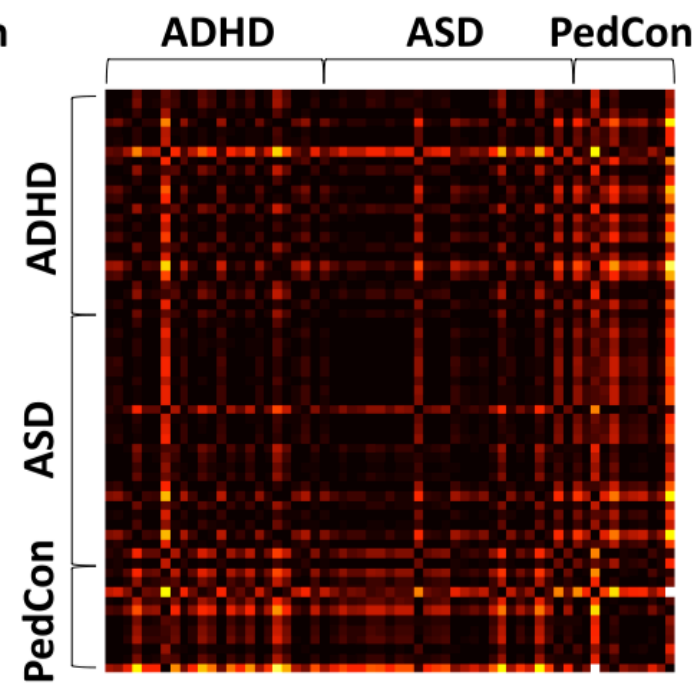
(e) Clustering Coefficient
cluster_acc = 85.25 %
 $|w-b| = 0.3382$



(f) Characteristic Path Length
cluster_acc = 100 %
 $|w-b| = 0.3015$



(g) Small-worldness
cluster_acc = 100 %
 $|w-b| = 0.2867$



(h) Modularity
cluster_acc = 45.90 %
 $|w-b| = 0.0274$

Thank you



Papers and MATLAB codes can be downloaded
from www.stat.wisc.edu/~mchung