



Brain & Cognitive  
Sciences



University of Wisconsin  
**SCHOOL OF MEDICINE  
AND PUBLIC HEALTH**

# Topological characterization of brain connectivity using white matter fiber bundles

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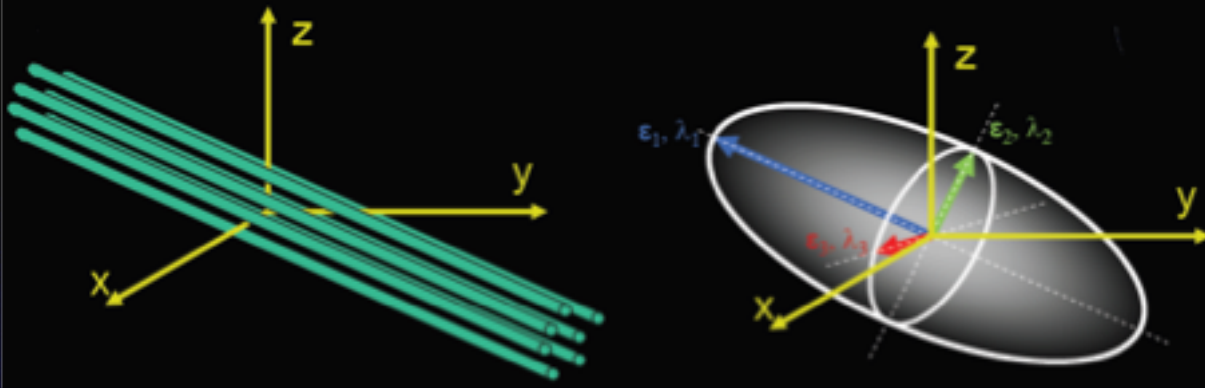


# Abstract

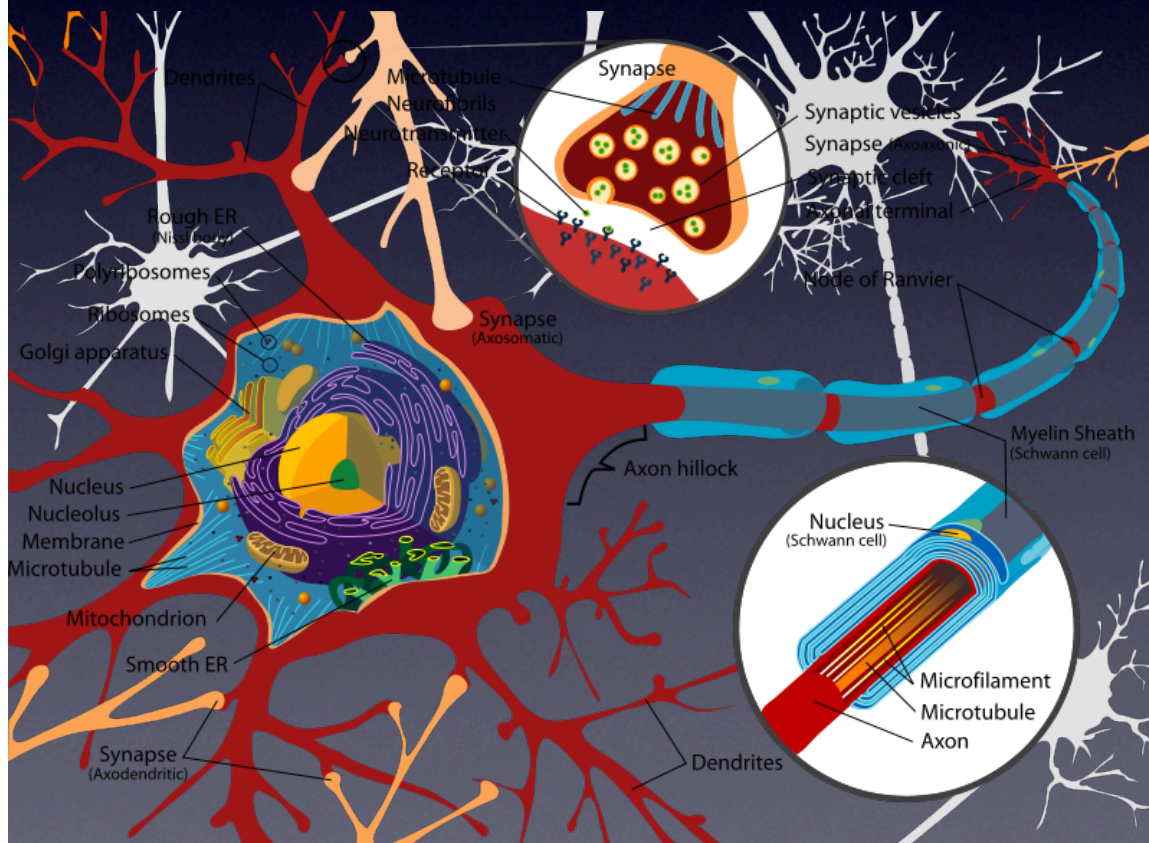
Structural brain connectivity has been mainly modeled as a network graph using white matter fiber tracts in DTI. The whole gray matter has been traditionally parcellated into disjoint regions. Fiber tracts provide information of how one gray matter region is connected to another via a connectivity matrix. The connectivity matrix is then thresholded to produce a binarized adjacency matrix, which is further used in constructing a graph. However, there is no gold standard for gray matter parcellation, which makes the identification of node, depends on the choice of parcellation. Depending on the scale of parcellation, the parameters of graph, which characterize graph topology, varies considerably. Another problem of the parcellation is the arbitrariness of thresholding the connectivity matrix. The topological parameters such as degree, sparsity and clustering coefficients change significantly depending on the level of threshold. The problems of parcellation and the subsequent arbitrary thresholding can be avoided if we do not use any parcellation in building the network. So the question is whether it is possible to construct a network graph without the usual parcellation scheme. We present a novel topological network graph construction technique called the epsilon-neighbor method that avoids parcellation and the subsequent connectivity matrix thresholding. The method is applied in quantifying abnormal connectivity in autism.

# Diffusion Tensor Imaging

Mori and van Zijl NMR Biomed 2002

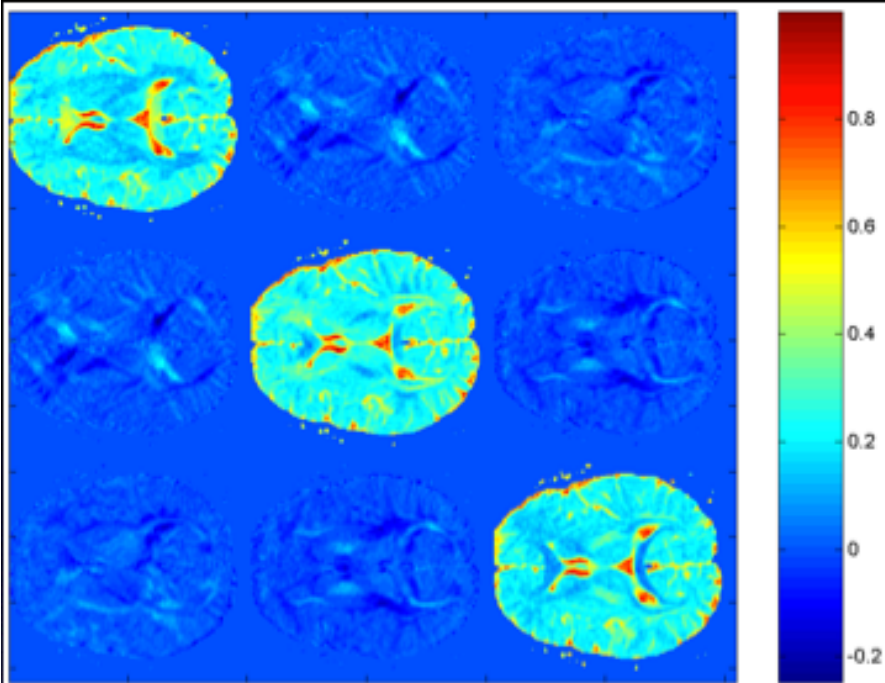


The movement of anisotropic water diffusion can be measured using DTI



The direction of neuronal filaments in the axon dictates the movement of water diffusion.

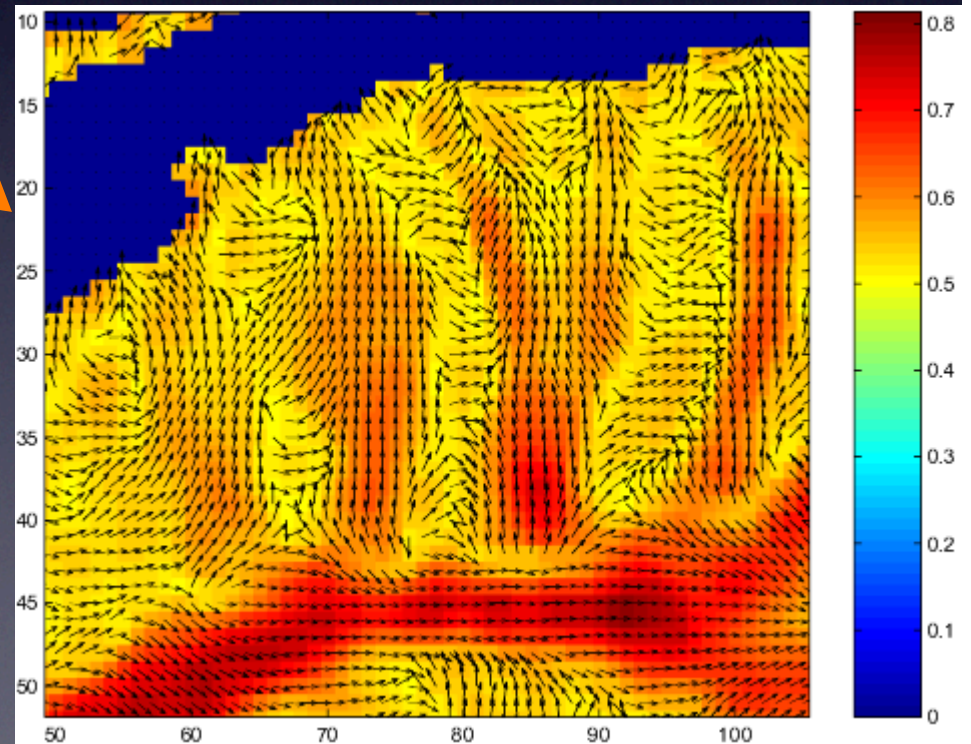




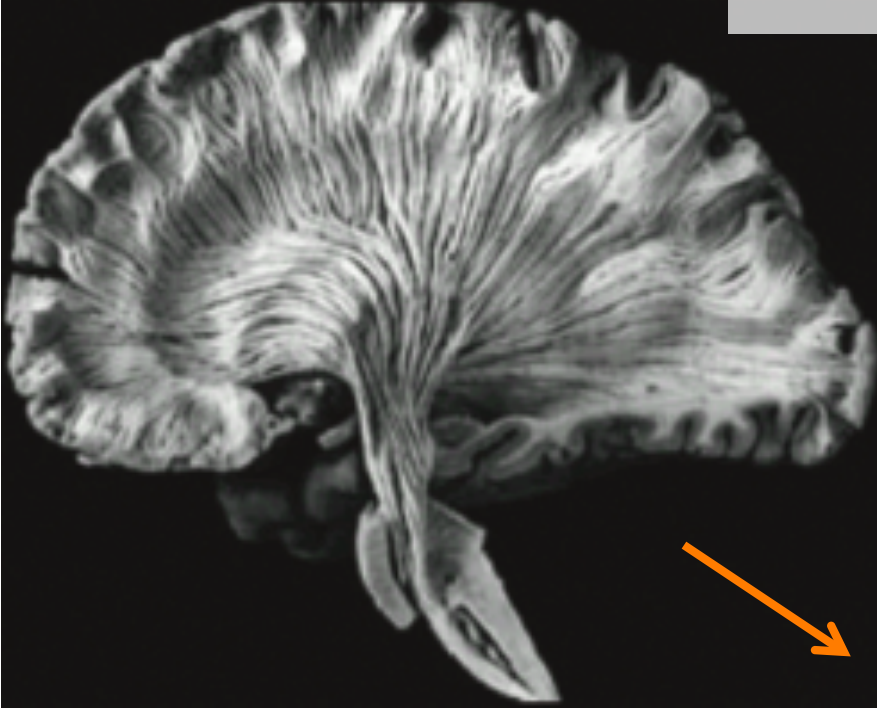
Direction of diffusion is encoded in 3x3 matrix  $D$  (diffusion tensor)

Principal eigenvector of  $D$

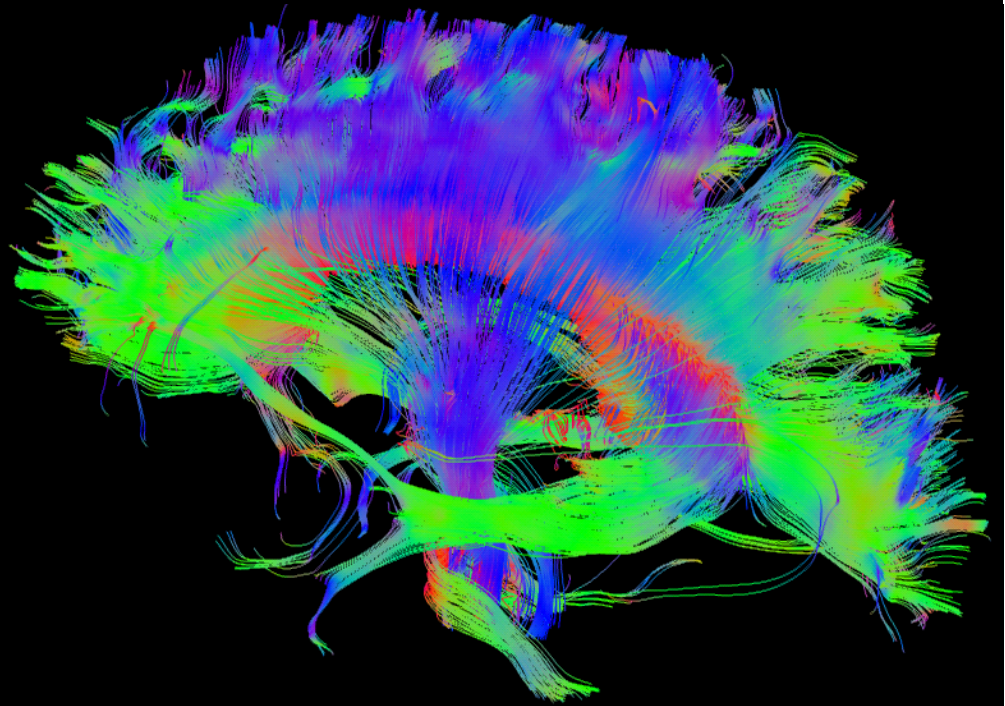
Tractography done using the second order Runge-Kutta algorithm with TEND (Lazar et al., HBM 2003)



# White Matter Fiber Tractography



Postmortem



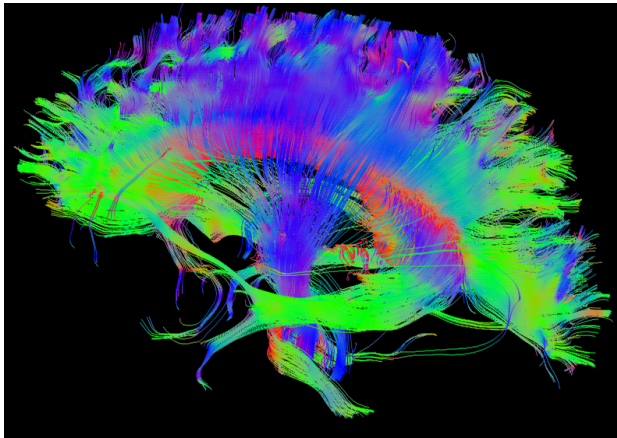
Reconstructed  
0.5 million tracts



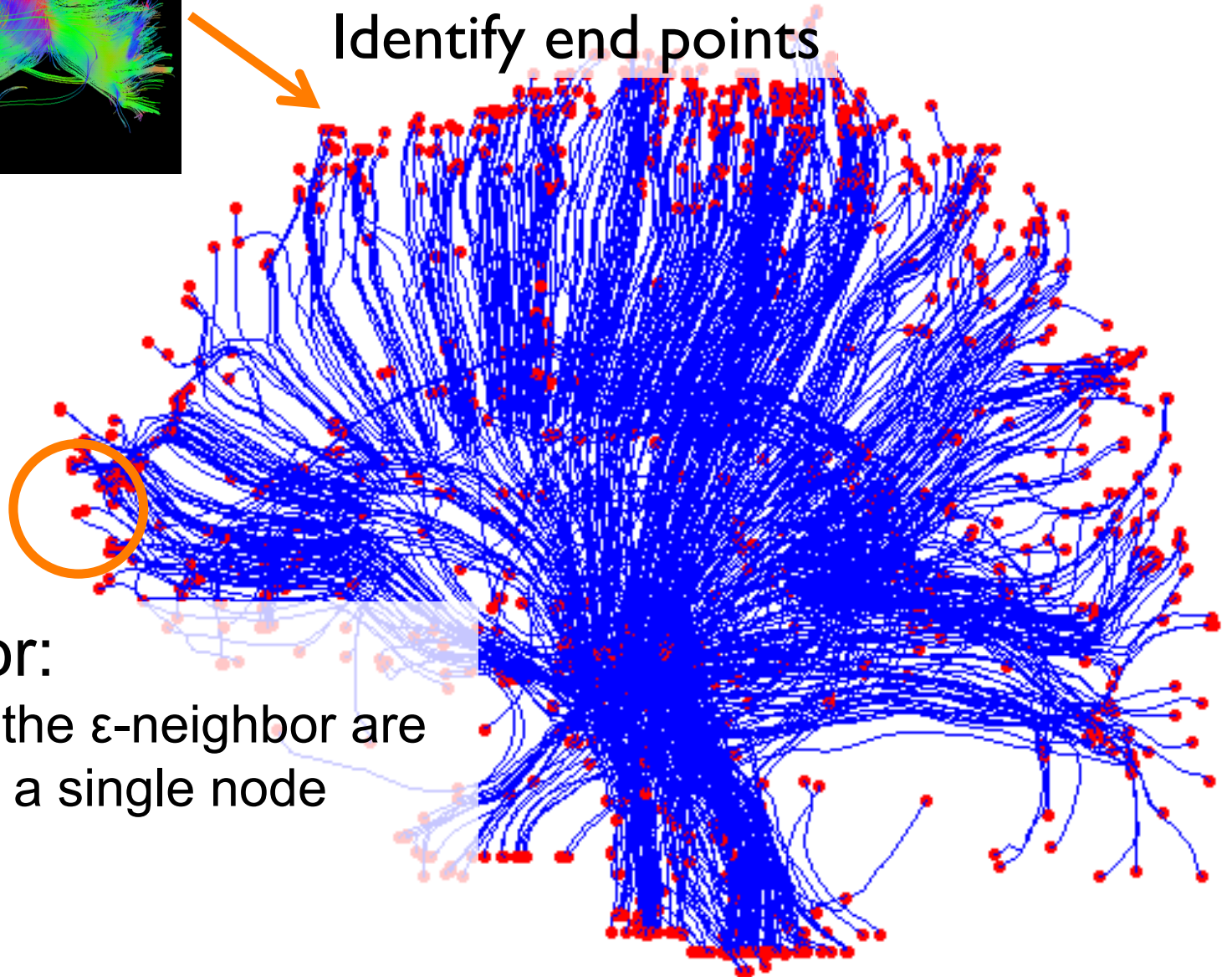
# Structural connectivity in DTI:

Structural connectivity will be explored using graph theoretic approaches.

# Graph construction



Identify end points

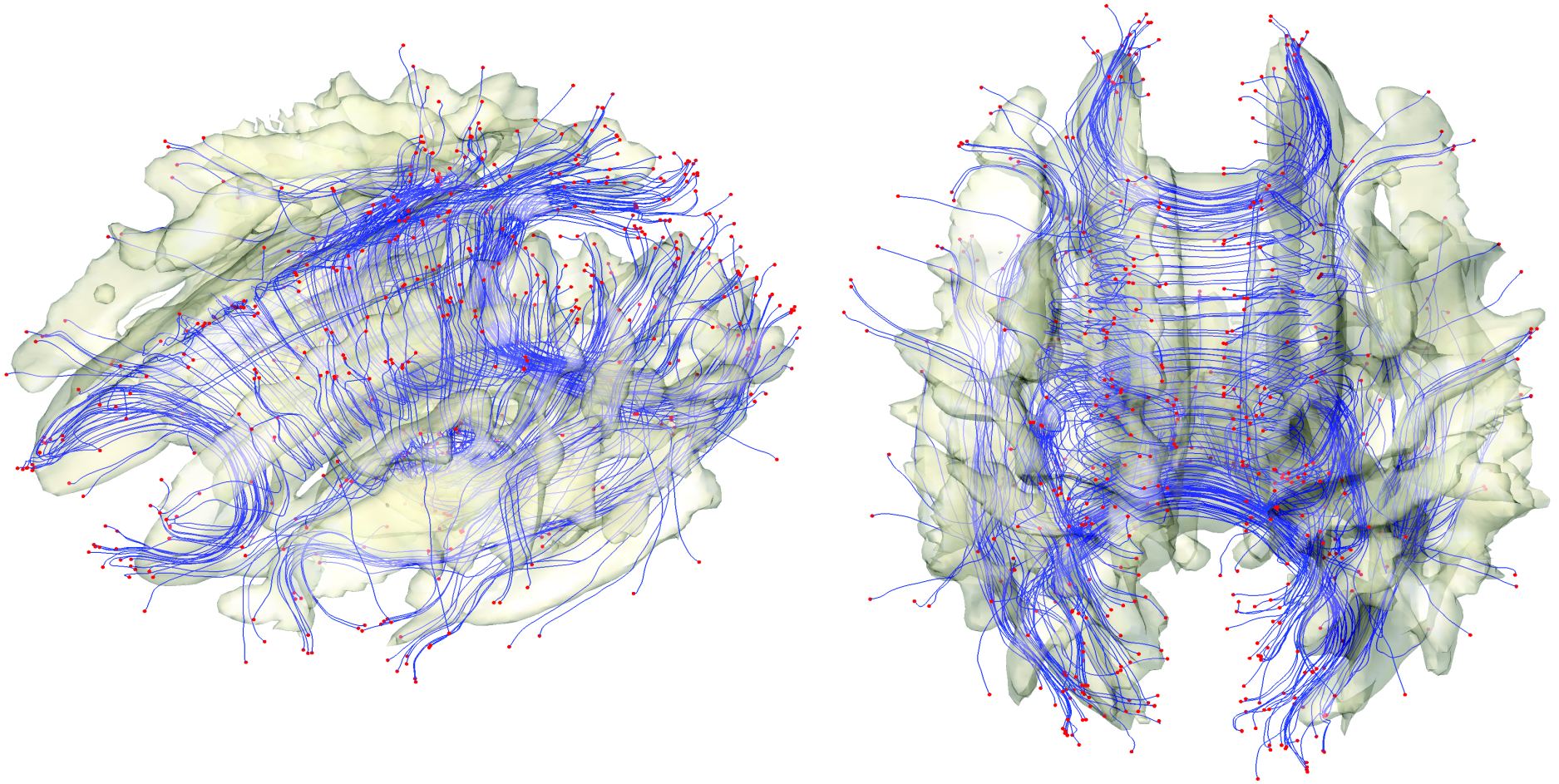


$\epsilon$ -neighbor:

All points in the  $\epsilon$ -neighbor are identified as a single node in a graph



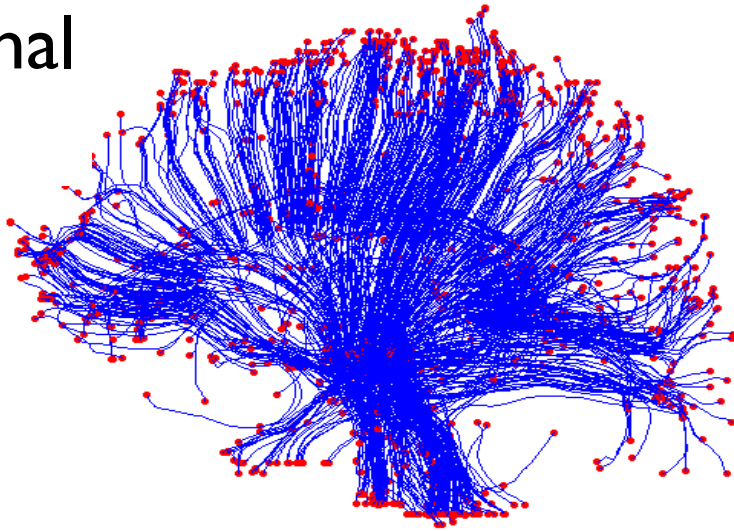
# End points of tracts



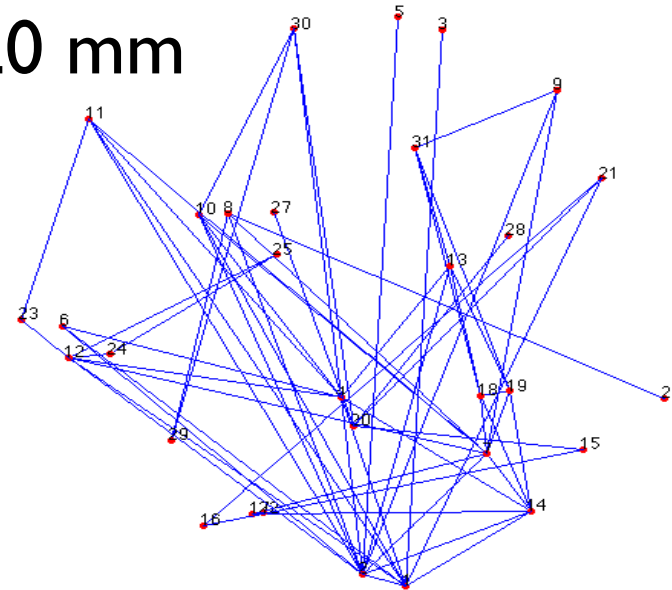
Surface: white matter boundary

# $\epsilon$ -neighbor graphs with different $\epsilon$

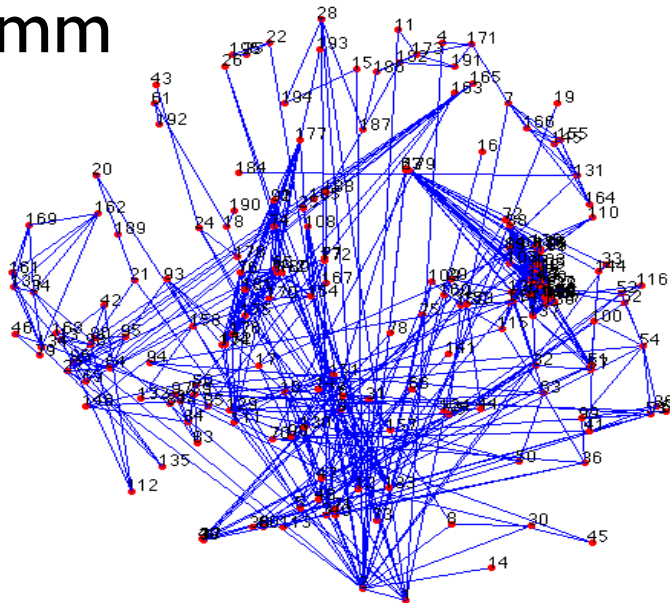
original  
data



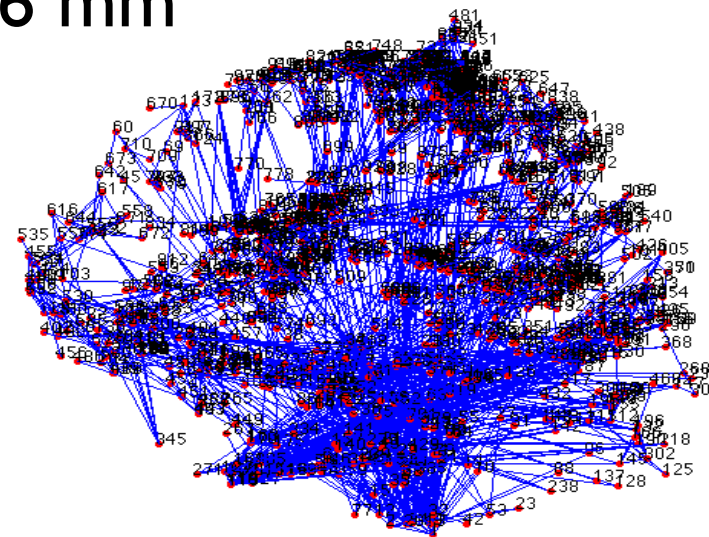
20 mm



10 mm

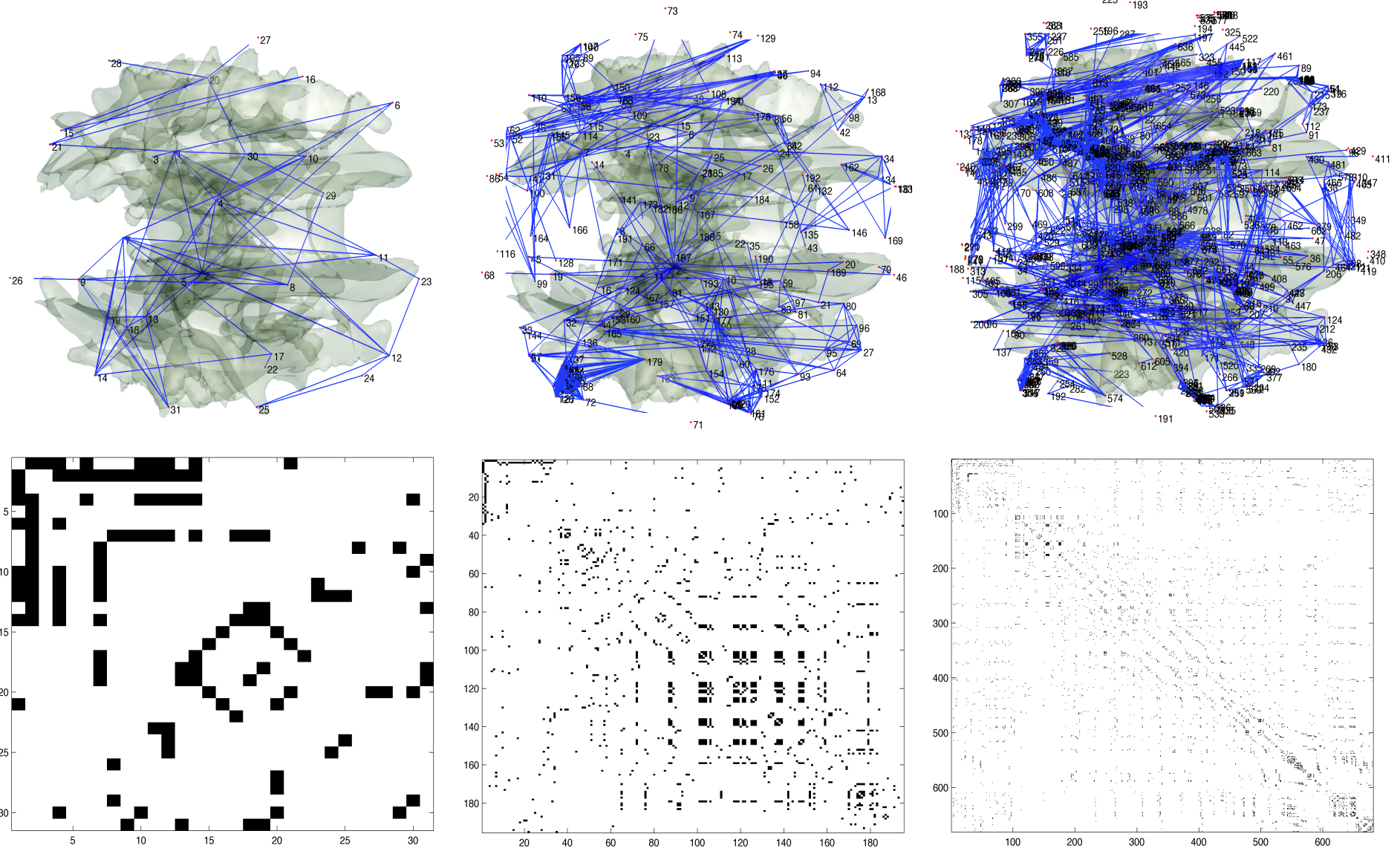


6 mm





# Adjacency matrix



# Application to autism

Autistic children (n=17)

Control subjects (n=14)

Matched for age, handedness, IQ and head size

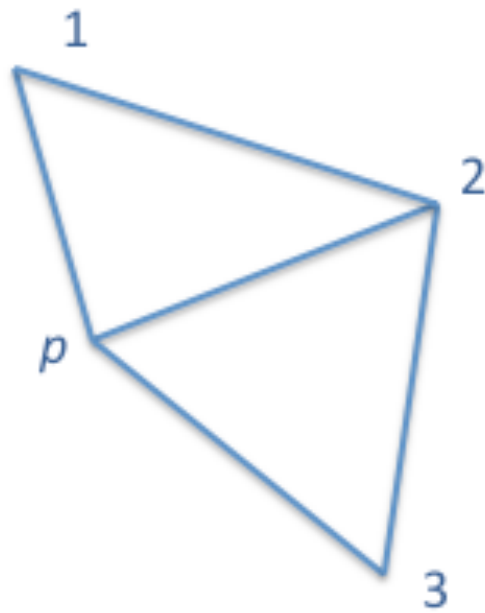


## Clustering coefficient

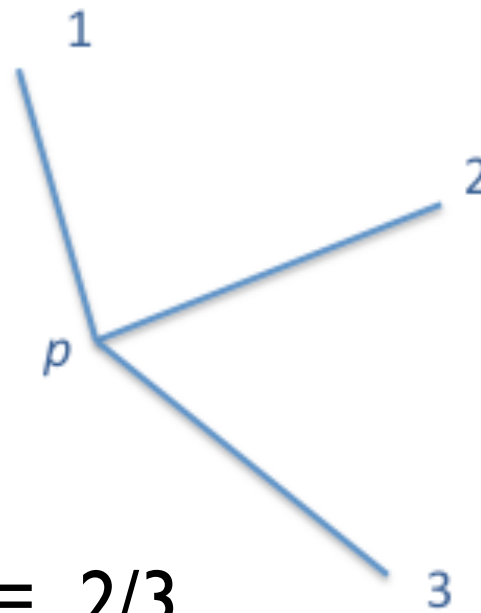
Newman et al., (2001)

At a given node  $p$ , there are  $k$  number of neighboring nodes.

$$c(p) = \frac{\text{actual number of edges}}{k(k-1)/2}$$

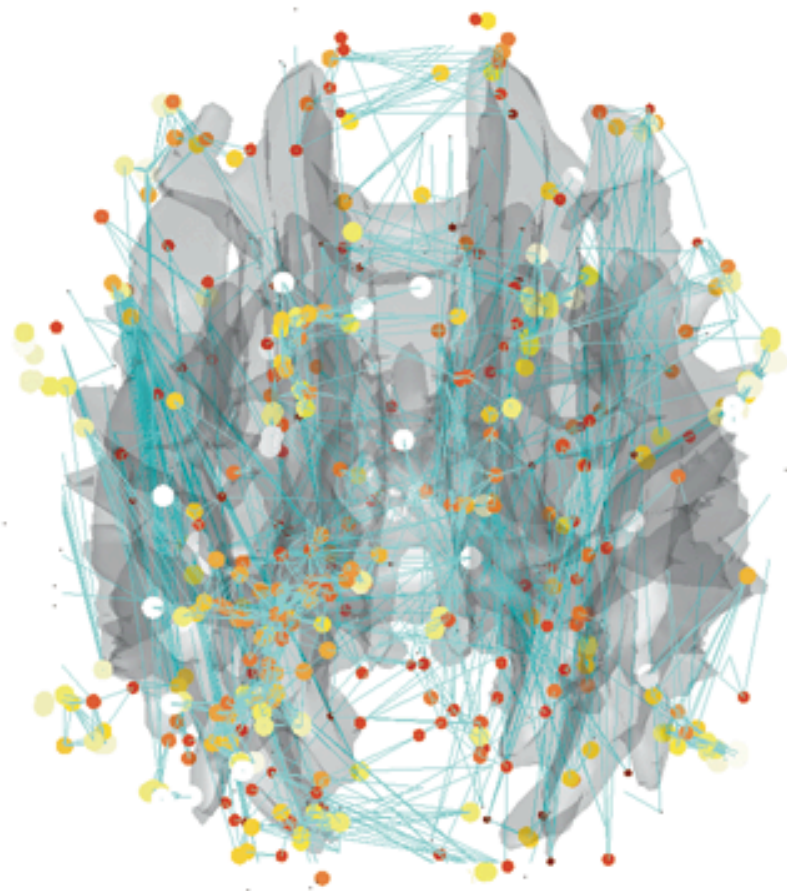


$$C(p) = 2/3$$

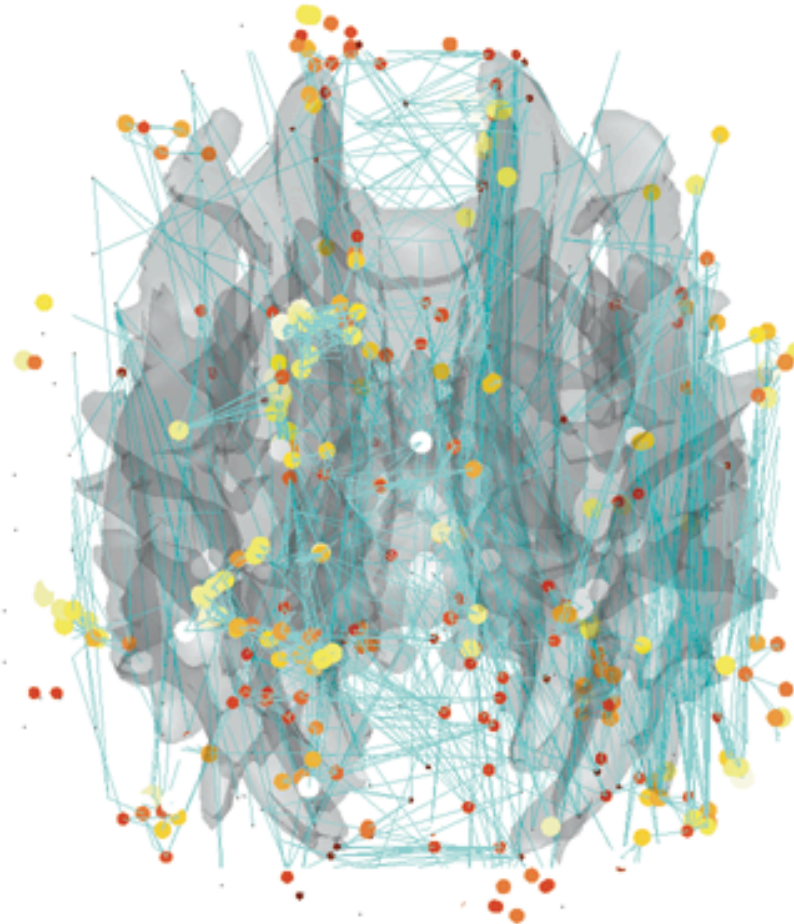


$$C(p) = 0/3$$

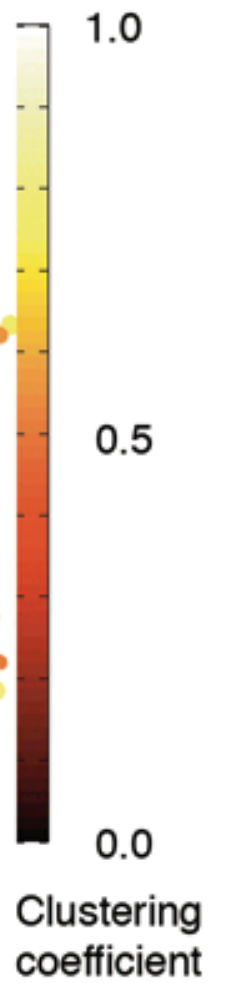
# Clustering coefficient



control 001

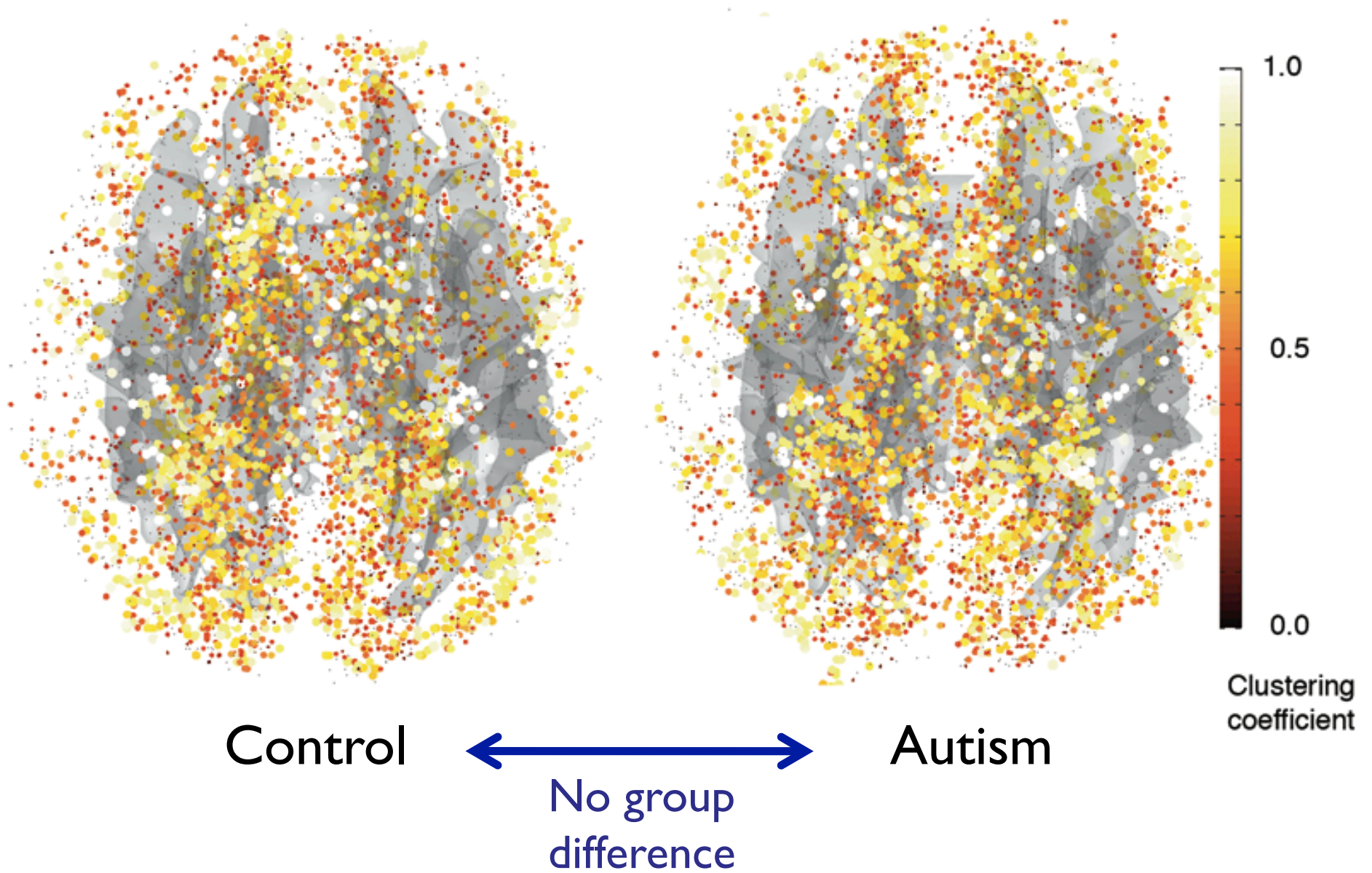


autism 120

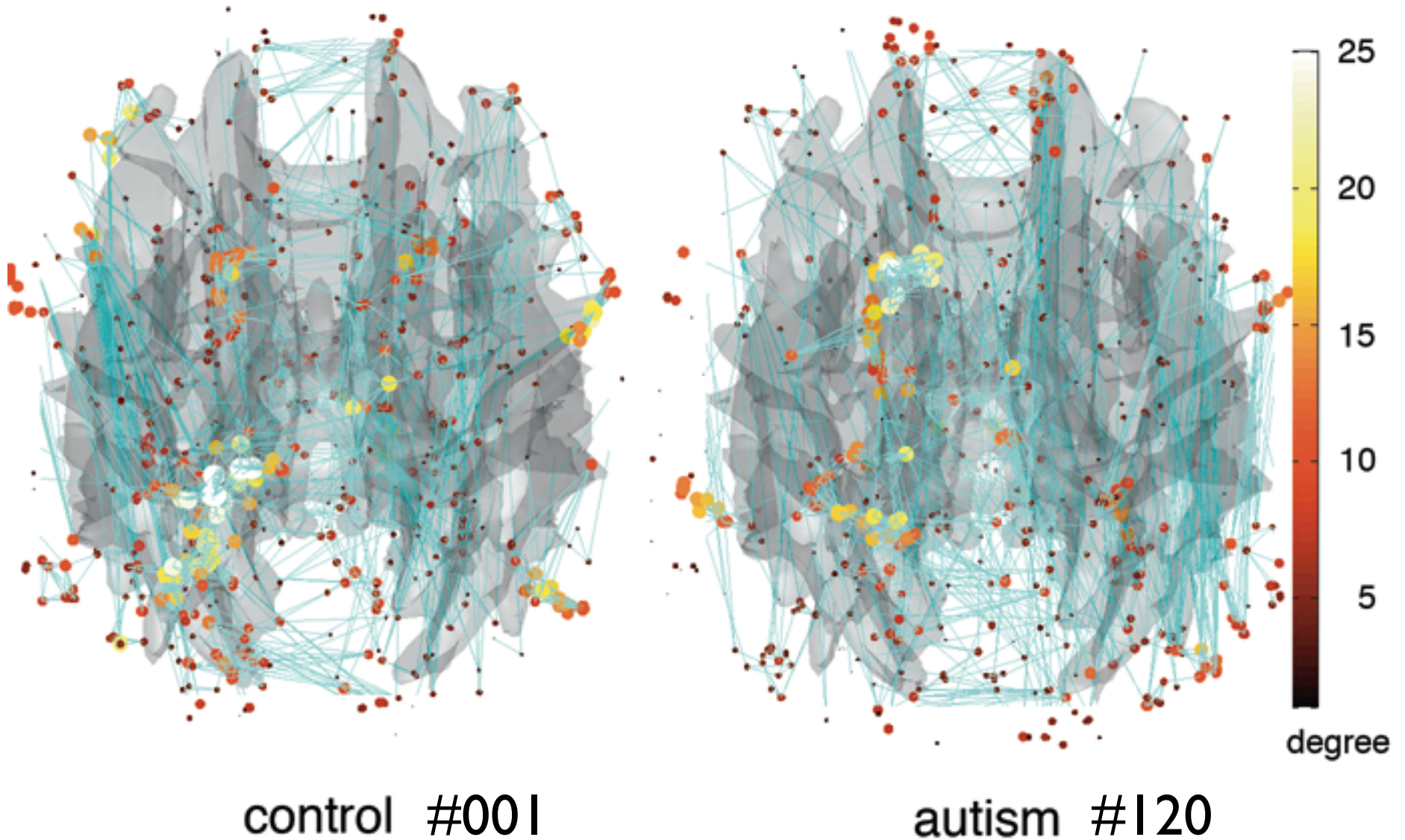




# Clustering coefficients for all subjects



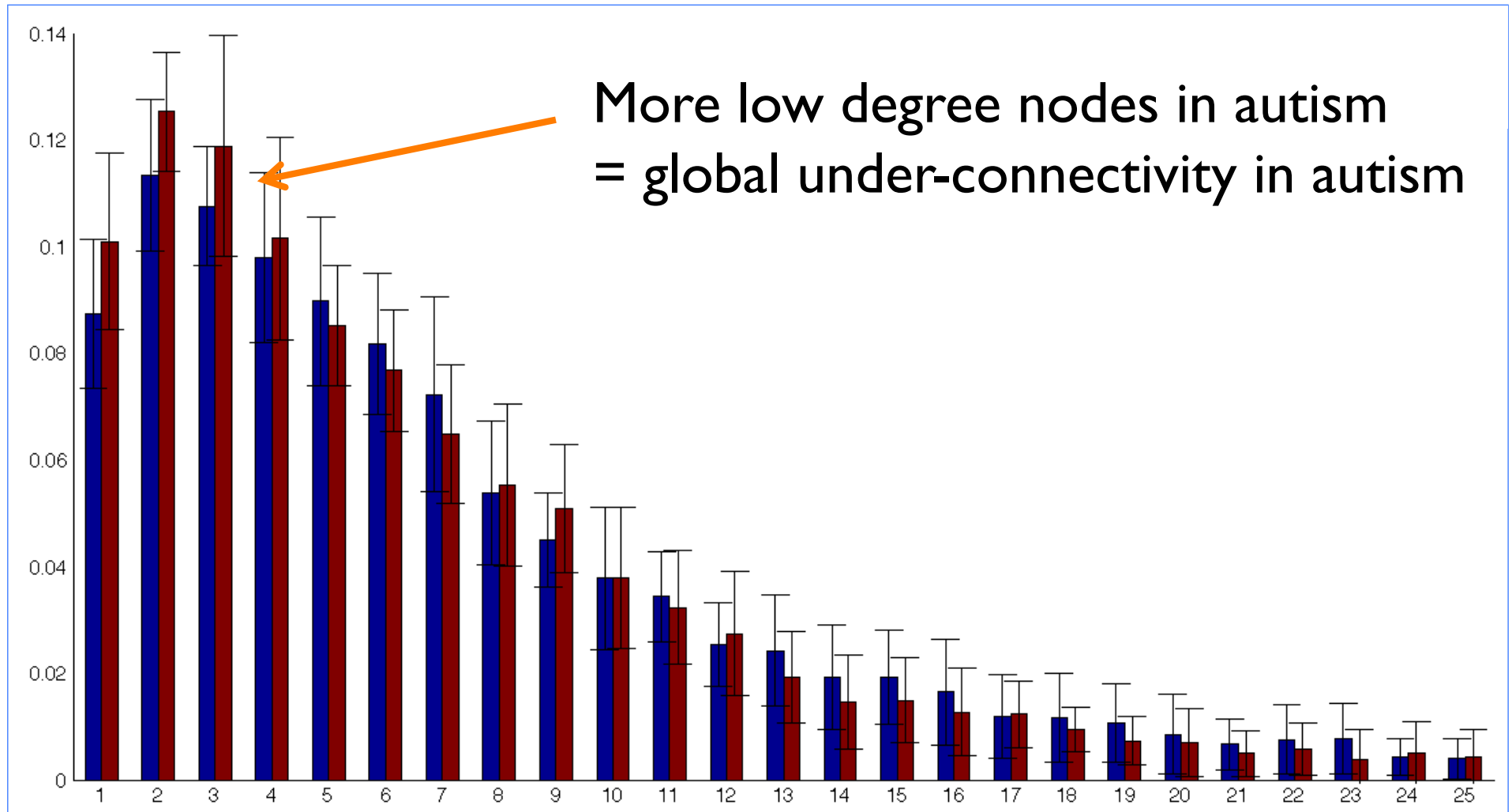
## Degree of nodes: measure of local network complexity





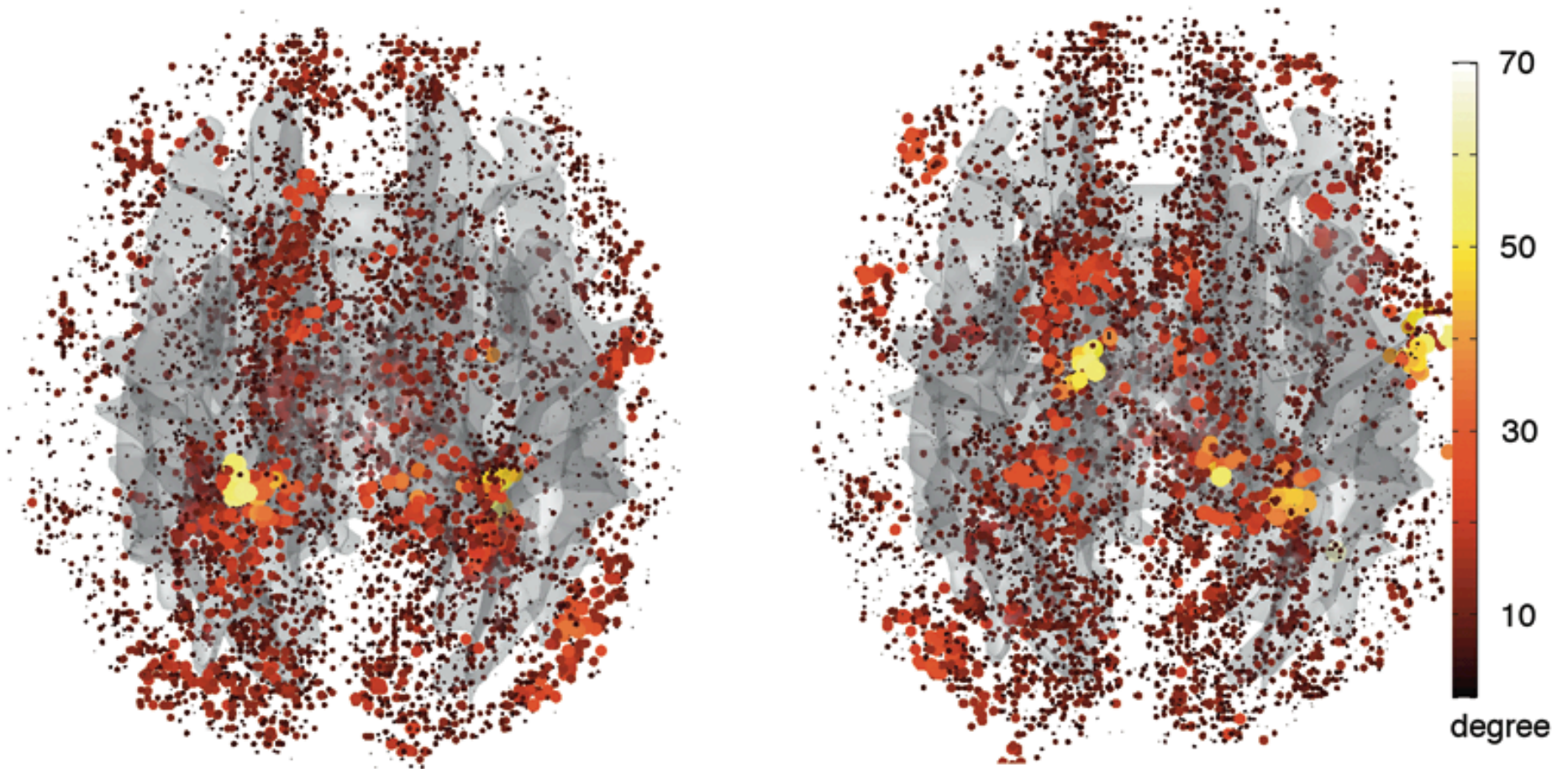
# Global degree distribution

red: autism  
blue: control



pvalues = 0.024, 0.015 and 0.080 for degrees 1, 2 and 3.

## Local degree distribution for all subjects

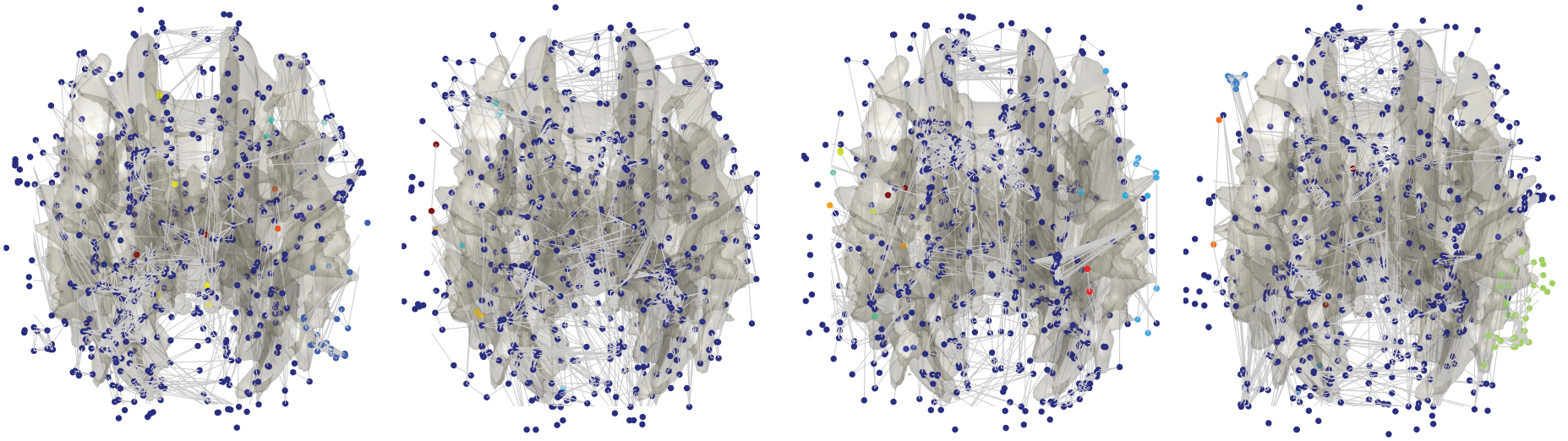


Control

Autism

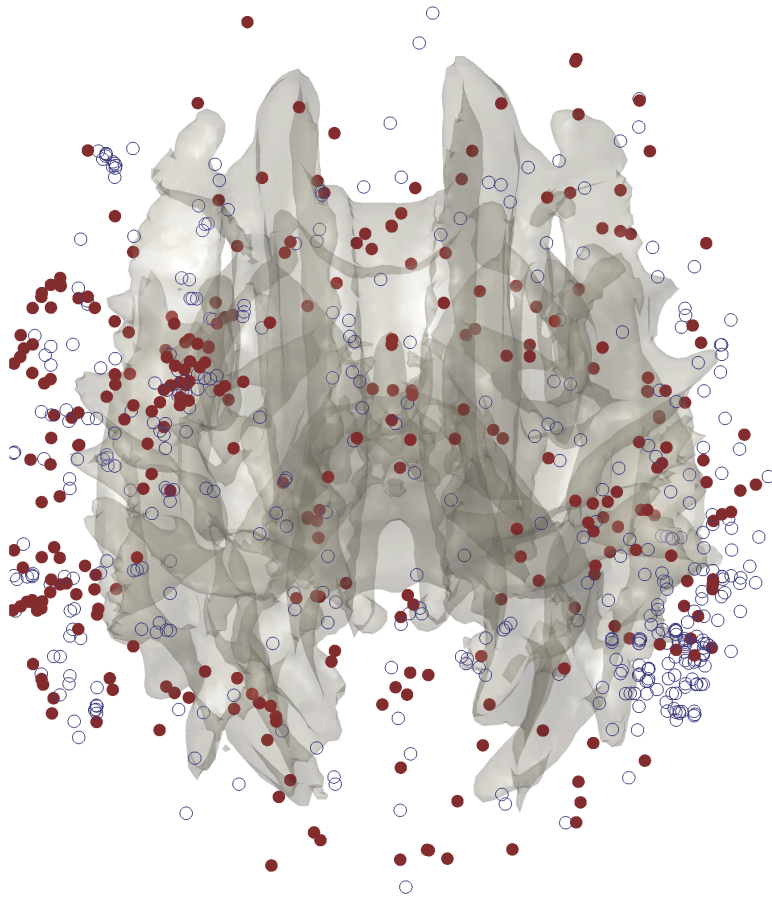


# Largest connected component



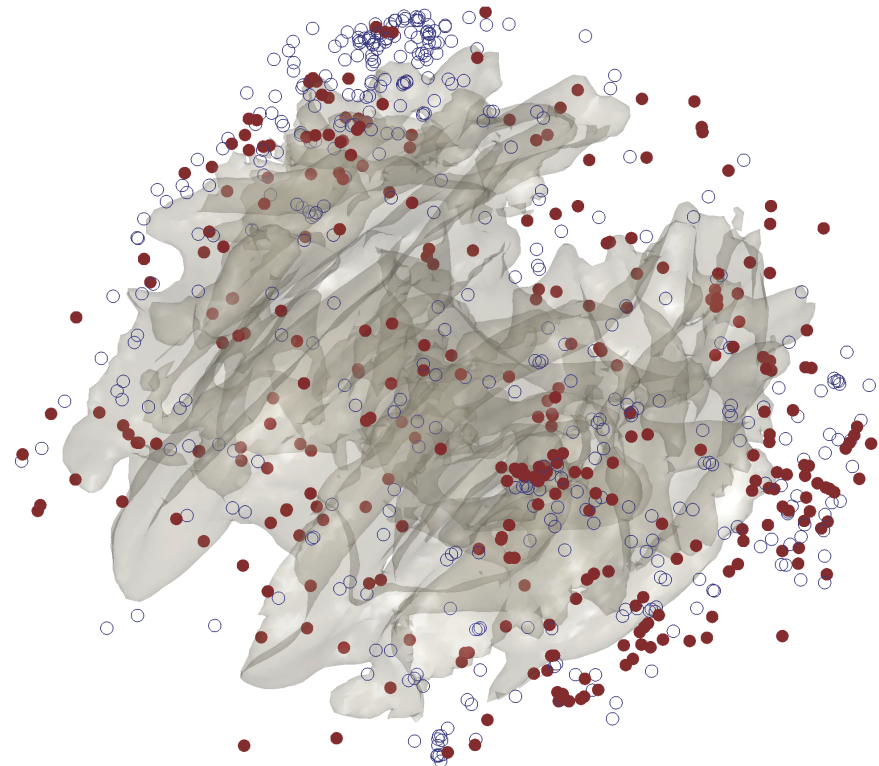
In average 96% of all nodes are connected to each other. We believe 100% of all nodes are supposed to be connected. 4% is a processing noise caused by weak connections.

# Group difference in disconnected components



Control=blue

Autism=red

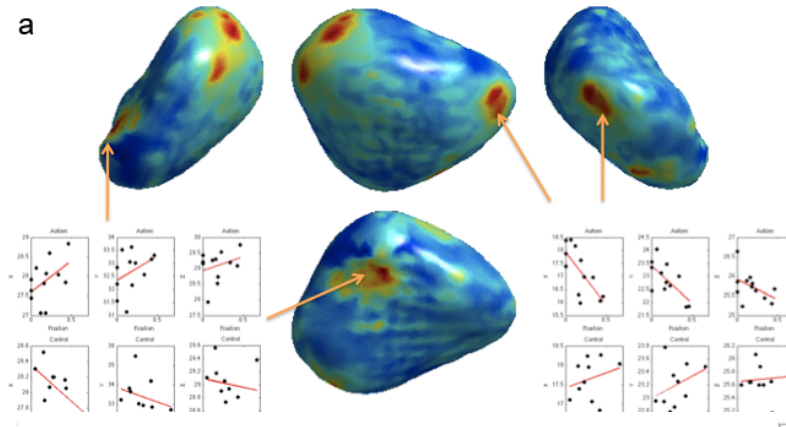


high clustering on the right parietal lobe  
(pvalue = 0.01)

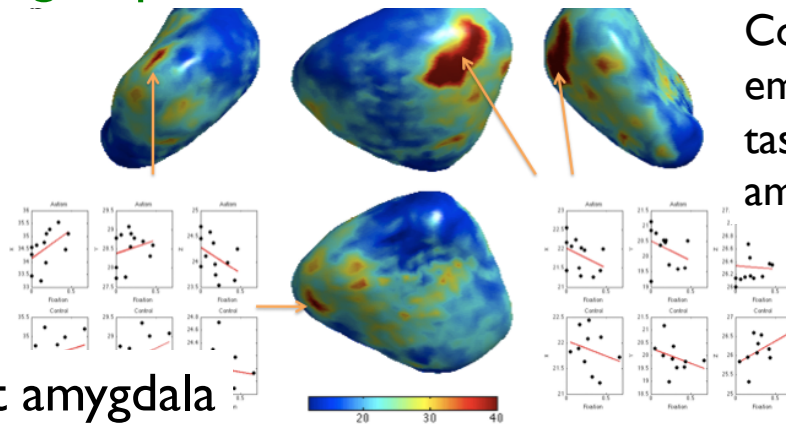


# Discussion

## Left amygdala



group difference at lateral nuclei



## Right amygdala

2 (Emotion)  $\times$  2 (Orientation)  
Neutral Emotional



Straight-ahead



Quarter-turned

Correlating facial  
emotion discrimination  
task response and  
amygdala shape

Amygdala networks correlated with behavioral measures

# Thank you

